

ICSE Class 10 Maths Selina Solutions Chapter 15: Two figures are considered comparable when their shapes are the same, but their sizes are different. Triangle resemblance is the subject of this ICSE Class 10 Maths Selina Solutions Chapter 15. The main ideas covered in this chapter include the fundamentals of understanding corresponding sides and corresponding angles of similar triangles, different conditions for two triangles to be similar, the Basic Proportionality Theorem, the relationship between the areas of two triangles, similarity as a size transformation, and finally applications to maps and models.

Students can consult ICSE Class 10 Maths Selina Solutions Chapter 15, which are created by knowledgeable our faculty members, if they are having trouble with the problems in this chapter or others.

ICSE Class 10 Maths Selina Solutions Chapter 15 Overview

ICSE Class 10 Maths Selina Solutions Chapter 15, focused on Similarity, explores the concept of similarity in geometric figures, particularly triangles. ICSE Class 10 Maths Selina Solutions Chapter 15 for this chapter provide clear explanations and step-by-step solutions to problems involving similar triangles, ratios, and their properties.

Through practice exercises and detailed explanations, these ICSE Class 10 Maths Selina Solutions Chapter 15 help students grasp the criteria for similarity and apply them effectively. This chapter is essential for understanding geometric relationships and preparing for the ICSE Class 10 Maths exam, ensuring students develop confidence in handling similarity problems.

ICSE Class 10 Maths Selina Solutions Chapter 15

Below we have provided ICSE Class 10 Maths Selina Solutions Chapter 15 –

1. In the figure, given below, straight lines AB and CD intersect at P; and $AC \parallel BD$. Prove that:

(i) $\triangle APC$ and $\triangle BPD$ are similar.

(ii) If $BD = 2.4$ cm, $AC = 3.6$ cm, $PD = 4.0$ cm and $PB = 3.2$ cm; find the lengths of PA and PC.

Solution:

(i) In $\triangle APC$ and $\triangle BPD$, we have

$$\angle APC = \angle BPD \text{ [Vertically opposite angles]}$$

$$\angle ACP = \angle BDP \text{ [Alternate angles as, } AC \parallel BD]$$

Thus, $\triangle APC \sim \triangle BPD$ by AA similarity criterion

(ii) So, by corresponding parts of similar triangles, we have

$$PA/PB = PC/PD = AC/BD$$

Given, $BD = 2.4$ cm, $AC = 3.6$ cm, $PD = 4.0$ cm and $PB = 3.2$ cm

$$PA/(3.2) = PC/4 = 3.6/2.4$$

$$PA/3.2 = 3.6/2.4 \text{ and } PC/4 = 3.6/2.4$$

Thus,

$$PA = (3.6 \times 3.2) / 2.4 = 4.8 \text{ cm and}$$

$$PC = (3.6 \times 4) / 2.4 = 6 \text{ cm}$$

2. In a trapezium ABCD, side AB is parallel to side DC; and the diagonals AC and BD intersect each other at point P. Prove that:

(i) $\triangle APB$ is similar to $\triangle CPD$.

(ii) $PA \times PD = PB \times PC$.

Solution:

(i) In $\triangle APB$ and $\triangle CPD$, we have

$$\angle APB = \angle CPD \text{ [Vertically opposite angles]}$$

$$\angle ABP = \angle CDP \text{ [Alternate angles as, } AB \parallel DC]$$

Thus, $\triangle APB \sim \triangle CPD$ by AA similarity criterion.

(ii) As $\triangle APB \sim \triangle CPD$

Since the corresponding sides of similar triangles are proportional, we have

$$PA/PC = PB/PD$$

Thus,

$$PA \times PD = PB \times PC$$

3. P is a point on side BC of a parallelogram ABCD. If DP produced meets AB produced at point L, prove that:

(i) $DP : PL = DC : BL$.

(ii) $DL : DP = AL : DC$.

Solution:

(i) As $AD \parallel BC$, we have $AD \parallel BP$ also.

So, by BPT

$$DP/PL = AB/BL$$

And, since ABCD is a parallelogram, $AB = DC$

Hence,

$$DP/PL = DC/BL$$

i.e., $DP : PL = DC : BL$

(ii) As $AD \parallel BC$, we have $AD \parallel BP$ also.

