



# Compiler Design



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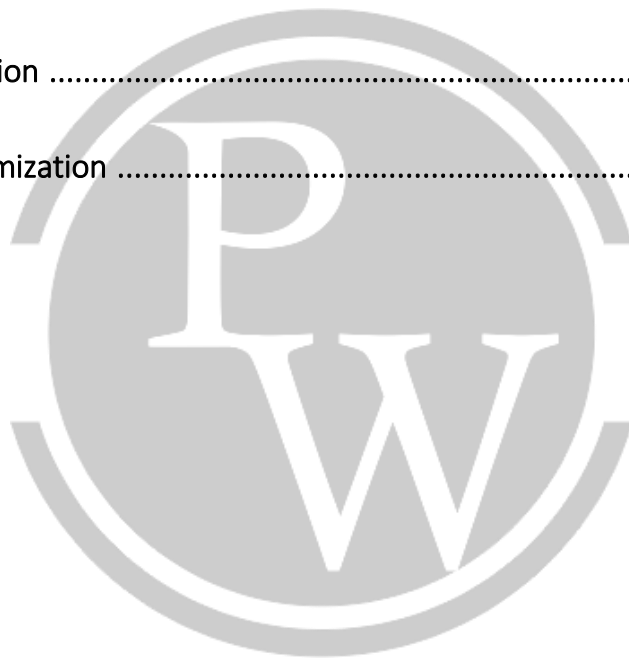
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# Compiler Design

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# 1

# INTRODUCTION AND LEXICAL ANALYSIS

## 1.1 CD Introduction

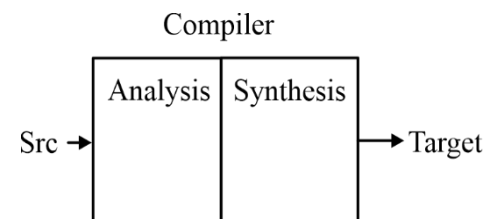
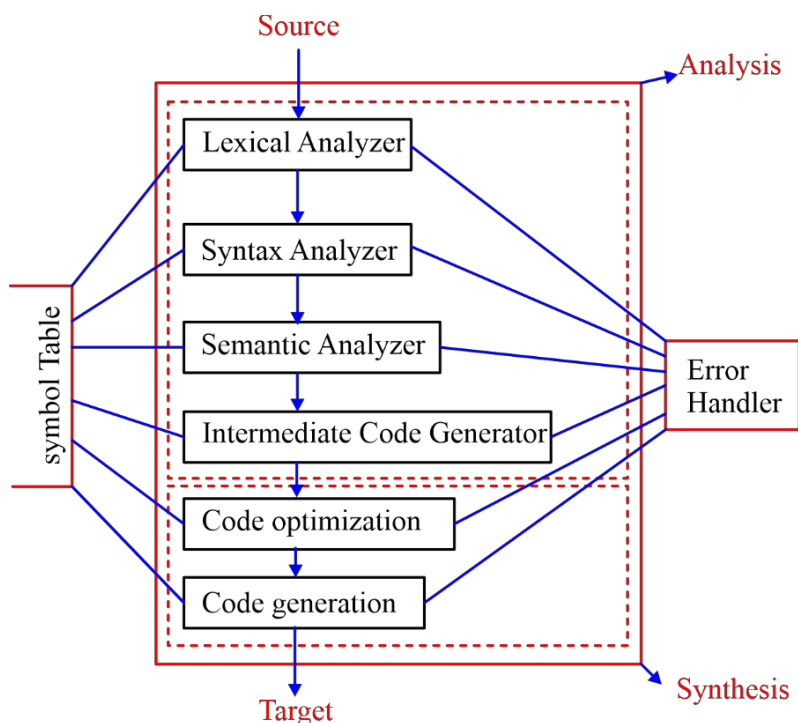
### 1.1.1 Definition

Convert High Level Language to Low Level Language.



- High Level Language can perform more than one operation in a single Statement.
- Low Level Language can perform at most one operation in a statement.

## 1.2 Analysis and Synthesis model of Compiler



- There are 6 phases of the Compiler





**1. Lexical Analyzer:**

- Program of DFA, it checks for spelling mistakes of program.
- Divides source code into stream of tokens.

**2. Syntax Analyzer:**

- Checks grammatical errors of the program (Parser).
- Parser is a DPDA.

**3. Semantic Analyzer:**

Checks for meaning of the program.

**Example:**

Type miss match, stack overflow

**4. Intermediate Code Generation:**

- This phase makes the work of next 2 phases much easier.
- Enforces reusability and portability.

**5. Code optimization:**

- Loop invariant construct
- Common sub expression elimination
- Strength Reduction
- Function in lining

Deadlock elimination

**6. Symbol Table:**

- (1) Data about Data (Meta data)
- (2) Data structure used by compiler and shared by all the phrase.



# 2

# PARSING

## 2.1 CD - Grammar

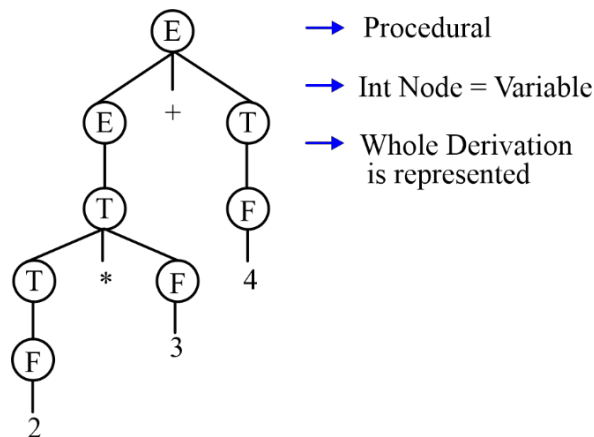
- In compiler we only use: Type – 2 (CFG) and Type – 3 Regular grammar.
- Compiler = Program of Grammar
- Compiler = Membership algorithm
- Every programming Language is Context Sensitive Grammar (Context Sensitive Language)

