HIGHER SECONDARY SECOND YEAR MATHEMATICS MODEL QUESTION PAPER 2019 - 20

Check the question paper for fairness of printing. If there is

any lack of fairness, inform the Hall Supervisor immediately. Use Blue or Black ink to write and underline and pencil to

[Maximum Marks:90

Time Allowed: 15 Minutes + 2.30 Hours]

(a)

(b)

draw diagrams.

Instructions:

		P.	ART-1				
Note:	(i)	All questions are compu	ilsory.		$20 \times 1 = 20$		
	(ii)	Choose the most suitable and write the option code					
L	If $A = \begin{bmatrix} 3 & 5 \\ 1 & 2 \end{bmatrix}$, $B = adjA$ and $C = 3A$, then	$\frac{ adjB }{ C } =$				
		(b) 1		(d) l			
2.	If the inverse of the matrix $\begin{bmatrix} 1 & 2 \\ 3 & -5 \end{bmatrix}$ is $\frac{1}{11} \begin{bmatrix} a & b \\ c & d \end{bmatrix}$, then the ascending order of a,b,c,d is						
	(a) a,b,c,d	(b) d, b, c, a	(c) c.a.b,d	(d) h,a			
3.	The least value of n satisfying $\left(\frac{\sqrt{3}}{2} + \frac{i}{2}\right)^n = 1$ is						
	(a) 30	(b) 24	(c) 12	(d) 18			
4.	The principal argument of $\frac{3}{-1+i}$ is						
	(a) $\frac{-5\pi}{6}$	(b) $\frac{-2\pi}{3}$	(c) $\frac{-3\pi}{4}$	(d) =	<u>π</u> 2		
5.	The polynomial equation $x^3 + 2x + 3 = 0$ has						
	(a) one negative and two real roots		(b) one positive and two imaginary roots				
	(c) three real		(d) no solution				
Ŋ.	The domain of the function defined by $f(x) = \sin^{-1}(\sqrt{x-1})$ is						
	(a) [1,2]	(b) $[-1,1]$	(c) [0, 1]	(d) [-	- 1,0]		
7.	If $x + y = k$	is a normal to the parabola y	$\simeq 12x$, then the	value of k is			
	(a) 3	(b) -1	(c) 1	(d) 9			
B.	The circle passing through $(1,-2)$ and touching the x-axis at $(3,0)$, again passing through the point is						
	(a) $(-5,2)$	(b) $(2, -5)$	(c) $(5,-2)$	(d) {-	-2.5)		
9.	The volume of the parallelepiped with its edges represented by the vectors $\hat{i} + \hat{j}$, $\hat{i} + 2\hat{j}$, $\hat{i} + \hat{j} + \pi \hat{k}$ is						
	(a) $\frac{\pi}{2}$	(b) $\frac{\pi}{3}$	(c) x	(d) $\frac{\pi}{4}$			
10.	If the line $\frac{x}{x}$	$\frac{-2}{3} = \frac{v-1}{-5} = \frac{z+2}{2}$ lies in the	plane $x + 3y -$	$\alpha z + \beta = 0, th$	nen (n,β) is		