So, by BPT

$$DL/DP = AL/AB$$

And, since ABCD is a parallelogram, $AB = DC$

Hence,

$$DL/DP = AL/AB$$

i.e., $DL : DP = AL : DC$

4. In quadrilateral ABCD, the diagonals AC and BD intersect each other at point O. If $AO = 2CO$ and $BO = 2DO$; show that:

(i) ΔAOB is similar to ΔCOD .

(ii) $OA \times OD = OB \times OC$.

Solution:

(i) Given,

$$AO = 2CO \text{ and } BO = 2DO,$$

$$AO/CO = 2/1 = BO/DO$$

And,

$$\angle AOB = \angle DOC \text{ [Vertically opposite angles]}$$

Hence, $\triangle AOB \sim \triangle COD$ [SAS criterion for similarity]

$$(ii) \text{ As, } AO/CO = 2/1 = BO/DO \text{ [Given]}$$

Thus,

$$OA \times OD = OB \times OC$$

5. In $\triangle ABC$, angle ABC is equal to twice the angle ACB , and bisector of angle ABC meets the opposite side at point P . Show that :

$$(i) \text{ } CB : BA = CP : PA$$

$$(ii) \text{ } AB \times BC = BP \times CA$$

Solution:

(i) In $\triangle ABC$, we have

$$\angle ABC = 2 \angle ACB \text{ [Given]}$$

Now, let $\angle ACB = x$

$$\text{So, } \angle ABC = 2x$$

Also given, BP is bisector of $\angle ABC$

$$\text{Thus, } \angle ABP = \angle PBC = x$$

By using the angle bisector theorem,

i.e. the bisector of an angle divides the side opposite to it in the ratio of other two sides.

Therefore, $CB : BA = CP : PA$.

(ii) In $\triangle ABC$ and $\triangle APB$,

$$\angle ABC = \angle APB \text{ [Exterior angle property]}$$

$$\angle BCP = \angle ABP \text{ [Given]}$$

Thus, $\triangle ABC \sim \triangle APB$ by AA criterion for similarity

Now, since corresponding sides of similar triangles are proportional we have

$$CA/AB = BC/BP$$

Therefore, $AB \times BC = BP \times CA$

6. In $\triangle ABC$, $BM \perp AC$ and $CN \perp AB$; show that:

$$\frac{AB}{AC} = \frac{BM}{CN} = \frac{AM}{AN}$$

Solution:

In $\triangle ABM$ and $\triangle ACN$,

$$\angle AMB = \angle ANC \text{ [Since, } BM \perp AC \text{ and } CN \perp AB]$$

$$\angle BAM = \angle CAN \text{ [Common angle]}$$

Hence, $\triangle ABM \sim \triangle ACN$ by AA criterion for similarity

So, by corresponding sides of similar triangles we have

$$\frac{AB}{AC} = \frac{BM}{CN} = \frac{AM}{AN}$$

7. In the given figure, $DE \parallel BC$, $AE = 15$ cm, $EC = 9$ cm, $NC = 6$ cm and $BN = 24$ cm.

(i) Write all possible pairs of similar triangles.

(ii) Find the lengths of ME and DM .

Solution:

(i) In $\triangle AME$ and $\triangle ANC$,

$$\angle AME = \angle ANC \text{ [Since } DE \parallel BC \text{ so, } ME \parallel NC]$$

$$\angle MAE = \angle NAC \text{ [Common angle]}$$

Hence, $\triangle AME \sim \triangle ANC$ by AA criterion for similarity

In $\triangle ADM$ and $\triangle ABN$,

$$\angle ADM = \angle ABN \text{ [Since } DE \parallel BC \text{ so, } DM \parallel BN]$$

$$\angle DAM = \angle BAN \text{ [Common angle]}$$

Hence, $\triangle ADM \sim \triangle ABN$ by AA criterion for similarity

In $\triangle ADE$ and $\triangle ABC$,

$$\angle ADE = \angle ABC \text{ [Since } DE \parallel BC \text{ so, } ME \parallel NC]$$

$$\angle AED = \angle ACB \text{ [Since } DE \parallel BC]$$

Hence, $\triangle ADE \sim \triangle ABC$ by AA criterion for similarity

(ii) Proved above that, $\triangle AME \sim \triangle ANC$

So as corresponding sides of similar triangles are proportional, we have

$$ME/NC = AE/AC$$

$$ME/6 = 15/24$$

$$ME = 3.75 \text{ cm}$$

And, $\triangle ADE \sim \triangle ABC$ [Proved above]