### 2.1.1 Parse Tree and Syntax Tree

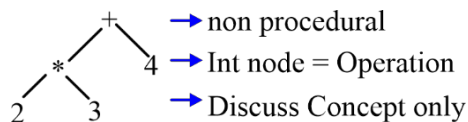
G:  $E \rightarrow E + T / T$      $E \rightarrow E + T \rightarrow T + T \rightarrow T * F + T \rightarrow F * F + T \rightarrow 2 * F + T \rightarrow 2 * 3 + T \rightarrow 2 * 3 + F$   
 $T \rightarrow T * F / F$

$E \rightarrow 2 * 3 + 4$

**Parse Tree:**

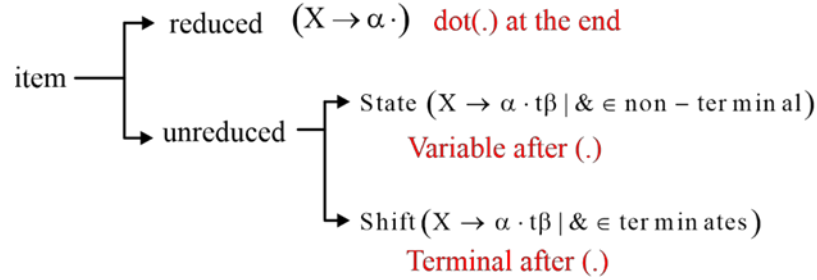


**Syntax Tree:**



- To check to priority / Associativity:  
Randomly derive till you have enough operators, then check which one is done first.
- If priority of 2 operators is same and both Left and Right associative → **Ambiguous Grammar** [Useless]

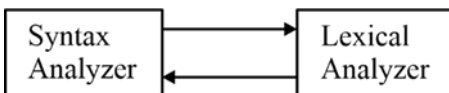
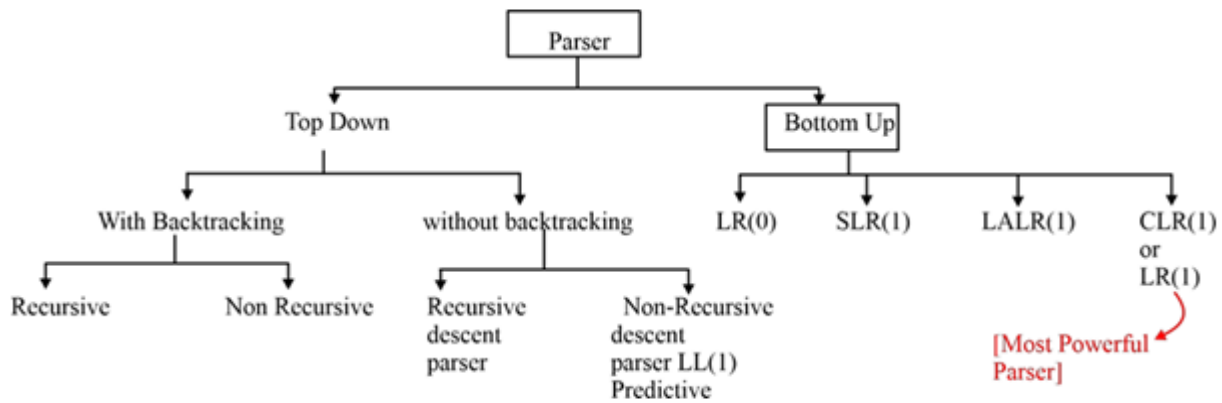
## 2.1.2 Types of Parsers in Bottom Up: [CD - Parser]



## 2.2 CD-Syntax Analysis / Parsing

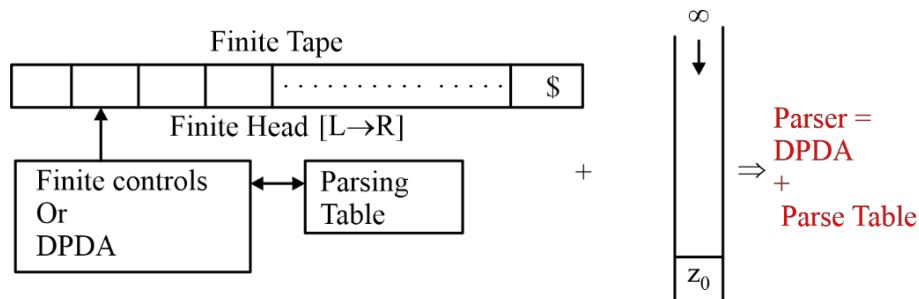
Grammatical Errors are checked by the help of parsers.

- Parsers are basically DPDA



- All of these parsers are table driven.

### 2.2.1 Mathematical Model of Parser



- Parsers generate Parse Tree, for a given string by the given grammar.

### 2.2.2 Top-Down Parser (LL (1))

- It uses LMD and is equivalent to DFS in graph.