	The Innerton Str. 1 + cos x is increasing in the circulati						
	(a) $\left[\frac{5\pi}{8}, \frac{3\pi}{4}\right]$	$(b)\left[\frac{\pi}{2},\frac{5\pi}{8}\right]$	(c) $\left[\frac{\pi}{4}, \frac{\pi}{2}\right]$	(d) $\left[0, \frac{\pi}{4}\right]$			
12.	The curve $y = ax^4 + bx^2$ with $ab > 0$						
	(a) has no horizontal tangent		(b) is concave up				
	(c) is concave down		(d) has no points of inflection				
13.	If $u = (x - y)^2$, the (a) 1	hen $\frac{\partial u}{\partial x} + \frac{\partial u}{\partial y}$ is					
	(a) t	(b) · l	(c) 0	(d) 2			
14,	The value of $\int_0^1 \frac{1}{1}$	dx is					
	(a) $\frac{\pi}{2}$	(b) π	(c) $\frac{3\pi}{2}$	(d) 2π			
15.	The volume of solid of revolution of the region bounded by $y^2 = x(a - x)$ about x-axis is						
	(a) πα ³	(b) $\frac{\pi a^3}{4}$	(c) = 5	$(d) \frac{\pi a'}{6}$			
16.	If m, n are the order and degree of the differential equation $\left[\frac{d^4y}{dx^4} + \frac{d^2y}{dx^2}\right]^{\frac{1}{2}} = a\frac{d^3y}{dx^4}$ respectively, then						
	the value of 4m-	-n is					
	(a) 15	(b) 12	(c) 14	(d) 13			
17.	The solution of th	e differential equation	$\frac{dy}{dx} = \frac{y}{x} + \frac{\phi \left(\frac{y}{x} \right)}{\phi \left(\frac{y}{x} \right)}$) is			
	$(a) \qquad x\phi\left(\frac{y}{x}\right) = b$	$(b) \phi\left(\frac{y}{x}\right) = kx$	(c) $p\phi\left(\frac{1}{2}\right)$	$\left(\frac{y}{x}\right) = k \qquad (d) \phi\left(\frac{y}{x}\right) = ky$			
18.	A random variable X has the following distribution.						
	[x 1 P(X=x) c	2 2e	3 4 3c 4c			
	Then the value of	e ia					
	(a) 0.1	(b) 0.2	(c) 0.3	(d) 0.4			
19.	If $P\{X = 0\} = 1 - P\{X = 1\}$ and $E[X] = 3Var(X)$, then $P\{X = 0\}$ is						
	(a) $\frac{2}{3}$	(b) 2/2	(c) $\frac{1}{2}$				
	(a) 3	5	3	(d) $\frac{1}{5}$			
20	Which one is the	contrapositive of the sta	tement (ava)	17			

(b) $\neg r \rightarrow (p \lor q)$

(d) $p \rightarrow (q \vee r)$

(a) $\neg r \rightarrow (\neg p \land \neg q)$

(c) $r \to (p \land q)$

(a) (-5,5) (b) (-6,7) (c) (5,-5) (d) (6,-7)

PART-II

Note:

Answer any SEVEN questions.

 $7 \times 2 = 14$

- (ii) Question number 30 is compulsory.
- 21. Solve the following system of linear equations by Cramer's rule: 2x y = 3, x + 2y = -1,
- 22. If z_1 , z_2 and z_3 are complex numbers such that $|z_i| = |z_j| = |z_j| = |z_j| = |z_j| = 1$, find the value of $\left|\frac{1}{z_1} + \frac{1}{z_2} + \frac{1}{z_3} + \frac{1}{z_3}\right|$.
- 23. Find the value of $\sin\left(\frac{\pi}{3} + \cos^{-1}\left(-\frac{1}{2}\right)\right)$.
- 24. Find the equation of the parabola with vertex (-1,-2),axis parallel to y-axis and passing through (3,6).
- 25. If $\hat{a}, \hat{b}, \hat{c}$ are three unit vectors such that \hat{b} and \hat{c} are non-parallel and $\hat{a} \times (\hat{b} \times \hat{c}) = \frac{1}{2}\hat{b}$, find the angle between \hat{a} and \hat{c} .
- 26. If the mass m(x) (in kilogram) of a thin rod of length x (in meters) is given by, $m(x) = \sqrt{3}x$ then what is the rate of change of mass with respect to the length when it is x = 27 meters?
- 27. Evaluate: $\int_{0}^{\infty} e^{-m} x' dx$, where a > 0.
- 28. Show that $y = ax + \frac{b}{x}$, $x \ne 0$ is a solution of the differential equation $x^2y'' + xy' y = 0$.
- 29. Find the mean of a random variable X, whose probability density function is $f'(x) = \begin{cases} \lambda e^{-ix} & \text{for } x \ge 0 \\ 0 & \text{otherwise} \end{cases}$
- 30. Let * be a binary operation on set Q of rational numbers defined as $a*b = \frac{ab}{8}$. Write the identity for *, if any.

PART-III

Note:

(i) Answer any SEVEN questions.

 $7 \times 3 = 21$

- (ii) Question number 40 is compulsory.
- 31. Find the inverse of $\begin{bmatrix} 2 & -1 \\ 5 & -2 \end{bmatrix}$ by Gauss Jordan method.
- 32. If $\omega \neq 1$ is a cube root of unity, show that the roots of the equation (z-1)' + 8 = 0 are $-1, 1-2\omega, 1-2\omega^2$.