So as corresponding sides of similar triangles are proportional, we have

$$AD/AB = AE/AC = 15/24 \dots (1)$$

Also, $\triangle ADM \sim \triangle ABN$ [Proved above]

So as corresponding sides of similar triangles are proportional, we have

$$DM/BN = AD/AB = 15/24 \dots \text{ From (1)}$$

$$DM/24 = 15/24$$

$$DM = 15 \text{ cm}$$

8. In the given figure, $AD = AE$ and $AD^2 = BD \times EC$. Prove that: triangles ABD and CAE are similar.

Solution:

In $\triangle ABD$ and $\triangle CAE$,

$$\angle ADE = \angle AED \text{ [Angles opposite to equal sides are equal.]}$$

$$\text{So, } \angle ADB = \angle AEC \text{ [As } \angle ADB + \angle ADE = 180^\circ \text{ and } \angle AEC + \angle AED = 180^\circ]$$

And, $AD^2 = BD \times EC$ [Given]

$$AD/BD = EC/AD$$

$$AD/BD = EC/AE$$

Thus, $\triangle ABD \sim \triangle CAE$ by SAS criterion for similarity.

9. In the given figure, $AB \parallel DC$, $BO = 6$ cm and $DQ = 8$ cm; find: $BP \times DO$.

Solution:

In $\triangle DOQ$ and $\triangle BOP$,

$$\angle QDO = \angle PBO \text{ [As } AB \parallel DC \text{ so, } PB \parallel DQ.]$$

$$\text{So, } \angle DOQ = \angle BOP \text{ [Vertically opposite angles]}$$

Hence, $\triangle DOQ \sim \triangle BOP$ by AA criterion for similarity

Since, corresponding sides of similar triangles are proportional we have

$$DO/BO = DQ/BP$$

$$DO/6 = 8/BP$$

$$BP \times DO = 48 \text{ cm}^2$$

10. Angle BAC of triangle ABC is obtuse and $AB = AC$. P is a point in BC such that $PC = 12$ cm. PQ and PR are perpendiculars to sides AB and AC respectively. If $PQ = 15$ cm and $PR = 9$ cm; find the length of PB .

Solution:

In $\triangle ABC$,

$$AC = AB \text{ [Given]}$$

$$\text{So, } \angle ABC = \angle ACB \text{ [Angles opposite to equal sides are equal.]}$$

In $\triangle PRC$ and $\triangle PQB$,

$$\angle ABC = \angle ACB$$

$$\angle PRC = \angle PQB \text{ [Both are right angles.]}$$

Hence, $\triangle PRC \sim \triangle PQB$ by AA criterion for similarity

Since, corresponding sides of similar triangles are proportional we have

$$PR/PQ = RC/QB = PC/PB$$

$$PR/PQ = PC/PB$$

$$9/15 = 12/PB$$

Thus,

$$PB = 20 \text{ cm}$$

11. State, true or false:

(i) Two similar polygons are necessarily congruent.

(ii) Two congruent polygons are necessarily similar.

(iii) All equiangular triangles are similar.

(iv) All isosceles triangles are similar.

(v) Two isosceles-right triangles are similar.

(vi) Two isosceles triangles are similar, if an angle of one is congruent to the corresponding angle of the other.

(vii) The diagonals of a trapezium, divide each other into proportional segments.

Solution:

(i) False

(ii) True

(iii) True

(iv) False

(v) True

(vi) True

(vii) True

12. Given: $\angle GHE = \angle DFE = 90^\circ$, $DH = 8$, $DF = 12$, $DG = 3x - 1$ and $DE = 4x + 2$.

Find: the lengths of segments DG and DE.