### 2.2.3 Algorithm to construct Parsing Table

1. Remove Left Recursion if any.
  2. Left Factor [Remove Common Prefix]
  3. Find first and follow set
  4. Construct the table.
- If we increase the look ahead symbol:

### 2.2.4 Removal of common Prefix: (Left Factor)

1.  $S \rightarrow a \mid a b \mid a A$   $S \rightarrow a Y$   
 $Y \rightarrow \epsilon \mid b \mid A$
2.  $A \rightarrow a b A \mid a A \mid b$   
 $A \rightarrow a \times \mid b$   $A \rightarrow a \times \mid b$   
 $X \rightarrow b A \mid A$   $X \rightarrow b A \mid a x \mid b$   
 $A \rightarrow a X \mid b$   
 $X \rightarrow a X \mid b$   
 $Y Y \rightarrow A \mid \epsilon$

### 2.2.5 First and Follow

- First Set  $\rightarrow$  extreme Left terminal from which the string of that variable starts.  
 $\rightarrow$  it never contains variable, but may contain ' $\epsilon$ '.  
 $\rightarrow$  we can always find the first of any variable.
- Follow set  $\rightarrow$  Follow set contains terminals and \$.  
It can never contain variable and ' $\epsilon$ '.  
How to find follow set?  
  1. Include \$ in follow of start variable.
  2. If production is of type  $\rightarrow$   
 $A \rightarrow \alpha B \beta$   $\alpha \beta \rightarrow$  strings of grammar symbol].  
 $\text{follow}(B) = \text{first}(\beta)$ .  
If,  $\beta \rightarrow \epsilon$ , i.e.  $A \rightarrow \alpha B$ , then  $\text{follow}(B) = \text{follow}(A)$ .
- Productions like:  $A \rightarrow \alpha A$  gives no follow set.

## 2.2.6 Example of first and follow set

- $S \rightarrow AB \mid CD$   
 $A \rightarrow aA \mid a$   
 $B \rightarrow bB \mid b$   
 $C \rightarrow cC \mid c$   
 $D \rightarrow dD \mid d$

	First	Follow
S	a, c	\$
A	a	b
B	b	\$
C	c	D
D	D	\$

## 2.2.7 Entity into Table: Top Down

- No of Rows = number of unique variable in Grammar.
  - No of columns = [Terminals + \$]
  - For a Variable (Row) fill the column (Terminal) if its P, there in its first with the production required.
  - If  $\epsilon$  is in first put  $V \rightarrow \epsilon$  under \$ and its follow.
- If any cell has multiple items, then its not possible to have LL (1) Parser, since that will be ambiguous.
  - In top down we do: Derivation  
In Bottom up we do: Production.

**Question:** Construct LL (1) Parsing Table for the given Grammar:  $E \rightarrow E + T \mid T$ ;  $T \rightarrow T * F \mid F$ ;  $F \rightarrow (E) \mid id$ ;  $\Rightarrow G_0$

$\Rightarrow$  Removing Left Recursion:

$E \rightarrow TE'$

$E' \rightarrow + TE' \mid \epsilon$

$T \rightarrow FT' \quad G_1$

$T' \rightarrow * FT' \mid \epsilon$

$F \rightarrow (E) \mid id$

	First	Follow
E	C, id	\$, )
E'	+, $\epsilon$	\$, )
T	C, id	+, \$, )
T'	*, $\epsilon$	+, \$, )
F	C, id	*, +, \$, )

- Left Factoring not Required:  
Construction of Table: [LL (1)]

	+	*	(	)	id	\$
E	Error	Error	$E \rightarrow TE'$	Error	$E \rightarrow TE'$	Error
E'	$E' \rightarrow TE'$	Error	Error	$E' \rightarrow \epsilon$	Error	$E' \rightarrow \epsilon$
T	Error	Error	$T \rightarrow FT'$	Error	$T \rightarrow FT'$	error
T'	$T' \rightarrow \epsilon$	$T' \rightarrow * FT'$	Error	$T' \rightarrow \epsilon$	Error	$T' \rightarrow \epsilon$
F	Error	Error	$F \rightarrow (E)$	Error	$F \rightarrow id$	error

- Since for  $G_1$ , Table constructed with no multiple entries. Hence successfully completed. Hence  $G_1$  is LL (1)

**Question:** Construct LL (1) Parsing Table for the following Grammar:

$S \rightarrow L = R \mid R$ ;  $L \rightarrow * R \mid id$ ;  $R \rightarrow L \Rightarrow G_0$

**Solution:** Left Factoring:

$$\begin{aligned}
 S &\rightarrow L = R \mid L & S &\rightarrow LX \\
 L &\rightarrow *R \mid id & \Rightarrow & \times \Rightarrow = R \mid \in \\
 R &\rightarrow L & L &\rightarrow *R \mid id \\
 & & R &\rightarrow L
 \end{aligned}
 \Rightarrow G_1$$

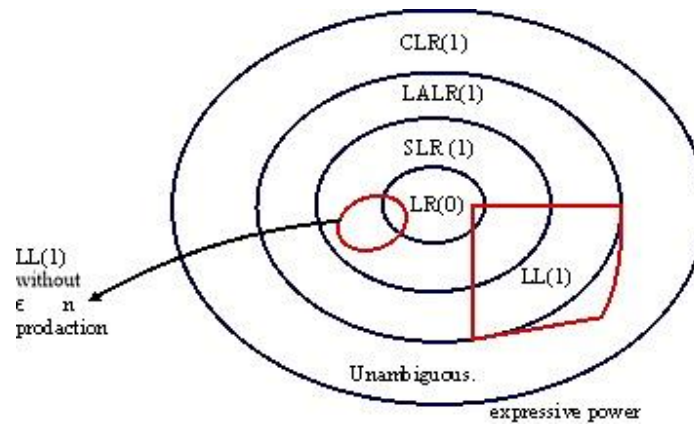
	First	Follow
S	*, id	\$
×	=, ∈	\$
L	*, id	\$
R	*, id	\$

Construction of Table:

	*	=	Id	\$
S	S→LX	Error	S→L X	Error
L	L→*R	Error	L→id	Error
R	R→L	Error	R→L	Error
×	Error	X→ = R	Error	X→∈

- $G_1$  is a LL (1) Grammar.

## 2.2.8 Hierarchy of Parsers: [for $\epsilon$ - free Grammar]



- For  $\epsilon$ -producing grammars every LL (1) may not be LALR (1).

### Note:

We can't construct any parser for ambiguous grammar. Except: Operator precedence, parser possible for some ambiguous grammar.