- 33. Find all real numbers satisfying $4^4 3(2^{3/2}) + 2^5 = 0$.
- 34. Find the centre, foci, and eccentricity of the hyperbola $12x^2 4y^2 24x + 32y 127 = 0$.
- 35. Find the image of the point whose position vector is $\hat{i} + 2\hat{j} + 3\hat{k}$ in the plane $\hat{r} \cdot (\hat{i} + 2\hat{j} + 4\hat{k}) = 38$.
- 36. Evaluate: $\lim_{x\to 0^+} x \log x$.
- 37. Find a linear approximation for the function given below at the indicated points. $f(x) = x^3 5x + 12$, $x_0 = 2$.
- 38. By using the properties of definite integrals, evaluate $\int_{1}^{3} |x-t| dx$
- 39. Solve: $\frac{dy}{dx} + 2y \cot x = 3x^2 \cos ec^2 x$.
- 40. A fair coin is tossed a fixed number of times. If the probability of getting seven heads is equal to that of getting nine heads, find the probability of getting exactly two heads.

PART - IV

Note: Answer all the questions.

 $7 \times 5 = 35$

(a) By using Gaussian elimination method, balance the chemical reaction equation:
C₂H₆ + O₂ → H₂O + CO₂

OR

- **(b)** If z = x + iy and $\arg\left(\frac{z i}{z + 2}\right) = \frac{\pi}{4}$, show that $x^2 + y^2 + 3x 3y + 2 = 0$
- **42.** (a) Solve the equation: $3x^4 16x^3 + 26x^2 16x + 3 = 0$.

(OR

- **(b)** Solve: $\tan^{-1} \left(\frac{x-1}{x-2} \right) + \tan^{-1} \left(\frac{x+1}{x+2} \right) = \frac{\pi}{4}$.
- 43. (a) A rod of length 1.2m moves with its ends always touching the coordinate axes. The locus of a point P on the rod, which is 0.3m from the end in contact with x -axis is an ellipse. Find the eccentricity.

(OR)

(b) Find the non-parametric and Cartesian equations of the plane passing through the point (4, 2, 4), and is perpendicular to the planes 2x + 5y + 4z + 6 = 0 and 4x + 7y + 6z + 2 = 0.

44. (a) A steel plant is capable of producing x tonnes per day of a low-grade steel and y tonnes per day of a high-grade steel, where $y = \frac{40-5x}{10-x}$. If the fixed market price of low-grade steel is half that of high-grade steel, then what should be optimal productions in low-grade steel and high-grade steel in order to have maximum receipts.

(OR)

- (b) Let $z(x,y) = xe^y + ye^{-t}, x = e^{-t}, y = st^2, s, t \in \mathbb{R}$. Find $\frac{\partial z}{\partial s}$ and $\frac{\partial z}{\partial t}$.
- 45. (a) Find the area of the region bounded between the parabola $x^2 = y$ and the curve y = |x|.

(OR)

- (h) Water at temperature $100^{\circ}C$ cools in 10° minutes to $80^{\circ}C$ in a room temperature of $25^{\circ}C$. Find
 - (i) The temperature of water after 20 minutes
 - (ii) The time when the temperature is $40^{\circ}C = \left[\log_{e} \frac{11}{15} = -0.3101; \log_{e} 5 = 1.6094\right]$
- 46. (a) Suppose a discrete random variable can take only the values 0, 1, and 2. The probability mass function is defined by

$$f(x) = \begin{cases} \frac{x^2 + 1}{k}, & \text{for } x = 0, 1, 2\\ 0 & \text{otherwise} \end{cases}$$

Find (i) the value of k (ii) cumulative distribution function (iii) $P(x \ge 1)$

(OR)

- (b) Using truth table check whether the statements $\neg (p \lor q) \lor (\neg p \land q)$ and $\neg p$ are logically equivalent.
- 47. (a) Prove by vector method that $\sin(\alpha + \beta) = \sin \alpha \cos \beta + \cos \alpha \sin \beta$.

(K. Similaran)

(OR)

(b) Find the equations of tangent and normal to the curve y' - 4x - 2y + 5 = 0 at the point where it cuts the x-axis.