

ICSE Class 9 Maths Selina Solutions Chapter 5 - Factorisation

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ICSE Class 9 Maths Selina Solutions Chapter 5: Here we provide you with detailed ICSE Class 9 Maths Selina Solution Chapter 5 Factorization. Our PW Subject experts have prepared these questions according to the latest syllabus for ICSE Class 9 Maths exam. Selina's solutions are considered very useful for ICSE Class 9 Maths exam preparation. For better and more strategic preparation in the right direction, our blog serves as a guide for ICSE Class 9 Maths 2024 aspirants.

ICSE Class 9 Maths Selina Solutions Chapter 5

In mathematics, Factorization is writing a number or other mathematical object as the product of several factors, usually the product of smaller or simpler similar objects. For example, 3×5 is an integer factorization of 15 and is a polynomial factorization of $x^2 - 4$.

Selina's solutions are considered very useful for ICSE class 9 Maths Selina Solutions Chapter 5 preparation. Here we bring you with detailed answers and solutions for Selina Solutions for Class 9 Maths Chapter 5 - Factorization. Subject experts have prepared these questions as per the syllabus prescribed by CISCE for ICSE.

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ICSE Class 9 Maths Selina Solutions Chapter 5 PDF

ICSE Class 9 Maths Selina Solutions Chapter 5 Factorization

Here we have provided ICSE Class 9 Maths Selina Solutions Chapter 5 Factorization for the ease of students so that they can prepare better for their ICSE Class 9 Maths Exam.

Exercise 5(A)

Factorise by taking out the common factors:

$$1. 2(2x - 5y)(3x + 4y) - 6(2x - 5y)(x - y)$$

Solution:

Identifying and taking $(2x - 5y)$ common from both the terms, we have

$$= (2x - 5y)[2(3x + 4y) - 6(x - y)]$$

$$= (2x - 5y)(6x + 8y - 6x + 6y)$$

$$= (2x - 5y)(8y + 6y)$$

$$= (2x - 5y)(14y)$$

$$= (2x - 5y)14y$$

$$2. xy(3x^2 - 2y^2) - yz(2y^2 - 3x^2) + zx(15x^2 - 10y^2)$$

Solution:

We have, $xy(3x^2 - 2y^2) - yz(2y^2 - 3x^2) + zx(15x^2 - 10y^2)$

Changing signs to arrive at a common term

So,

$$= xy(3x^2 - 2y^2) + yz(3x^2 - 2y^2) + zx(15x^2 - 10y^2)$$

$$= xy(3x^2 - 2y^2) + yz(3x^2 - 2y^2) + 5zx(3x^2 - 2y^2)$$

$$= (3x^2 - 2y^2)(xy + yz + 5zx)$$

$$3. ab(a^2 + b^2 - c^2) - bc(c^2 - a^2 - b^2) + ca(a^2 + b^2 - c^2)$$

Solution:

We have, $ab(a^2 + b^2 - c^2) - bc(c^2 - a^2 - b^2) + ca(a^2 + b^2 - c^2)$

Changing signs to arrive at a common term

So,

$$= ab(a^2 + b^2 - c^2) + bc(a^2 + b^2 - c^2) + ca(a^2 + b^2 - c^2)$$

$$= (a^2 + b^2 - c^2) (ab + bc + ca)$$

$$4. 2x(a - b) + 3y(5a - 5b) + 4z(2b - 2a)$$

Solution:

$$\text{We have, } 2x(a - b) + 3y(5a - 5b) + 4z(2b - 2a)$$

Taking common factors, we get

$$= 2x(a - b) + 15y(a - b) - 8z(a - b)$$

$$= (a - b) (2x + 15y - 8z)$$

Factorize by the grouping method:

$$5. a^3 + a - 3a^2 - 3$$

Solution:

$$\text{We have, } a^3 + a - 3a^2 - 3$$

Grouping to arrive at a common term

$$= a(a^2 + 1) - 3(a^2 + 1)$$

Taking common, we get

$$= (a^2 + 1) (a - 3)$$

$$6. 16(a + b)^2 - 4a - 4b$$

Solution:

$$\text{We have, } 16(a + b)^2 - 4a - 4b$$

Grouping to arrive at a common term

$$= 16(a + b)^2 - 4(a + b)$$

Taking common, we get

$$= 4(a + b) [4(a + b) - 1]$$

$$= 4(a + b)(4a + 4b - 1)$$

7. Factorize by the grouping method:

$$a^4 - 2a^3 - 4a + 8$$

Solution:

$$\text{We have, } a^4 - 2a^3 - 4a + 8$$

Grouping to arrive at a common term

$$= a^3(a - 2) - 4(a - 2)$$

Taking common, we get

$$= (a^3 - 4)(a - 2)$$

$$8. ab - 2b + a^2 - 2a$$

Solution:

$$\text{We have, } ab - 2b + a^2 - 2a$$

Grouping to arrive at a common term

$$= b(a - 2) + a(a - 2)$$

Taking common, we get

$$= (b + a)(a - 2)$$

$$9. ab(x^2 + 1) + x(a^2 + b^2)$$

Solution:

$$\text{We have, } ab(x^2 + 1) + x(a^2 + b^2)$$

On expanding,

$$= abx^2 + ab + a^2x + b^2x$$

Now, grouping to arrive at a common term

$$= abx^2 + a^2x + b^2x + ab$$

$$= ax(bx + a) + b(bx + a)$$

Taking common, we get

$$= (ax + b)(bx + a)$$

$$10. a^2 + b - ab - a$$

Solution:

We have, $a^2 + b - ab - a$

Grouping to arrive at a common term

$$= a^2 - a + b - ab$$

$$= a(a - 1) - b(-1 + a)$$

$$= a(a - 1) - b(a - 1)$$

Taking common, we get

$$= (a - b)(a - 1)$$

$$11. (ax + by)^2 + (bx - ay)^2$$

Solution:

We have, $(ax + by)^2 + (bx - ay)^2$

On expanding,

$$= a^2x^2 + b^2y^2 + 2abxy + b^2x^2 + a^2y^2 - 2abxy$$

$$= a^2x^2 + b^2y^2 + b^2x^2 + a^2y^2$$

Rearranging terms, we get

$$= a^2x^2 + b^2x^2 + a^2y^2 + b^2y^2$$

Taking common, we get

$$= x^2(a^2 + b^2) + y^2(a^2 + b^2)$$

$$= (x^2 + y^2) (a^2 + b^2)$$

$$12. a^2x^2 + (ax^2 + 1)x + a$$

Solution:

$$\text{We have, } a^2x^2 + (ax^2 + 1)x + a$$

Regrouping the terms, we have

$$= a^2x^2 + a + (ax^2 + 1)x$$

$$= a(ax^2 + 1) + x(ax^2 + 1)$$

Taking common, we get

$$= (ax^2 + 1) (a + x)$$

$$13. (2a - b)^2 - 10a + 5b$$

Solution:

$$\text{We have, } (2a - b)^2 - 10a + 5b$$

Taking common,

$$= (2a - b)^2 - 5(2a - b)$$

Now,

$$= (2a - b) [(2a - b) - 5]$$

$$= (2a - b) (2a - b - 5)$$

$$14. a(a - 4) - a + 4$$

Solution:

$$\text{We have, } a(a - 4) - a + 4$$

By grouping, we get

$$= a(a - 4) - 1(a - 4)$$

Now, taking the common term

$$= (a - 4) (a - 1)$$

$$15. y^2 - (a + b) y + ab$$

Solution:

We have, $y^2 - (a + b) y + ab$

On expanding,

$$= y^2 - ay - by + ab$$

$$= (y^2 - ay) - by + ab$$

Taking 'y' and 'b' common from the group, we get

$$= y(y - a) - b(y - a)$$

$$= (y - a) (y - b)$$

$$16. a^2 + 1/a^2 - 2 - 3a + 3/a$$

Solution:

We have, $a^2 + 1/a^2 - 2 - 3a + 3/a$

On grouping terms, we get

$$= (a^2 - 2 + 1/a^2) - 3a + 3/a$$

$$= [a^2 - (2 \times a \times 1/a) + 1/a^2] - 3(a - 1/a)$$

$$= (a - 1/a)^2 - 3(a - 1/a) \text{ \{Since, } (x - y)^2 = x^2 - 2xy + y^2\}}$$

Taking $(a - 1/a)$ as common, we get

$$= (a - 1/a) [(a - 1/a) - 3]$$

$$= (a - 1/a) (a - 1/a - 3)$$

$$17. x^2 + y^2 + x + y + 2xy$$

Solution:

We have, $x^2 + y^2 + x + y + 2xy$

On rearranging terms, we get

$$= (x^2 + y^2 + 2xy) + (x + y) \text{ \{Since, } (x + y)^2 = x^2 + 2xy + y^2\}}$$

Now,

$$= (x + y)^2 + (x + y)$$

$$= (x + y)(x + y + 1)$$

$$18. a^2 + 4b^2 - 3a + 6b - 4ab$$

Solution:

We have, $a^2 + 4b^2 - 3a + 6b - 4ab$

On rearranging terms, we get

$$= a^2 + 4b^2 - 4ab - 3a + 6b$$

Now,

$$= a^2 + (2b)^2 - 2 \times a \times (2b) - 3(a - 2b) \text{ \{Since, } (a - b)^2 = a^2 - 2ab + b^2\}}$$

$$= (a - 2b)^2 - 3(a - 2b)$$

$$= (a - 2b) [(a - 2b) - 3]$$

$$= (a - 2b) (a - 2b - 3)$$

$$19. m(x - 3y)^2 + n(3y - x) + 5x - 15y$$

Solution:

We have, $m(x - 3y)^2 + n(3y - x) + 5x - 15y$

Now,

Taking $(x - 3y)$ common from all the three terms, we get

$$= m(x - 3y)^2 - n(x - 3y) + 5(x - 3y)$$

$$= (x - 3y) [m(x - 3y) - n + 5]$$

$$= (x - 3y) (mx - 3my - n + 5)$$

$$20. x(6x - 5y) - 4(6x - 5y)^2$$

Solution:

$$\text{We have, } x(6x - 5y) - 4(6x - 5y)^2$$

Now,

Taking $(6x - 5y)$ common from the three terms, we get

$$= (6x - 5y) [x - 4(6x - 5y)]$$

$$= (6x - 5y) (x - 24x + 20y)$$

$$= (6x - 5y) (-23x + 20y)$$

$$= (6x - 5y) (20y - 23x)$$

Exercise 5(B)

Factorize:

$$1. a^2 + 10a + 24$$

Solution:

$$\text{We have, } a^2 + 10a + 24$$

By splitting the middle term, we get

$$= a^2 + 6a + 4a + 24$$

$$= a(a + 6) + 4(a + 6)$$

$$= (a + 4) (a + 6)$$

$$2. a^2 - 3a - 40$$

Solution:

$$\text{We have, } a^2 - 3a - 40$$

By splitting the middle term, we get

$$= a^2 - 8a + 5a - 40$$

$$= a(a - 8) + 5(a - 8)$$

$$= (a + 5) (a - 8)$$

$$3. 1 - 2a - 3a^2$$

Solution:

$$\text{We have, } 1 - 2a - 3a^2$$

By splitting the middle term, we get

$$= 1 - 3a + a - 3a^2$$

$$= 1(1 - 3a) + a(1 - 3a)$$

$$= (1 + a) (1 - 3a)$$

$$4. x^2 - 3ax - 88a^2$$

Solution:

$$\text{We have, } x^2 - 3ax - 88a^2$$

By splitting the middle term, we get

$$= x^2 - 11ax + 8ax - 88a^2$$

$$= x(x - 11a) + 8a(x - 11a)$$

$$= (x + 8a) (x - 11a)$$

5. $6a^2 - a - 15$

Solution:

We have, $6a^2 - a - 15$

By splitting the middle term, we get

$$= 6a^2 + 9a - 10a - 15$$

$$= 3a(2a + 3) - 5(2a + 3)$$

$$= (3a - 5)(2a + 3)$$

6. $24a^3 + 37a^2 - 5a$

Solution:

We have, $24a^3 + 37a^2 - 5a$

Taking 'a' common from all

$$= a(24a^2 + 37a - 5)$$

$$= a(24a^2 + 40a - 3a - 5) \text{ {By splitting the middle term}}$$

$$= a[8a(3a + 5) - 1(3a + 5)]$$

$$= a[(8a - 1)(3a + 5)]$$

$$= a(8a - 1)(3a + 5)$$

7. $a(3a - 2) - 1$

Solution:

We have, $a(3a - 2) - 1$

On expanding,

$$= 3a^2 - 2a - 1$$

By splitting the middle term, we get

$$= 3a^2 - 3a + a - 1$$

$$= 3a(a - 1) + 1(a - 1)$$

$$= (3a + 1)(a - 1)$$

$$8. a^2b^2 + 8ab - 9$$

Solution:

We have, $a^2b^2 + 8ab - 9$

By splitting the middle term, we get

$$= a^2b^2 + 9ab - ab - 9$$

$$= ab(ab + 9) - 1(ab + 9)$$

$$= (ab - 1)(ab + 9)$$

$$9. 3 - a(4 + 7a)$$

Solution:

We have, $3 - a(4 + 7a)$

On expanding,

$$= 3 - 4a - 7a^2$$

By splitting the middle term, we get

$$= 3 + 3a - 7a - 7a^2$$

$$= 3(1 + a) - 7a(1 + a)$$

$$= (1 + a)(3 - 7a)$$

$$10. (2a + b)^2 - 6a - 3b - 4$$

Solution:

We have, $(2a + b)^2 - 6a - 3b - 4$

$$= (2a + b)^2 - 3(2a + b) - 4$$

Let's assume that $(2a + b) = x$

So, the expression becomes

$$= x^2 - 3x - 4$$

By splitting the middle term, we get

$$= x^2 - 4x + x - 4$$

$$= x(x - 4) + 1(x - 4)$$

$$= (x - 4)(x + 1)$$

Resubstituting the value of x , we get

$$= (2a + b - 4)(2a + b + 1)$$

$$11. 1 - 2(a + b) - 3(a + b)^2$$

Solution:

We have, $1 - 2(a + b) - 3(a + b)^2$

Let's assume $(a + b) = x$

Then, the expression becomes

$$= 1 - 2x - 3x^2$$

By splitting the middle term, we get

$$= 1 - 3x + x - 3x^2$$

$$= 1(1 - 3x) + x(1 - 3x)$$

$$= (1 - 3x)(1 + x)$$

Resubstituting the value of x , we get

$$= [1 - 3(a + b)] [1 + (a + b)]$$

$$= (1 - 3a - 3b) (1 + a + b)$$

$$12. 3a^2 - 1 - 2a$$

Solution:

We have, $3a^2 - 1 - 2a$

Rearranging,

$$= 3a^2 - 2a - 1$$

By splitting the middle term, we get

$$= 3a^2 - 3a + a - 1$$

$$= 3a(a - 1) + 1(a - 1)$$

$$= (3a + 1) (a - 1)$$

$$13. x^2 + 3x + 2 + ax + 2a$$

Solution:

We have, $x^2 + 3x + 2 + ax + 2a$

By splitting the middle term, we get

$$= (x^2 + 2x + x + 2) + ax + 2a$$

$$= x(x + 2) + 1(x + 2) + a(x + 2)$$

$$= (x + 2) (x + a + 1)$$

$$14. (3x - 2y)^2 + 3(3x - 2y) - 10$$

Solution:

We know, $(3x - 2y)^2 + 3(3x - 2y) - 10$

Let's assume that $(3x - 2y) = a$

So, the expression becomes

$$= a^2 + 3a - 10$$

By splitting the middle term, we get

$$= a^2 + 5a - 2a - 10$$

$$= a(a + 5) - 2(a + 5)$$

$$= (a - 2)(a + 5)$$

$$= (3x - 2y + 5)(3x - 2y - 2)$$

$$15. 5 - (3a^2 - 2a)(6 - 3a^2 + 2a)$$

Solution:

$$\text{Given, } 5 - (3a^2 - 2a)(6 - 3a^2 + 2a)$$

$$= 5 - (3a^2 - 2a)[6 - (3a^2 - 2a)]$$

$$\text{Let's substitute } (3a^2 - 2a) = x$$

And, the expression becomes,

$$= 5 - x(6 - x)$$

$$= 5 - 6x - x^2$$

$$= 5 - 5x - x - x^2$$

$$= 5(1 - x) - x(1 - x)$$

$$= (1 - x)(5 - x)$$

$$= (x - 1)(x - 5)$$

$$= (3a^2 - 2a - 1) (3a^2 - 2a - 5)$$

Now,

$$= (3a^2 - 3a + a - 1) (3a^2 + 3a - 5a - 5) \text{ {By splitting the middle term}}$$

$$= [3a(a - 1) + 1(a - 1)] [3a(a + 1) - 5(a + 1)]$$

$$= [(3a + 1) (a - 1)] [(3a - 5) (a + 1)]$$

$$= (3a + 1) (3a - 5) (a + 1)(a - 1)$$

$$16. \frac{1}{35} + \frac{12a}{35} + a^2$$

Solution:

$$\text{We have, } \frac{1}{35} + \frac{12a}{35} + a^2$$

Taking common,

$$= \frac{1}{35} (1 + 12a + 35a^2)$$

$$= \frac{1}{35} (35a^2 + 12a + 1)$$

$$= \frac{1}{35} (35a^2 + 7a + 5a + 1) \text{ {By splitting the middle term}}$$

$$= \frac{1}{35} [7a(5a + 1) + 1(5a + 1)]$$

$$= \frac{1}{35} [(7a + 1) (5a + 1)]$$

$$= \frac{[(7a + 1) (5a + 1)]}{35}$$

$$17. (x^2 - 3x) (x^2 - 3x - 1) - 20.$$

Solution:

$$\text{We have, } (x^2 - 3x) (x^2 - 3x - 1) - 20$$

$$= (x^2 - 3x)[(x^2 - 3x) - 1] - 20$$

Let's

$$= a[a - 1] - 20 \dots (\text{Taking } x^2 - 3x = a)$$

$$= a^2 - a - 20$$

$$= a^2 - 5a + 4a - 20$$

$$= a(a - 5) + 4(a - 5)$$

$$= (a - 5)(a + 4)$$

$$= (x^2 - 3x - 5)(x^2 - 3x + 4)$$

18. Find each trinomial (quadratic expression), given below, find whether it is factorisable or not. Factorise, if possible.

(i) $x^2 - 3x - 54$

(ii) $2x^2 - 7x - 15$

(iii) $2x^2 + 2x - 75$

(iv) $3x^2 + 4x - 10$

(v) $x(2x - 1) - 1$

Solution:

(i) Given, $x^2 - 3x - 54$

On comparing with the general form $ax^2 + bx + c$, we get

$$a = 1, b = -3 \text{ and } c = -54$$

$$\text{So, } b^2 - 4ac = (-3)^2 - 4(1)(-54) = 9 + 216 = 225$$

225 is a perfect square

Thus, $x^2 - 3x - 54$ is factorisable

Now,

$$x^2 - 3x - 54 = x^2 - 9x + 6x - 54$$

$$= x(x - 9) + 6(x - 9)$$

$$= (x + 6)(x - 9)$$

(ii) Given, $2x^2 - 7x - 15$

On comparing with the general form $ax^2 + bx + c$, we get

$$a = 2, b = -7 \text{ and } c = -15$$

$$\text{So, } b^2 - 4ac = (-7)^2 - 4(2)(-15) = 49 + 120 = 169$$

169 is a perfect square

Thus, $2x^2 - 7x - 15$ is factorisable

Now,

$$2x^2 - 7x - 15 = 2x^2 - 10x + 3x - 15$$

$$= 2x(x - 5) + 3(x - 5)$$

$$= (2x + 3)(x - 5)$$

(iii) Given, $2x^2 + 2x - 75$

On comparing with the general form $ax^2 + bx + c$, we get

$$a = 2, b = 2 \text{ and } c = -75$$

$$\text{So, } b^2 - 4ac = (2)^2 - 4(2)(-75) = 4 + 600 = 604$$

604 is not a perfect square

Thus, $2x^2 + 2x - 75$ is not factorizable

(iv) Given, $3x^2 + 4x - 10$

On comparing with the general form $ax^2 + bx + c$, we get

$$a = 3, b = 4 \text{ and } c = -10$$

$$\text{So, } b^2 - 4ac = (4)^2 - 4(3)(-10) = 16 + 120 = 136$$

136 is a not perfect square

Thus, $3x^2 + 4x - 10$ is not factorizable

(v) Given, $x(2x - 1) - 1$

$$= 2x^2 - x - 1$$

On comparing with the general form $ax^2 + bx + c$, we get

$$a = 2, b = -1 \text{ and } c = -1$$

$$\text{So, } b^2 - 4ac = (-1)^2 - 4(2)(-1) = 1 + 8 = 9$$

9 is a perfect square

Thus, $x(2x - 1) - 1$ is factorisable

Now,

$$x(2x - 1) - 1 = 2x^2 - x - 1$$

$$= 2x^2 - 2x + x - 1$$

$$= 2x(x - 1) + 1(x - 1)$$

$$= (2x + 1)(x - 1)$$

19. Factorise:

$$(i) 4\sqrt{3}x^2 + 5x - 2\sqrt{3}$$

$$(ii) 7\sqrt{2}x^2 - 10x - 4\sqrt{2}$$

Solution:

$$(i) \text{ We have, } 4\sqrt{3}x^2 + 5x - 2\sqrt{3}$$

By splitting the middle term, we get

$$= 4\sqrt{3}x^2 + 8x - 3x - 2\sqrt{3}$$

$$= 4x(\sqrt{3}x + 2) - \sqrt{3}(\sqrt{3}x + 2)$$

$$= (4x - \sqrt{3})(\sqrt{3}x + 2)$$

(ii) We have, $7\sqrt{2}x^2 - 10x - 4\sqrt{2}$

By splitting the middle term, we get

$$= 7\sqrt{2}x^2 - 14x + 4x - 4\sqrt{2}$$

$$= 7\sqrt{2}x(x - \sqrt{2}) + 4(x - \sqrt{2})$$

$$= (7\sqrt{2}x + 4)(x - \sqrt{2})$$

20. Give possible expressions for the length and the breadth of the rectangle whose area is $12x^2 - 35x + 25$.

Solution:

We have, $12x^2 - 35x + 25$

By splitting the middle term, we get

$$= 12x^2 - 20x - 15x + 25$$

$$= 4x(3x - 5) - 5(3x - 5)$$

$$= (3x - 5)(4x - 5)$$

Hence,

Length = $(3x - 5)$ and breadth = $(4x - 5)$ or,

Length = $(4x - 5)$ and breadth = $(3x - 5)$

Exercise 5(C)

Factorize:

1. $25a^2 - 9b^2$

Solution:

We have, $25a^2 - 9b^2$

$$= (5a)^2 - (3b)^2$$

$$= (5a + 3b) (5a - 3b) \text{ [As } x^2 - y^2 = (x + y)(x - y)\text{]}$$

$$2. a^2 - (2a + 3b)^2$$

Solution:

$$\text{We have, } a^2 - (2a + 3b)^2$$

$$= [a - (2a + 3b)] [a + (2a + 3b)] \text{ [As } x^2 - y^2 = (x + y)(x - y)\text{]}$$

$$= (a - 2a - 3b) (a + 2a + 3b)$$

$$= (-a - 3b) (3a + 3b)$$

$$= -3(a + 3b) (a + b)$$

$$3. a^2 - 81(b-c)^2$$

Solution:

$$\text{We have, } a^2 - 81(b-c)^2$$

$$= a^2 - [9(b - c)]^2$$

$$= [a - 9(b - c)] [a + 9(b - c)] \text{ [As } x^2 - y^2 = (x + y)(x - y)\text{]}$$

$$= (a - 9b + 9c) (a + 9b - 9c)$$

$$4. 25(2a - b)^2 - 81b^2$$

Solution:

$$\text{We have, } 25(2a - b)^2 - 81b^2$$

$$= [5(2a - b)]^2 - (9b)^2$$

$$= [5(2a - b) - 9b] [5(2a - b) + 9b] \text{ [As } x^2 - y^2 = (x + y)(x - y)\text{]}$$

$$= (10a - 5b - 9b) (10a - 5b + 9b)$$

$$= (10a - 14b) (10a + 4b)$$

$$= 2(5a - 7b) \cdot 2(5a + 2b)$$

$$= 2(5a - 7b) (5a + 2b)$$

$$5. 50a^3 - 2a$$

Solution:

We have, $50a^3 - 2a$

$$= 2a(25a^2 - 1)$$

$$= 2a[(5a)^2 - 1^2]$$

$$= 2a(5a - 1)(5a + 1) \text{ [As } x^2 - y^2 = (x + y)(x - y)\text{]}$$

$$6. 4a^2b - 9b^3$$

Solution:

We have, $4a^2b - 9b^3$

$$= b(4a^2 - 9b^2)$$

$$= b[(2a)^2 - (3b)^2]$$

$$= b[(2a + 3b) (2a - 3b)] \text{ [As } x^2 - y^2 = (x + y)(x - y)\text{]}$$

$$= b(2a + 3b)(2a - 3b)$$

$$7. 3a^5 - 108a^3$$

Solution:

We have, $3a^5 - 108a^3$

$$= 3a^3(a^2 - 36)$$

$$= 3a^3(a^2 - 6^2)$$

$$= 3a^3(a - 6) (a + 6) \text{ [As } x^2 - y^2 = (x + y)(x - y)\text{]}$$

$$8. 9(a - 2)^2 - 16(a + 2)^2$$

Solution:

We have, $9(a - 2)^2 - 16(a + 2)^2$

$$= [3(a - 2)]^2 - [4(a + 2)]^2$$

$$= [3(a - 2) - 4(a + 2)] [3(a - 2) + 4(a + 2)] \text{ [As } x^2 - y^2 = (x + y)(x - y)\text{]}$$

$$= [3a - 6 - 4a - 8] [3a - 6 + 4a + 8]$$

$$= [-a - 14] [7a + 2]$$

$$= -(a + 14) (7a + 2)$$

9. $a^4 - 1$

Solution:

We have, $a^4 - 1$

$$= (a^2)^2 - 1^2$$

$$= (a^2 - 1) (a^2 + 1) \text{ [As } x^2 - y^2 = (x + y)(x - y)\text{]}$$

$$= [(a - 1)(a + 1)] (a^2 + 1)$$

$$= (a - 1)(a + 1)(a^2 + 1)$$

10. $a^3 + 2a^2 - a - 2$

Solution:

We have, $a^3 + 2a^2 - a - 2$

$$= a^2(a + 2) - 1(a + 2)$$

$$= (a^2 - 1) (a + 2)$$

$$= (a - 1) (a + 1) (a + 2) \text{ [As } x^2 - y^2 = (x + y)(x - y)\text{]}$$

11. $(a + b)^3 - a - b$

Solution:

We have, $(a + b)^3 - a - b$

$$= (a + b)^3 - (a + b)$$

$$= (a + b) [(a + b)^2 - 1]$$

$$= (a + b) [(a + b - 1)(a + b + 1)] \text{ [As } x^2 - y^2 = (x + y)(x - y)\text{]}$$

$$= (a + b)(a + b - 1)(a + b + 1)$$

12. $a(a - 1) - b(b - 1)$

Solution:

We have, $a(a - 1) - b(b - 1)$

$$= a^2 - a - b^2 + b$$

$$= (a^2 - b^2) - (a - b)$$

$$= (a + b)(a - b) - (a - b) \text{ [As } x^2 - y^2 = (x + y)(x - y)\text{]}$$

$$= (a - b) [(a + b) - 1]$$

$$= (a - b)(a + b - 1)$$

13. $4a^2 - (4b^2 + 4bc + c^2)$

Solution:

We know, $4a^2 - (4b^2 + 4bc + c^2)$

$$= (2a)^2 - [(2b)^2 + 2(2b)(c) + c^2]$$

$$= (2a)^2 - (2b + c)^2$$

$$= (2a - 2b - c)(2a + 2b + c) \text{ [As } x^2 - y^2 = (x + y)(x - y)\text{]}$$

14. $4a^2 - 49b^2 + 2a - 7b$

Solution:

We know, $4a^2 - 49b^2 + 2a - 7b$

$$= (2a)^2 - (7b)^2 + (2a - 7b)$$

$$= [(2a - 7b)(2a + 7b)] + (2a - 7b) \text{ [As } x^2 - y^2 = (x + y)(x - y)\text{]}$$

$$= (2a - 7b) [(2a + 7b) + 1]$$

$$= (2a - 7b)(2a + 7b + 1)$$

$$15. 9a^2 + 3a - 8b - 64b^2$$

Solution:

$$\text{We have, } 9a^2 + 3a - 8b - 64b^2$$

$$= 9a^2 - 64b^2 + 3a - 8b$$

$$= (3a)^2 - (8b)^2 + (3a - 8b)$$

$$= [(3a - 8b)(3a + 8b)] + (3a - 8b) \text{ [As } x^2 - y^2 = (x + y)(x - y)\text{]}$$

$$= (3a - 8b) [(3a + 8b) + 1]$$

$$= (3a - 8b)(3a + 8b + 1)$$

$$16. 4a^2 - 12a + 9 - 49b^2$$

Solution:

$$\text{We have, } 4a^2 - 12a + 9 - 49b^2$$

$$= [(2a)^2 - 2(2a)(3) + 3^2] - (7b)^2$$

$$= (2a - 3)^2 - (7b)^2$$

$$= (2a - 7b - 3)(2a + 7b - 3) \text{ [As } x^2 - y^2 = (x + y)(x - y)\text{]}$$

$$17. 4xy - x^2 - 4y^2 + z^2$$

Solution:

$$\text{We have, } 4xy - x^2 - 4y^2 + z^2$$

On rearranging,

$$= z^2 - x^2 - 4y^2 + 4xy$$

$$= z^2 - (x^2 + 4y^2 - 4xy)$$

$$= z^2 - (x - 2y)^2$$

$$= (z - x + 2y)(z + x - 2y) \text{ [As } x^2 - y^2 = (x + y)(x - y)\text{]}$$

$$18. a^2 + b^2 - c^2 - d^2 + 2ab - 2cd$$

Solution:

$$\text{We have, } a^2 + b^2 - c^2 - d^2 + 2ab - 2cd$$

On rearranging,

$$= a^2 + 2ab + b^2 - c^2 - d^2 - 2cd$$

$$= (a^2 + 2ab + b^2) - (c^2 + d^2 + 2cd)$$

$$= (a + b)^2 - (c + d)^2$$

$$= (a + b + c + d)(a + b - c - d) \text{ [As } x^2 - y^2 = (x + y)(x - y)\text{]}$$

$$19. 4x^2 - 12ax - y^2 - z^2 - 2yz + 9a^2$$

Solution:

$$\text{We have, } 4x^2 - 12ax - y^2 - z^2 - 2yz + 9a^2$$

On rearranging,

$$= 4x^2 - 12ax + 9a^2 - y^2 - z^2 - 2yz$$

$$= (4x^2 - 12ax + 9a^2) - (y^2 + z^2 + 2yz)$$

$$= (2x - 3a)^2 - (y + z)^2$$

$$= (2x - 3a + y + z) (2x - 3a - y - z) \text{ [As } x^2 - y^2 = (x + y)(x - y)\text{]}$$

$$20. (a^2 - 1) (b^2 - 1) + 4ab$$

Solution:

$$\text{We have, } (a^2 - 1) (b^2 - 1) + 4ab$$

By cross multiplying and expanding, we get

$$= (1 - a^2 - b^2 + a^2b^2) + 4ab$$

On manipulating,

$$= (a^2b^2 + 1 + 2ab) - (a^2 + b^2 - 2ab)$$

Now,

$$= (ab + 1)^2 - (a - b)^2$$

$$= [(ab + 1) - (a - b)] [(ab + 1) + (a - b)]$$

$$= (ab + 1 - a + b) (ab + 1 + a - b) \text{ [As } x^2 - y^2 = (x + y)(x - y)\text{]}$$

$$21. x^4 + x^2 + 1$$

Solution:

$$\text{We have, } x^4 + x^2 + 1$$

$$= x^4 + 2x^2 + 1 - x^2$$

$$= (x^2 + 1)^2 - x^2 \text{ [As } a^2 - b^2 = (a + b)(a - b)\text{]}$$

$$= (x^2 + 1 - x) (x^2 + 1 + x)$$

$$22. (a^2 + b^2 - 4c^2)^2 - 4a^2b^2$$

Solution:

We have, $(a^2 + b^2 - 4c^2)^2 - 4a^2b^2$

$$= (a^2 + b^2 - 4c^2)^2 - (2ab)^2$$

$$= [(a^2 + b^2 - 4c^2) + (2ab)] [(a^2 + b^2 - 4c^2) - (2ab)] \text{ [As } x^2 - y^2 = (x + y)(x - y)]$$

$$= [(a^2 + b^2 + 2ab) - 4c^2] [(a^2 + b^2 - 2ab) - 4c^2]$$

$$= [(a + b)^2 - (2c)^2] [(a - b)^2 - (2c)^2]$$

$$= [(a + b - 2c) (a + b + 2c)] [(a - b - 2c) (a - b + 2c)] \text{ [As } x^2 - y^2 = (x + y)(x - y)]$$

$$= (a + b - 2c) (a + b + 2c) (a - b - 2c) (a - b + 2c)$$

$$23. (x^2 + 4y^2 - 9z^2)^2 - 16x^2y^2$$

Solution:

We have, $(x^2 + 4y^2 - 9z^2)^2 - 16x^2y^2$

$$= (x^2 + 4y^2 - 9z^2)^2 - (4xy)^2$$

$$= (x^2 + 4y^2 - 9z^2 - 4xy) (x^2 + 4y^2 - 9z^2 + 4xy) \text{ [As } x^2 - y^2 = (x + y)(x - y)]$$

$$= [(x^2 - 4xy + 4y^2) - 9z^2] [(x^2 + 4xy + 4y^2) - 9z^2]$$

$$= [(x - 2y)^2 - (3z)^2] [(x + 2y)^2 - (3z)^2]$$

$$= [(x - 2y + 3z) (x - 2y - 3z)] [(x + 2y + 3z) (x + 2y - 3z)] \text{ [As } x^2 - y^2 = (x + y)(x - y)]$$

$$= (x - 2y + 3z) (x - 2y - 3z) [(x + 2y + 3z) (x + 2y - 3z)]$$

$$24. (a + b)^2 - a^2 + b^2$$

Solution:

We have, $(a + b)^2 - a^2 + b^2$

On expanding,

$$= (a^2 + 2ab + b^2) - a^2 + b^2$$

$$= 2b^2 + 2ab$$

$$= 2b(b + a)$$

$$25. a^2 - b^2 - (a + b)^2$$

Solution:

$$\text{We have, } a^2 - b^2 - (a + b)^2$$

On expanding,

$$= a^2 - b^2 - (a^2 + b^2 + 2ab)$$

$$= a^2 - b^2 - a^2 - b^2 - 2ab$$

$$= -2b^2 - 2ab$$

$$= -2b(b + a)$$

$$26. 9a^2 - (a^2 - 4)^2$$

Solution:

$$\text{We have, } 9a^2 - (a^2 - 4)^2$$

$$= (3a)^2 - (a^2 - 4)^2$$

$$= [3a - (a^2 - 4)][3a + (a^2 - 4)] \text{ [As } x^2 - y^2 = (x + y)(x - y)]$$

$$= [3a - (a^2 - 4)][3a + (a^2 - 4)]$$

$$= (3a - a^2 + 4)(3a + a^2 - 4)$$

$$= (-a^2 + 3a + 4)(a^2 + 3a - 4)$$

$$= (-a^2 + 4a - a + 4)(a^2 + 4a - a - 4) \text{ [By splitting the middle term]}$$

$$= [a(-a + 4) + 1(-a + 4)][a(a + 4) - 1(a + 4)]$$

$$= [(-a + 4)(a + 1)][(a - 1)(a + 4)]$$

$$= (4 - a)(a + 1)(a - 1)(a + 4)$$

$$27. x^2 + 1/x^2 - 11$$

Solution:

$$\text{We have, } x^2 + 1/x^2 - 11$$

$$= x^2 + 1/x^2 - 2 - 9$$

$$= (x^2 + 1/x^2 - 2 \times x \times 1/x) - 9$$

$$= (x - 1/x)^2 - 9$$

$$= (x - 1/x + 3)(x - 1/x - 3) \text{ [As } a^2 - b^2 = (a + b)(a - b)]$$

$$28. 4x^2 + 1/4x^2 + 1$$

Solution:

$$\text{We have, } 4x^2 + 1/4x^2 + 1$$

$$= 4x^2 + 1/4x^2 + 2 - 1$$

$$= [(2x)^2 + (1/2x)^2 + 2 \times 2x \times 1/2x] - 1$$

$$= (2x + 1/2x)^2 - 1$$

$$= (2x + 1/2x + 1)(2x + 1/2x - 1) \text{ [As } x^2 - y^2 = (x + y)(x - y)]$$

$$29. 4x^4 - x^2 - 12x - 36$$

Solution:

$$\text{We know, } 4x^4 - x^2 - 12x - 36$$

$$= 4x^4 - (x^2 + 12x + 36)$$

$$= (2x^2)^2 - [x^2 + 2(x)(6) + 6^2]$$

$$= (2x^2)^2 - (x + 6)^2$$

$$= (2x^2 + x + 6)(2x^2 - x - 6) \text{ [As } x^2 - y^2 = (x + y)(x - y)]$$

$$= (2x^2 + x + 6)(2x^2 - 4x + 3x - 6) \text{ [By splitting the middle term]}$$

$$= (2x^2 + x + 6) [2x(x - 2) + 3(x - 2)]$$

$$= (2x^2 + x + 6) [(2x + 3)(x - 2)]$$

$$= (2x^2 + x + 6)(2x + 3)(x - 2)$$

$$30. a^2(b + c) - (b + c)^3$$

Solution:

$$\text{We have, } a^2(b + c) - (b + c)^3$$

$$= (b + c) [a^2 - (b + c)^2]$$

$$= (b + c) [(a - b - c)(a + b + c)] \text{ [As } x^2 - y^2 = (x + y)(x - y)\text{]}$$

$$= (b + c)(a - b - c)(a + b + c)$$

Exercise 5(D)