### Example:

$G: S \rightarrow a S a \mid b S b \mid a \mid b$  (Unambiguous but no parser)  $L(G) = \omega(a + b) \omega R$   
(Odd palindrome)

- Every RG is not LL (1) as it may be ambiguous, or Recursive or Common Prefix.
- Parsers exists only for the grammar if its Language is DCFL.
- There are some grammars whose Language is DCFL but no parser is possible for it.



### 2.4.9 Operator Precedence Grammar

Format: (1) No 2 or more variable side by side  
(2) No  $\in$  production.

**Example:**

$$\begin{array}{lll} E \rightarrow E + T \mid T & E \rightarrow E * E & \\ T \rightarrow T * F \mid F & S \rightarrow aSa \mid bSb \mid a \mid b & \\ F \rightarrow (E) \mid id & E \rightarrow a / b & \text{O.G.} \\ \text{O.G.} & \text{O.G.} & \\ & \text{Or} & \\ S \rightarrow AB & & \\ A \rightarrow aA \mid \in & \text{Not O.G.} & \\ B \rightarrow bB \mid \in & & \end{array}$$

### 2.2.10 Checking LL (1) without Table

$$\begin{array}{ll} A \rightarrow \alpha_1 | \alpha_2 | \alpha_3 \text{ then } \rightarrow & A \rightarrow \alpha_1 | \alpha_2 | \alpha_3 | \in \\ \text{first}(\alpha_1) \cap \text{first}(\alpha_2) = \emptyset & \text{first}(\alpha_1) \cap \text{first}(\alpha_2) = \emptyset \\ \text{first}(\alpha_1) \cap \text{first}(\alpha_3) = \emptyset & \text{first}(\alpha_1) \cap \text{first}(\alpha_3) = \emptyset \\ \text{first}(\alpha_2) \cap \text{first}(\alpha_3) = \emptyset & \text{first}(\alpha_2) \cap \text{first}(\alpha_3) = \emptyset \\ & \text{follow}(A) \cap \text{first}(\alpha_1) = \emptyset \\ & \text{follow}(A) \cap \text{first}(\alpha_2) = \emptyset \\ & \text{follow}(A) \cap \text{first}(\alpha_3) = \emptyset \end{array}$$

### 2.2.11 Bottom-UP Parser

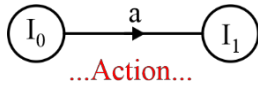
- It uses RMD in reverse and has no problem with:
  - (a) Left recursion (b) Common Prefix
- SLR (1) LR (0) CLR (1) LR (1)
- LR (0) items LALR (1) items
- LR (1) = LR(0) + 1 Lookahead
- No parser possible for ambiguous grammar.
- There are some unambiguous grammars for which, there are no Parser.

### 2.2.12 Basic Algorithm for Construction

- Augment the grammar and expand it, and give numbers to it
- Construct LR (0) or LR (1) item set.
- From that fill the entries in the Table Accordingly.

### 2.2.13 Types of Entries

(1) **Shift Entries:** Transitions or Terminals



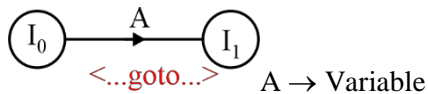
**Entry:**

	a
I <sub>0</sub>	S <sub>1</sub>

$a \in \text{Terminal}$   $I_0, I_1$ : Item sets.

- Shift entries are some for all Bottom – up Parser.

(2) **State Entry:** Transition or non – terminal (variable)



**Entry:**

	A
I <sub>0</sub>	1

- Same for all Bottom-up Parser.

(3) **Reduce Entity:** done for each separate production in the item set of type:

$$i > \times \rightarrow \alpha$$

where,  $i \rightarrow \text{Production Number}$

$\times \rightarrow \text{Producing Variable}$

$\alpha \rightarrow \text{Grammar String}$

(a) LR (0) Parser:

Put  $R_i$  in every cell of the set-in action table (**ALL**).

(b) SLR (1) Parser:

Put  $R_i$  only in the follow(x) form the Grammar. (**Follow(x)**)

(c) LALR (1) and CLR (1):

Put  $R_i$  only in the look ahead of the production (**Lookaheads**)

### 2.2.14 Conflicts

#### LR (0) Parser:

**SR:** Shift Reduce Conflict

$S \rightarrow X \rightarrow \alpha \cdot t\beta \Rightarrow$  then SR

$R \rightarrow Y \rightarrow \delta \cdot$  conflict

**RR:** Reduce Reduce conflict

$R \rightarrow X \rightarrow \alpha \cdot \Rightarrow$  then RR

$R \rightarrow X \rightarrow \beta \cdot$

#### SLR (1) Parser:

**SR:**

$S \rightarrow X \rightarrow \alpha \cdot t\beta \quad \$ \Rightarrow$  then SR

$R \rightarrow Y \rightarrow \delta \cdot$  conflict

$t \in \text{follow}(Y)$

**RR:**

$X \rightarrow \alpha \cdot \quad \$ \Rightarrow$  then RR

$Y \rightarrow \beta \cdot$

$\text{Follow}(X) \cap \text{follow}(Y) \neq \emptyset$

LALR (1) and CLR (1): Same as SLR (1), but instead

**SR:**

$X \rightarrow \alpha \cdot t\beta \cdot L_1 \quad \$ \Rightarrow$  then SR

$Y \rightarrow \delta \cdot L_2$  conflict

$T \in L_2$

**RR:**

$X \rightarrow \alpha \cdot, L_1 \quad \$$  then RR

$Y \rightarrow \beta \cdot, L_2$  conflict

$L_1 \cap L_2 \neq \emptyset$

### 2.4.15 Inadequate Static

A static having ANY conflict is called a conflicting state or independent state.

**Note:**

The state  $S' \rightarrow S$  or  $S' \rightarrow S, \$$  is accepted state, and this is not a reduction.

- The only difference between CLR (1) and LALR (1) is that, the states with the similar items, but different Lookaheads are merged together to Reduce space.

### Important Points

- If CLR (1) doesn't have any conflict, then conflict may or may not arise after merging in LALR (1).
- If LALR (1) has SR – conflict, then we can conclude that CLR (1) also has SR – Conflict.
- LALR (1) has SR – conflict if and only if CLR (1) also has SR.



- We can construct parser for every unambiguous regular grammar: [CLR (1) Parser].

	<div>L Left to right scan of i/p</div>	<div>R Using reverse RMD</div>	<div>(0) No Lookahead</div>	
S	L	R	(1)	
Simple	L to R Scan	Using Reverse RMD	Lookahead	
L	A	L	R	(1)
Look	Ahead	L to R Scan	Revers RMD	Lookahead
C	L	R	(1)	
Canonical	L to R Scan	reverse RMD	Lookahead	

**Very Important Point:**

LALR (1) Parser can Parse non LALR (1) grammar, when only non-SR – Conflict by favouring shift over reduce.

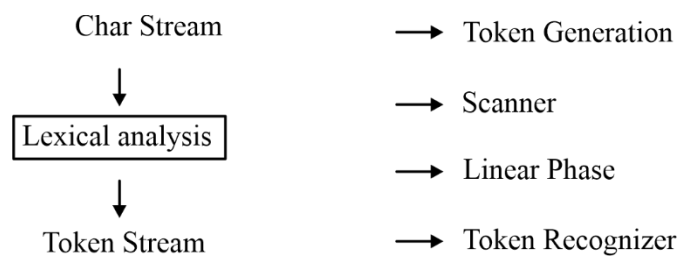
**Example:**  $E \rightarrow E + E \mid E * E \mid id \mid 2 + 3 * 5 \Rightarrow E + E \cdot * 5$



# 3

## LEXICAL ANALYSIS

### 3.1 Lexical Analysis



#### 3.1.1 Definition

Scan the whole program, char by char and produces the corresponding token.

- Also produces /Lexical Errors (if any).
- Functions of Lexical Analyzer.
  - (1) Scans all the character of the program.
  - (2) Token recognizer.
  - (3) Ignores the comment & spaces.
  - (4) Maximal Munch Rule [Longest Prefix Match].

#### Note:

The Lexical Analyser uses, the Regular Expression.  
Prioritization of Rules.  
Longest Prefix match .

- Lexeme → smallest unit of program or Logic.
- Token → internal representation of Lexeme.

#### 3.1.2 Types of Token

- (1) Identifier
- (2) Keywords
- (3) Operators
- (4) Literals/Constants
- (5) Special Symbol

### 3.1.3 Token Separation

- (1) Spaces
- (2) Punctuation

### 3.1.4 Implementation

- LEX tool  $\Rightarrow$  Lex.yy.e
- All identifiers will have entry in symbol Table/ LA, gives entries into the symbol Table.  
Regular Expression  $\rightarrow$  DFA  $\rightarrow$  Lexical Analyzer

### 3.1.5 Find number of Tokens

- (1) `void main () {`  
`Printf("gate");`  
`}`  
 { 11 Tokens}
- (2) `int x, *P;`  
`x = 10; p = &x; x++;`  
 [18 Tokens]
- (3) `int x;`  
`x = y;`  
`x == y;`  
 [11 Tokens]
- (4) `int 1x23;` [Lexical Error]
- (5) `char ch = 'A';`  
 [5 Token]
- (6) `char ch = 'A;`  
 Lexical Error.
- (7) `char *p = "gate";`  
 [6 Tokens]
- (8) `char * p = "gate;`  
 Error.
- (9) `int x = 10;`  
`/* comment x = x + 1; ERROR`  
`x = x + 1; [11 Tokens]`





# 4

# SYNTAX DIRECTED TRANSACTION

## 4.1 Syntax Directed Transaction

CFG + Transition } SDT  
Syntax + Transition }

**SDT: CFG + Transition → 1) Meaning 2) Semantic**

### 4.1.1 Application of SDTL

- (1) Used to perform Semantic Analysis.
- (2) Produce Parse Tree.
- (3) Produce intermediate representation.
- (4) Evaluate an expression.
- (5) Convert infix to prefix or postfix.

**Example:**  $S \rightarrow S_1 S_2$  [ $S.\text{count} = S_1.\text{count} + S_2.\text{count}$ ]

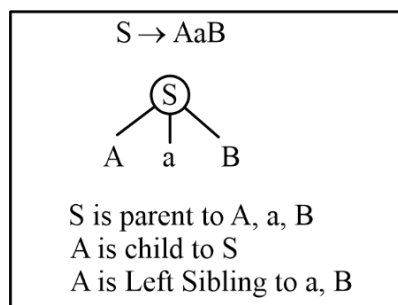
$S \rightarrow (S_1)$  [ $S.\text{count} = S_1.\text{count} + 1$ ]

$S \rightarrow \epsilon$  [ $S.\text{count} = 0$ ]

- Count is an attribute for non-terminal

### 4.1.2 Attributes

- (1) Inherited Attribute
- (2) Synthesized Attribute



- (1) Inherited Attribute: (RHS)

$S \rightarrow \boxed{A} B$   $\{A.x = f(B.x \mid S.x)\}$

- The computation at any node (non-terminal) depends on parent or siblings (S).

- In above Example, x is inherited attribute.

(2) **Synthesized Attribute: (LHS)**

$$S \rightarrow AB \{S.x = f(A.x \mid B.x)\}$$

x is synthesized attribute.

The computation at any node (non-terminal) depends on children.

### 4.1.3 Identifying Attribute Type

- Always check every Translation.