Factorize:

$$1. a^3 - 27$$

Solution:

$$\text{We have, } a^3 - 27$$

$$= a^3 - 3^3$$

$$= (a - 3) [a^2 + (a \times 3) + 3^2] \text{ [As, } a^3 - b^3 = (a - b)(a^2 + ab + b^2)\text{]}$$

$$= (a - 3)(a^2 + 3a + 9)$$

$$2. 1 - 8a^3$$

Solution:

$$\text{We have, } 1 - 8a^3$$

$$= 1^3 - (2a)^3$$

$$= (1 - 2a) [12 + (1 \times 2a) + (2a)^2]$$

$$= (1 - 2a) (1 + 2a + 4a^2) \text{ [As, } a^3 - b^3 = (a - b) (a^2 + ab + b^2)]$$

$$3. 64 - a^3b^3$$

Solution:

We have, $64 - a^3b^3$

$$= 4^3 - (ab)^3$$

$$= (4 - ab) [4^2 + (4 \times ab) + (ab)^2]$$

$$= (4 - ab) (16 + 4ab + a^2b^2) \text{ [As, } a^3 - b^3 = (a - b) (a^2 + ab + b^2)]$$

$$4. a^6 + 27b^3$$

Solution:

We have, $a^6 + 27b^3$

$$= (a^2)^3 + (3b)^3$$

$$= (a^2 + 3b) [(a^2)^2 - (a^2 \times 3b) + (3b)^2]$$

$$= (a^2 + 3b) (a^4 - 3a^2b + 9b^2) \text{ [As, } a^3 + b^3 = (a + b) (a^2 - ab + b^2)]$$

$$5. 3x^7y - 81x^4y^4$$

Solution:

We have, $3x^7y - 81x^4y^4$

$$= 3xy (x^6 - 27x^3y^3)$$

$$= 3xy [(x^2)^3 - (3xy)^3]$$

$$= 3xy (x^2 - 3xy) [(x^2)^2 + (x^2 \times 3xy) + (3xy)^2] \text{ [As, } a^3 - b^3 = (a - b) (a^2 + ab + b^2)]$$

$$= 3xy (x^2 - 3xy) (x^4 + 3x^3y + 9x^2y^2)$$

$$= 3xy \cdot x(x - 3y) \cdot x^2(x^2 + 3xy + 9y^2) \text{ [Taking common from terms]}$$

$$= 3x^4y (x - 3y) (x^2 + 3xy + 9y^2)$$

$$6. a^3 - 27/a^3$$

Solution:

We have, $a^3 - 27/a^3$

$$= a^3 - (3/a)^3$$

$$= (a - 3/a) [a^2 + a \times 3/a + (3/a)^2] \text{ [As, } a^3 - b^3 = (a - b) (a^2 + ab + b^2)]$$

$$= (a - 3/a) (a^2 + 3 + 9/a^2)$$

$$7. a^3 + 0.064$$

Solution:

We have, $a^3 + 0.064$

$$= a^3 + (0.4)^3$$

$$= (a + 0.4) [a^2 - (a \times 0.4) + 0.4^2]$$

$$= (a + 0.4) (a^2 - 0.4a + 0.16) \text{ [As, } a^3 + b^3 = (a + b) (a^2 - ab + b^2)]$$

$$8. a^4 - 343a$$

Solution:

We have, $a^4 - 343a$

$$= a (a^3 - 343)$$

$$= a (a^3 - 7^3)$$

$$= a (a - 7) [a^2 + (a \times 7) + 7^2] \text{ [As, } a^3 - b^3 = (a - b) (a^2 + ab + b^2)]$$

$$= a (a - 7) (a^2 + 7a + 49)$$

$$9. (x - y)^3 - 8x^3$$

Solution:

We have, $(x - y)^3 - 8x^3$

$$= (x - y)^3 - (2x)^3$$

$$= (x - y - 2x) [(x - y)^2 + 2x(x - y) + (2x)^2] \text{ [As, } a^3 - b^3 = (a - b)(a^2 + ab + b^2)\text{]}$$

$$= (-x - y) [x^2 + y^2 - 2xy + 2x^2 - 2xy + 4x^2]$$

$$= -(x + y) [7x^2 - 4xy + y^2]$$

$$10. 8a^3/27 - b^3/8$$

Solution:

We have, $8a^3/27 - b^3/8$

$$= (2a/3)^3 - (b/2)^3$$

$$= (2a/3 - b/2) [(2a/3)^2 + (2a/3 \times b/2) + (b/2)^2] \text{ [As, } a^3 - b^3 = (a - b)(a^2 + ab + b^2)\text{]}$$

$$= (2a/3 - b/2) (4a^2/9 + ab/3 + b^2/4)$$

$$11. a^6 - b^6$$

Solution:

We have, $a^6 - b^6$

$$= (a^3)^2 - (b^3)^2$$

$$= (a^3 + b^3)(a^3 - b^3) \text{ [As } x^2 - y^2 = (x + y)(x - y)\text{]}$$

Now,

$$= [(a + b)(a^2 - ab + b^2)] [(a - b)(a^2 + ab + b^2)] \text{ [Using identities]}$$

$$= (a + b)(a - b)(a^2 - ab + b^2)(a^2 + ab + b^2)$$

$$12. a^6 - 7a^3 - 8$$

Solution:

We have, $a^6 - 7a^3 - 8$

By splitting the middle term,

$$= a^6 - 8a^3 + a^3 - 8$$

$$= a^3(a^3 - 8) + 1(a^3 - 8)$$

$$= (a^3 + 1)(a^3 - 8)$$

We know that,

$$a^3 - b^3 = (a - b)(a^2 + ab + b^2) \dots (1)$$

$$a^3 + b^3 = (a + b)(a^2 - ab + b^2) \dots (2)$$

Now,

$$(a^3 + 1)(a^3 - 8)$$

$$= [(a + 1)(a^2 - a + 1)][(a - 2)(a^2 + 2a + 4)] \dots \text{[Using (1) and (2)]}$$

$$= (a + 1)(a - 2)(a^2 + 2a + 4)(a^2 - a + 1)$$

$$13. a^3 - 27b^3 + 2a^2b - 6ab^2$$

Solution:

$$\text{We have, } a^3 - 27b^3 + 2a^2b - 6ab^2$$

$$= [a^3 - (3b)^3] + 2ab(a - 3b)$$

$$= (a - 3b)(a^2 + 3ab + 9b^2) + 2ab(a - 3b) \text{ [As, } a^3 - b^3 = (a - b)(a^2 + ab + b^2)]$$

Now, taking $(a - 3b)$ as common

$$= (a - 3b)[(a^2 + 3ab + 9b^2) + 2ab]$$

$$= (a - 3b)(a^2 + 5ab + 9b^2)$$

$$14. 8a^3 - b^3 - 4ax + 2bx$$

Solution:

$$\text{We have, } 8a^3 - b^3 - 4ax + 2bx$$

$$= (2a)^3 - b^3 - 2x(2a - b)$$

$$= (2a - b) [(2a)^2 - 2ab + b^2] - 2x(2a - b)$$

Taking $(2a - b)$ as common,

$$= (2a - b) [(4a^2 + 2ab + b^2) - 2x]$$

$$= (2a - b) (4a^2 + 2ab + b^2 - 2x)$$

$$15. a - b - a^3 + b^3$$

Solution:

We have, $a - b - a^3 + b^3$

$$= (a - b) - (a^3 - b^3)$$

$$= (a - b) - [(a - b) (a^2 + ab + b^2)] \text{ [As, } a^3 - b^3 = (a - b) (a^2 + ab + b^2)]$$

Now, taking $(a - b)$ as common

$$= (a - b) [1 - (a^2 + ab + b^2)]$$

$$= (a - b) (1 - a^2 - ab - b^2)$$

$$16. 2x^3 + 54y^3 - 4x - 12y$$

Solution:

We have, $2x^3 + 54y^3 - 4x - 12y$

$$= 2(x^3 + 27y^3 - 2x - 6y)$$

Now,

$$= 2 \{[(x)^3 + (3y)^3] - 2(x + 3y)\}$$

$$= 2 \{[(x + 3y) (x^2 - 3xy + 9y^2)] - 2(x + 3y)\} \text{ [As, } a^3 + b^3 = (a + b) (a^2 - ab + b^2)]$$

$$= 2 (x + 3y) (x^2 - 3xy + 9y^2 - 2)$$

$$17. 1029 - 3x^3$$

Solution:

We have, $1029 - 3 \times 3$

$$= 3(343 - x^3)$$

$$= 3(7^3 - x^3)$$

$$= 3(7 - x)(7^2 + 7x + x^2) \text{ [As, } a^3 - b^3 = (a - b)(a^2 + ab + b^2)]$$

$$= 3(7 - x)(49 + 7x + x^2)$$

18. Show that:

(i) $13^3 - 5^3$ is divisible by 8

(ii) $35^3 + 27^3$ is divisible by 62

Solution:

(i) We have, $(13^3 - 5^3)$

Now, using identity $(a^3 - b^3) = (a - b)(a^2 + ab + b^2)$

$$= (13 - 5)(13^2 + 13 \times 5 + 5^2)$$

$$= 8 \times (169 + 65 + 25)$$

Hence, the number is divisible by 8.