- |   |   |  |
|---|---|--|
| 1) $D \rightarrow T : L ; \{L.Type = T.Type\}$ inherited<br>$L \rightarrow L1, id ; \{L1.Type = L.Type\}$ inherited<br>$L \rightarrow id$<br>$T \rightarrow integer \{T.Type = int\}$ synthesized   | } | Type is neither inherited nor synthesized                    |
| 2) $E \rightarrow E1 + T \{E.val = E1.val + T.val\}$ synthesized<br>$E \rightarrow T \{E.val = T.val\}$ Synthesized<br>$T \rightarrow T1 - F \{T.val = T1.val - F.val\}$ Synthesized<br>$F \rightarrow id \{F.val = id.val\}$ synthesized | } | Val is synthesized attribute                                 |
| 3) $S \rightarrow AB \{Aa = B.x; S.y = A.x\}$ x is inherited   y is synthesized<br>$A \rightarrow a \{A.y = a\}$ y is synthesized<br>$B \rightarrow b \{B.y = a.y\}$ y is synthesized   | } | $x \Rightarrow$ inherited<br>$y \Rightarrow$ synthesized     |
| 4) $D \rightarrow T L \{L.in = T.type\}$ inherited(in)<br>$T \rightarrow int \{T.type = int\}$ /synthesized<br>$L \rightarrow id \{Add\ type(id.entry, L.in)\}$   | } | $in \Rightarrow$ inherited<br>$type \Rightarrow$ synthesized |

### 4.1.4 Syntax Directed Definitions (SDDs): (Attribute Grammar)

(1) **L-Attributed Grammar**

- Attribute is synthesized or restricted inherited. (1) Parent 2) Left sibling only).
- Translation can be appended anywhere in RHS of production.
- Example:  $S \rightarrow AB \{A.x = S.x + 2\}$   
 or,  $S \rightarrow AB \{B.x = f(A.x \mid S.x)\}$   
 or,  $S \rightarrow AB \{S.x = f(A.x \mid B.x)\}$
- Evaluation: In Order (Topological).

(2) **S-Attributed Grammar:**

- Attribute is synthesized only.
- The transaction is placed only at the end of production.
- Example:  $S \rightarrow AB \{S.x = f(Ax \mid Bx)\}$ .
- **Evaluation:** Reverse RMD (Bottom-Up Parsing).

### 4.1.5 Identify SDD

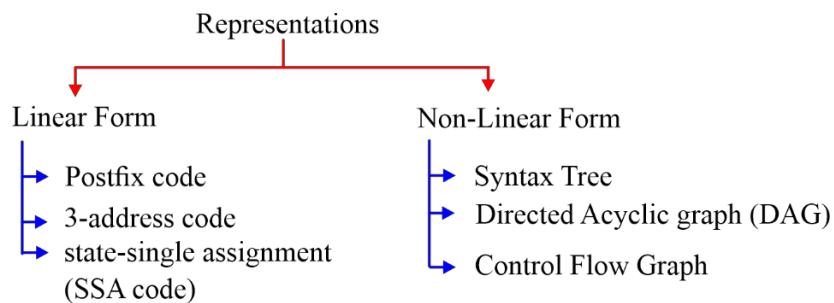
- (1)  $E \rightarrow E_1 + E_2$  {E.type = if (E<sub>1</sub>.type == int & & E.type == int) then int} Synthesizer else type – error.  
 $E \rightarrow id$  {E.type = Lookup (id.entry)} synthesizer.
- type is synthesized, hence S-attribute and also L-attributed Grammar.
  - Every S-attributed Grammar is also L-attributed Grammar.
  - For L-attributed Evaluation, use the In-order of annotated Parser Tree.
  - For S-attributed, reverse of RMD is used.
- find RMD Order.  
 → Consider its reverse.



# 5

# INTERMEDIATE, CODE OPTIMIZATION

## 5.1 Introduction



### Example Expression:

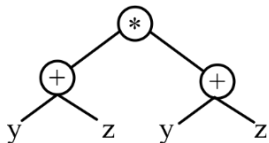
$(y + z) * (y + z)$

Post fix  $\rightarrow$   $yz + yz + *$

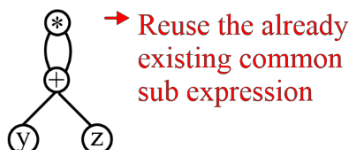
SSA  $\rightarrow$   $t_1 = y + z$   
 $t_2 = t_1 * t_2$   $\Rightarrow f_1$  and  $f_2$  cannot be reassigned

3AC  $\rightarrow$   $t_1 = y + z$   
 $t_2 = t_1 \times t_2$

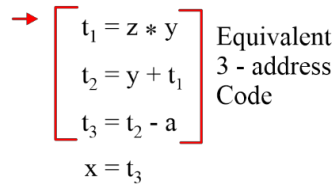
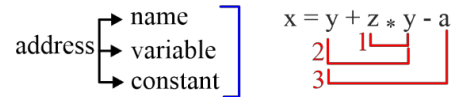
Syntax Tree  $\rightarrow$



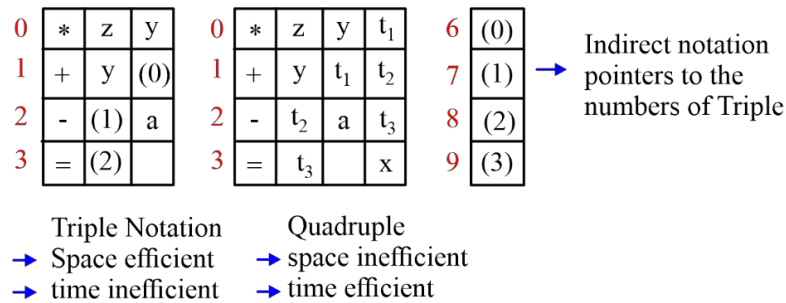
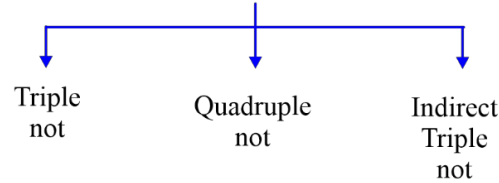
DAG  $\rightarrow$



**3-address Code:** Code in which, at most 3 addresses. [including LHS]

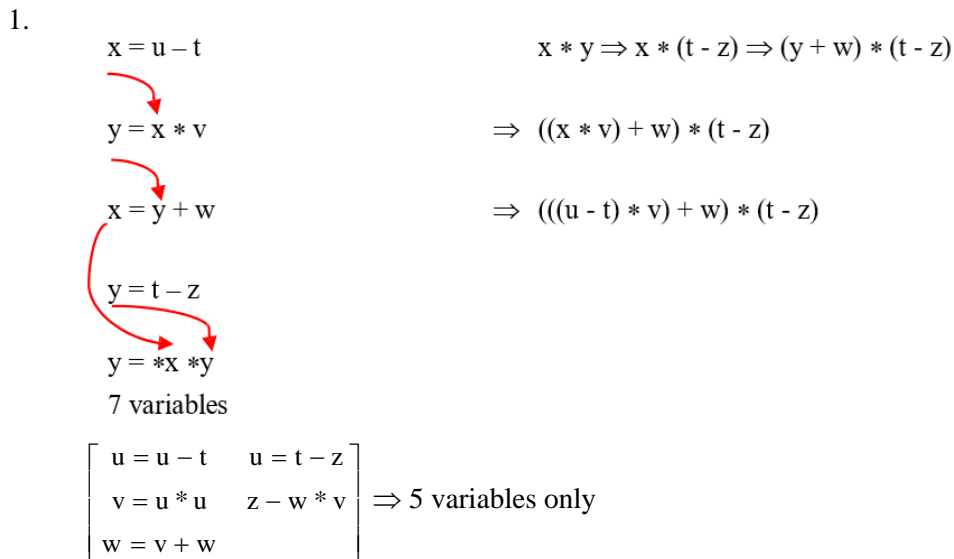


Representation of 3AC



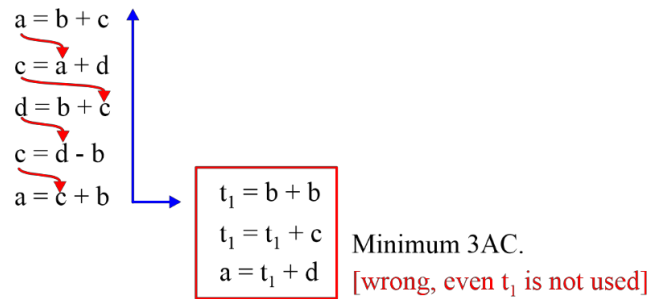
- 3AC done using operator precedence.

**Find minimum number of variables required in equivalent 3AC:**



⇒ Evaluating the expression:

$$\begin{aligned} a &\Rightarrow c + b \Rightarrow d - b + b \Rightarrow b + c - b + b \\ &\Rightarrow b + a + d - b + b \\ &\Rightarrow b + b + c + d - b + b \\ &\Rightarrow b + b + c + d \end{aligned}$$



∴ Minimum:

$$\left\{ \begin{array}{l} b = b + b \\ c = b + c \\ a = c + d \end{array} \right\} \Rightarrow \text{only 3 variables [most optimal]}$$

### 5.1.1 Static Single Assignment Code: (SSA Code)

Every variable (address) in the code has single assignment [single meaning] + 3AC.

1.  $x = u - t$   
 $y = x * u$   
 $x = y + w$   
 $y = t - z$   
 $y = x * y$

Find SSA?

⇒  $[u, t, v, w, z]$  are already assigned so we can't use them.

Equivalent SSA Code:

$x = u - t$   $y = x * u$

$p = y + w$

$q = t - x$

$r = p * q$

in use:  $x, y, p, q, r \Rightarrow$  additional

∴ Total Variable ⇒ 10.

2.  $p = a - b$

$q = p * c$

$p = u * v$

$q = p + q$

⇒  $[a, b, c, u, v]$  are already assigned,

Equivalent SSA Code:

$p = a - b$

$q = p * c$

$p_1 = v * u$

$q_2 = p_1 + q$

in use:  $p, q, p_1, q_2$

∴ Total Variable = 9



### 5.1.2 Control Flow Graphs

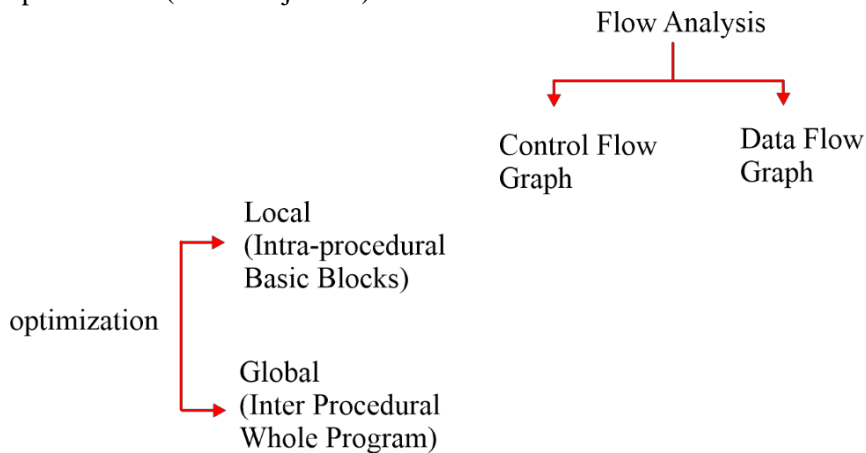
- CFG contain group of basic blocks and controls. CFG has nodes and edges to define basic blocks and controls.
- Basic Blocks: Sequence of 3-address code statements, in which control enters only from 1st statement (called as leader), and leaves from last statement.