(ii) $(35^3 + 27^3)$

Now, using identity $(a^3 + b^3) = (a + b)(a^2 - ab + b^2)$

$$= (35 + 27)(35^2 + 35 \times 27 + 27^2)$$

$$= 62 \times (35^2 + 35 \times 27 + 27^2)$$

Hence, the number is divisible by 62.

19. Evaluate:

Solution:

Let $a = 5.67$ and $b = 4.33$

Then,

$$= a + b$$

$$= 5.67 + 4.33$$

$$= 10$$

Exercise 5(E)

Factorize:

1. $x^2 + \frac{1}{4}x^2 + 1 - 7x - \frac{7}{2}x$

Solution:

We have,

$$= [x^2 + \frac{1}{4}(2x)^2 + 2 \times x \times \frac{1}{2}(2x)] - 7 [x + \frac{1}{2}(2x)]$$

$$= (x + \frac{1}{2}x)^2 - 7(x + 1/x)$$

Taking out $(x + \frac{1}{2}x)$ as common,

$$= (x + \frac{1}{2}x) (x + \frac{1}{2}x - 7)$$

2. $9a^2 + \frac{1}{9}a^2 - 2 - 12a + \frac{4}{3}a$

Solution:

3. $x^2 + (a^2 + 1) \frac{x}{a} + 1$

Solution:

4. $x^4 + y^4 - 27x^2y^2$

Solution:

We have, $x^4 + y^4 - 27x^2y^2$

$$= x^4 + y^4 - 2x^2y^2 - 25x^2y^2$$

$$= [(x^2) + (y^2) - 2x^2y^2] - 25x^2y^2$$

$$= (x^2 - y^2) - (5xy)^2$$

$$= (x^2 - y^2 - 5xy)(x^2 - y^2 + 5xy) \text{ [As } x^2 - y^2 = (x + y)(x - y)\text{]}$$

5. $4x^4 + 9y^4 + 11x^2y^2$

Solution:

We have, $4x^4 + 9y^4 + 11x^2y^2$

$$= 4x^4 + 9y^4 + 12x^2y^2 - x^2y^2$$

$$= (2x^2)^2 + (3y^2)^2 + 2(2x^2)(3y^2) - (xy)^2$$

$$= (2x^2 + 3y^2)^2 - (xy)^2$$

$$= (2x^2 + 3y^2 - xy)(2x^2 + 3y^2 + xy) \text{ [As } x^2 - y^2 = (x + y)(x - y)\text{]}$$

6. $x^2 + 1/x^2 - 3$

Solution:

We have, $x^2 + 1/x^2 - 3$

$$= x^2 + 1/x^2 - 2 - 1$$

$$= [x^2 + 1/x^2 - (2 \times x \times 1/x)] - 1$$

$$= (x - 1/x)^2 - 1$$

$$= (x - 1/x - 1)(x - 1/x + 1) \text{ [As } x^2 - y^2 = (x + y)(x - y)\text{]}$$

7. $a^2 - b^2 - 4a^2 + 4b^2$

Solution:

We have, $a - b - 4a^2 + 4b^2$

$$= (a - b) - 4(a^2 - b^2)$$

$$= (a - b) - 4(a - b)(a + b) \text{ [As } x^2 - y^2 = (x + y)(x - y)\text{]}$$

Taking $(a - b)$ common,

$$= (a - b) [1 - 4(a + b)]$$

$$= (a - b) [1 - 4a - 4b]$$

$$8. (2a - 3)^2 - 2(2a - 3)(a - 1) + (a - 1)^2$$

Solution:

$$\text{We have, } (2a - 3)^2 - 2(2a - 3)(a - 1) + (a - 1)^2$$

Comparing with the identity, $(a - b)^2 = a^2 - 2ab + b^2$

$$= [(2a - 3) - (a - 1)]^2$$

$$= (2a - a - 3 + 1)^2$$

$$= (a - 2)^2$$

$$9. (a^2 - 3a)(a^2 - 3a + 7) + 10$$

Solution:

$$\text{Let's substitute } (a^2 - 3a) = x$$

Then the given expression becomes,

$$= x(x + 7) + 10$$

$$= x^2 + 7x + 10$$

$$= x^2 + 5x + 2x + 10 \text{ [By splitting the middle term]}$$

$$= x(x + 5) + 2(x + 5)$$

$$= (x + 2)(x + 5)$$

Resubstituting the value of x,

$$= (a^2 - 3a + 2) (a^2 - 3a + 5)$$

$$= (a^2 - 3a + 5) (a^2 - 3a + 2)$$

$$= (a^2 - 3a + 5) [a^2 - 2a - a + 2] \text{ [By splitting the middle term]}$$

$$= (a^2 - 3a + 5) [a(a - 2) - 1(a - 5)]$$

$$= (a^2 - 3a + 5) [(a - 1) (a - 2)]$$

$$= (a^2 - 3a + 5) (a - 1) (a - 2)$$

$$10. (a^2 - a) (4a^2 - 4a - 5) - 6$$

Solution:

$$\text{Let's } a^2 - a = x$$

Then the expression becomes,

$$= x(4x - 5) - 6$$

$$= 4x^2 - 5x - 6$$

$$= 4x^2 - 8x + 3x - 6$$

$$= 4x(x - 2) + 3(x - 2)$$

$$= (4x + 3) (x - 2)$$

Resubstituting the value of x,

$$= (4a^2 - 4a + 3) (a^2 - a - 2)$$

$$= (4a^2 - 4a + 3) (a^2 - 2a + a - 2)$$

$$= (4a^2 - 4a + 3) [a(a - 2) + 1(a - 2)]$$

$$= (4a^2 - 4a + 3) [(a + 1) (a - 2)]$$

$$= (4a^2 - 4a + 3) (a + 1) (a - 2)$$

$$11. x^4 + y^4 - 3x^2y^2$$

Solution:

We have, $x^4 + y^4 - 3x^2y^2$

$$= (x^4 + y^4 - 2x^2y^2) - x^2y^2$$

$$= (x^2 - y^2)^2 - (xy)^2 \text{ [As } x^2 - y^2 = (x + y)(x - y)\text{]}$$

$$= (x^2 - y^2 - xy)(x^2 - y^2 + xy)$$

$$12. 5a^2 - b^2 - 4ab + 7a - 7b$$

Solution:

We have, $5a^2 - b^2 - 4ab + 7a - 7b$

$$= 4a^2 + a^2 - b^2 - 4ab + 7a - 7b$$

$$= a^2 - b^2 + 4a^2 - 4ab + 7a - 7b$$

$$= (a^2 - b^2) + 4a(a - b) + 7(a - b)$$

$$= (a + b)(a - b) + 4a(a - b) + 7(a - b) \text{ [As } x^2 - y^2 = (x + y)(x - y)\text{]}$$

$$= (a - b) [(a + b) + 4a + 7]$$

$$= (a - b) (5a + b + 7)$$

$$13. 12(3x - 2y)^2 - 3x + 2y - 1$$

Solution:

We have, $12(3x - 2y)^2 - 3x + 2y - 1$

$$= 12(3x - 2y)^2 - (3x - 2y) - 1$$

Let's substitute $(3x - 2y) = a$

Then, the expression becomes

$$= 12a^2 - a - 1$$

$$= 12a^2 - 4a + 3a - 1$$

$$= 4a(3a - 1) + 1(3a - 1)$$

$$= (4a + 1)(3a - 1)$$

Now, resubstituting the value of 'a' in the above

$$= [4(3x - 2y) + 1][3(3x - 2y) - 1]$$

$$= (12x - 8y + 1)(9x - 6y - 1)$$

$$14. 4(2x - 3y)^2 - 8x + 12y - 3$$

Solution:

$$\text{We have, } 4(2x - 3y)^2 - 8x + 12y - 3$$

$$= 4(2x - 3y)^2 - 4(2x + 3y) - 3$$

$$\text{Let's substitute } (2x - 3y) = a$$

$$= 4(a^2) - 4a - 3$$

$$= 4a^2 - 6a + 2a - 3 \text{ [By splitting the middle term]}$$

$$= 2a(2a - 3) + 1(2a - 3)$$

$$= (2a - 3)(2a + 1)$$

Now, resubstituting the value of 'a' in the above

$$= [2(2x - 3y) - 3][2(2x - 3y) + 1]$$

$$= (4x - 6y - 3)(4x - 6y + 1)$$

$$15. 3 - 5x + 5y - 12(x - y)^2$$

Solution:

$$\text{We have, } 3 - 5x + 5y - 12(x - y)^2$$

$$= 3 - 5(x - y) - 12(x - y)^2$$

Let's substitute $(x - y) = a$

$$= 3 - 5a - 12a^2$$

$$= 3 - 9a + 4a - 12a^2 \text{ [By splitting the middle term]}$$

$$= 3(1 - 3a) + 4a(1 - 3a)$$

$$= (1 - 3a)(4a + 3)$$

Now, resubstituting the value of 'a' in the above

$$= [1 - 3(x - y)][4(x - y) + 3]$$

$$= (1 - 3x + 3y)(4x - 4y + 3)$$

$$16. 9x^2 + 3x - 8y - 64y^2$$

Solution:

$$\text{We have, } 9x^2 + 3x - 8y - 64y^2$$

On rearranging,

$$= 9x^2 - 64y^2 + 3x - 8y$$

$$= [(3x)^2 - (8y)^2] + (3x - 8y)$$

$$= (3x - 8y)(3x + 8y) + (3x - 8y) \text{ [As } x^2 - y^2 = (x + y)(x - y)]$$

Taking $(3x - 8y)$ as common,

$$= (3x - 8y)(3x + 8y + 1)$$

$$17. 2\sqrt{3}x^2 + x - 5\sqrt{3}$$

Solution:

$$\text{We have, } 2\sqrt{3}x^2 + x - 5\sqrt{3}$$

By splitting the middle term,

$$= 2\sqrt{3}x^2 + 6x - 5x - 5\sqrt{3}$$

$$= 2\sqrt{3}x(x + \sqrt{3}) - 5(x + \sqrt{3})$$

$$= (2\sqrt{3}x - 5)(x + \sqrt{3})$$

$$18. \frac{1}{4}(a + b)^2 - \frac{9}{16}(2a - b)^2$$

Solution:

$$19. 2(ab + cd) - a^2 - b^2 + c^2 + d^2$$

Solution:

$$\text{We have, } 2(ab + cd) - a^2 - b^2 + c^2 + d^2$$

$$= 2ab + 2cd - a^2 - b^2 + c^2 + d^2$$

On rearranging and grouping, we get

$$= (c^2 + d^2 + 2cd) - (a^2 + b^2 - 2ab)$$

$$= (c + d)^2 - (a - b)^2$$

$$= [c + d - (a - b)][c + d + (a - b)] \text{ [As } x^2 - y^2 = (x + y)(x - y)]$$

$$= (c + d - a + b)(c + d + a - b)$$

20. Find the value of:

$$(i) 9872 - 132$$

$$(ii) (67.8)^2 - (32.2)^2$$

$$(iii) [(6.7)^2 - (3.3)^2] / (6.7 - 3.3)$$

$$(iv) [(18.5)^2 - (6.5)^2] / (18.5 - 6.5)$$

Solution:

$$(i) \text{ We have, } 9872 - 132$$

$$= (987 + 13)(987 - 13)$$

$$= 1000 \times 974$$

$$= 974000$$

(ii) We have, $(67.8)^2 - (32.2)^2$

$$= (67.8 + 32.2) (67.8 - 32.2)$$

$$= 100 \times 35.6$$

$$= 3560$$

Benefits of ICSE Class 9 Maths Selina Solutions Chapter 5 Factorization

1. Helps to plan a preparation strategy

Attempting ICSE Class 9 Maths Selina Solutions Chapter 5 is the best strategy to prepare for the exam. Candidates can plan study table for all subjects and give more time to weak sections. By this candidates can attempt all the questions during the exam. And at the closing time, they have to perfect everything they have learned.

2. Preparation Level Overview

One of the best advantages of ICSE Class 9 Maths Selina Solutions Chapter 5 Factorization is that it helps candidates know where they stand in terms of their preparation level. This helps candidates know where they are lagging behind. Candidates can learn from their mistakes and follow the test exam solutions and strategies.

3. Performance analysis

No one can learn anything unless they analyze their performance. Candidates can know their weak and strong points only by analyzing them. Analyzing the ICSE Class 9 Maths solution Chapter 5 will make the candidates aware that they will not repeat their mistakes in the exam hall. Analyzing the solutions helps the candidate to get an idea of where they stand in the competition to take the ICSE Class 9 Maths Exam.

5. Time planning aids

A candidate cannot afford to deal with a question that takes time. Some questions can be difficult and some can be solved at a glance. ICSE Class 9 Maths Selina Solutions help candidates to develop such skills. Candidates will implement the question solving pattern with right approach which will help them to crack the exam on time. Solving most of the questions in less time, they give the remaining time to the more difficult parts.

6. Improve Accuracy and Speed

It helps candidates to improve accuracy and speed. The more they solve different questions, the better they explain their concepts and tricks. Accuracy and speed are important in the selection process. This will help them clear the upcoming ICSE class 9 Maths Exam.

[wp-faq-schema title="ICSE Class 9 Maths Selina Solutions Chapter 5 FAQs" accordion=1]

Q1. What is Factorization?

Ans. In mathematics, Factorization is writing a number or other mathematical object as the product of several factors, usually the product of smaller or simpler similar objects. For example, 3×5 is an integer factorization of 15 and is a polynomial factorization of $x^2 - 4$.

Q2. Where can I get the ICSE Class 9 Maths Selina Solutions Chapter 5 Factorization?

Ans. You can get the ICSE Class 9 Maths Selina Solutions Chapter 5 - Factorization at PW blog section.

Q3. Is ICSE Class 9 Maths Selina Solutions Chapter 5 PDF available to download?

Ans. Yes, ICSE Class 9 Maths Selina Solutions Chapter 5 PDF is available for download on our page.

Q4. What are the Benefits of ICSE Class 9 Maths Selina Solutions Chapter 5 Factorization?

Ans. The details Benefits of ICSE Class 9 Maths Selina Solutions Chapter 5 Factorization are provided in the above article.

Q5. Are ICSE Class 9 Maths Selina Solutions Chapter 5 useful for exam preparation?

Ans. Yes, these ICSE Class 9 Maths Selina Solutions Chapter 5 are extremely beneficial for exam preparation. They cover all topics and exercises prescribed in the ICSE curriculum, ensuring comprehensive revision and practice.