**Example:**

1. $i = 1$	}	LB <sub>1</sub>
2. $j = 1$		LB <sub>2</sub>
3. $t1 = 5 * i$	}	LB <sub>3</sub>
4. $t2 = t1 + 5$		
5. $t3 = 4 * t2$		
6. $t4 = t3$		
7. $a[t4] = 1$	}	LB <sub>4</sub>
8. $j = j + 1$		
9. $\text{if } j \leq 5 \text{ goto } 3$	}	LB <sub>5</sub>
10. $i = i + 1$		
11. $\text{if } i < 5 \text{ goto } 2$	}	LB <sub>6</sub>

## 5.2 Code Optimization

Saves space / time. (Basic Objective)



### 5.2.1 Optimization Methods

- Constant folding
- Copy propagation
- Strength Reduction
- Dead code elimination
- Common sub expression elimination.
- Loop Optimization
- Peephole Optimization

### 1. Constant Folding

(i)  $x = 2 * 3 + y \Rightarrow x = 6 + y$

Folding

ii)  $x = 2 + y * 3$  can't fold the constant

### 2. Copy Propagation

i) Variable Propagation:

$x = y;$

$z = y + 2;$

$\Rightarrow z = x + 2;$

ii) Constant Propagation:

$x = 3$

$z = 3 + a;$

$\Rightarrow z = x + a$

### 3. Strength Reduction:

Replace expensive statement / instruction with cheaper one.

(i)  $x = 2 * y$  **costly**  $\Rightarrow x = y + y$ ; **Cheap**

(ii)  $x = 2 * y \Rightarrow x = y < 1$ ; **Much Cheaper**

(iii)  $x = y / 8 \Rightarrow x = y > 3;$

### 4. Dead Code Elimination:

$x = 2$ ; **FALSE**

if ( $x > 2$ )

printf("code"); **DEAD CODE CAN BE REMOVED**

else

printf("optimization");

$x = 2;$   
printf("optimization");

- Hence, above dead code never executes during execution. We can always delete such code.

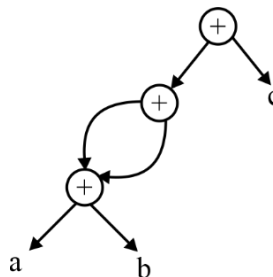
### 5. Common Sub Expression Elimination:

DAG is used to eliminate common sub expression.

**Example:**  $x = (a + b) + (a + b) + c;$

$\Rightarrow t_1 = a + b$

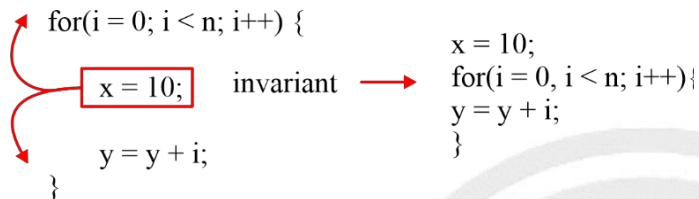
$x = t_1 + t_1 + c$



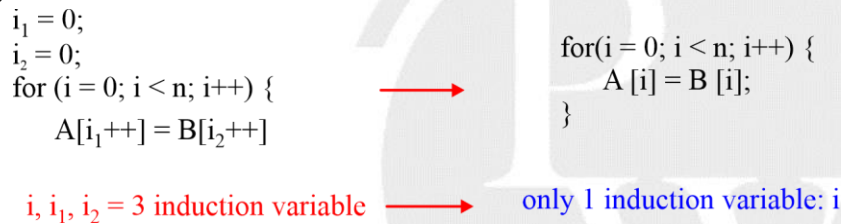
## 6. Loop Optimization:

### (i) Code Motion – Frequency Reduction:

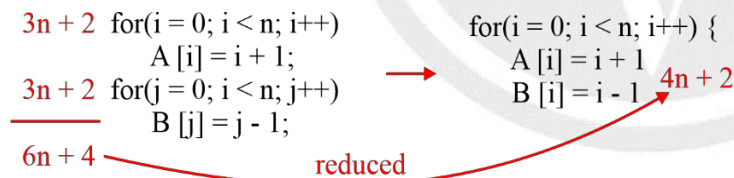
Move the loop invariant code outside of loop.



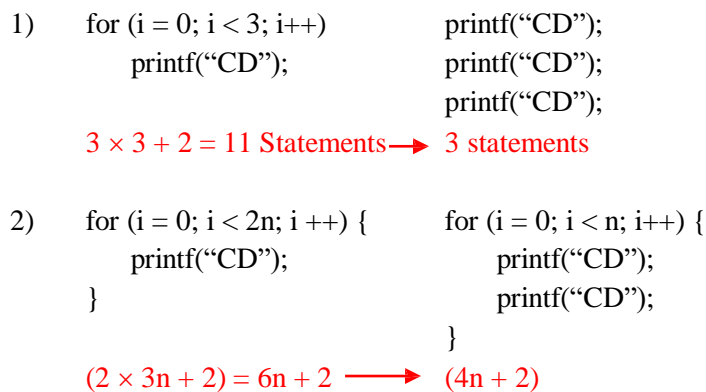
### (ii) Induction Variable elimination:



### (iii) Loop Merging / Combining: (Loop Jamming)



### (iv) Loop Unrolling:



## 7. Peephole Optimization:

Examines a short sequence of target instructions in a window (*peephole*) and replaces the instructions by a faster and/or shorter sequence when possible.

- Applied to intermediate code or target code
- Following Optimizations can be used:



- Redundant instruction elimination
- Flow-of-control optimizations
- Algebraic simplifications
- Use of machine idioms