Solution:

In $\triangle DHG$ and $\triangle DFE$,

$$\angle GHD = \angle DFE = 90^\circ$$

$$\angle D = \angle D \text{ [Common]}$$

Thus, $\triangle DHG \sim \triangle DFE$ by AA criterion for similarity

So, we have

$$DH/DF = DG/DE$$

$$8/12 = (3x - 1)/(4x + 2)$$

$$32x + 16 = 36x - 12$$

$$28 = 4x$$

$$x = 7$$

Hence,

$$DG = 3 \times 7 - 1 = 20$$

$$DE = 4 \times 7 + 2 = 30$$

13. D is a point on the side BC of triangle ABC such that angle ADC is equal to angle BAC. Prove that: $CA^2 = CB \times CD$.

Solution:

In $\triangle ADC$ and $\triangle BAC$,

$$\angle ADC = \angle BAC \text{ [Given]}$$

$$\angle ACD = \angle ACB \text{ [Common]}$$

Thus, $\triangle ADC \sim \triangle BAC$ by AA criterion for similarity

So, we have

$$CA/CB = CD/CA$$

Therefore,

$$CA^2 = CB \times CD$$

14. In the given figure, $\triangle ABC$ and $\triangle AMP$ are right angled at B and M respectively.

Given $AC = 10$ cm, $AP = 15$ cm and $PM = 12$ cm.

(i) $\triangle ABC \sim \triangle AMP$.

(ii) Find AB and BC.

Solution:

(i) In $\triangle ABC$ and $\triangle AMP$, we have

$$\angle BAC = \angle PAM \text{ [Common]}$$

$$\angle ABC = \angle PMA \text{ [Each} = 90^\circ]$$

Hence, $\triangle ABC \sim \triangle AMP$ by AA criterion for similarity

(ii) Now, in right triangle AMP

By using Pythagoras theorem, we have

$$AM = \sqrt{AP^2 - PM^2} = \sqrt{15^2 - 12^2} = 9$$

As $\triangle ABC \sim \triangle AMP$,

$$AB/AM = BC/PM = AC/AP$$

$$AB/9 = BC/12 = 10/15$$

So,

$$AB/9 = 10/15$$

$$AB = (10 \times 9) / 15 = 6 \text{ cm}$$

$$BC/12 = 10/15$$

$$BC = 8 \text{ cm}$$

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Exercise 15(B)

1. In the following figure, point D divides AB in the ratio 3: 5. Find:

(i) AE/EC (ii) AD/AB (iii) AE/AC

Also if,

(iv) $DE = 2.4$ cm, find the length of BC .

(v) $BC = 4.8$ cm, find the length of DE .

Solution:

(i) Given, $AD/DB = 3/5$

And $DE \parallel BC$.

So, by Basic Proportionality theorem, we have

$$AD/DB = AE/EC$$

$$AE/EC = 3/5$$

(ii) Given, $AD/DB = 3/5$

$$\text{So, } DB/AD = 5/3$$

Adding 1 both sides, we get

$$DB/AD + 1 = 5/3 + 1$$

$$(DB + AD)/AD = (5 + 3)/3$$

$$AB/AD = 8/3$$

Therefore,

$$AD/AB = 3/8$$

(iii) In $\triangle ABC$, as $DE \parallel BC$

By BPT, we have

$$AD/DB = AE/EC$$

$$\text{So, } AD/AB = AE/AC$$

From above, we have $AD/AB = 3/8$

Therefore,

$$AE/AC = 3/8$$

(iv) In $\triangle ADE$ and $\triangle ABC$,

$\angle ADE = \angle ABC$ [As $DE \parallel BC$, corresponding angles are equal.]

$\angle A = \angle A$ [Common angle]

Hence, $\triangle ADE \sim \triangle ABC$ by AA criterion for similarity

So, we have

$$AD/AB = DE/BC$$

$$3/8 = 2.4/BC$$

$$BC = 6.4 \text{ cm}$$

(v) Since, $\triangle ADE \sim \triangle ABC$ by AA criterion for similarity

So, we have

$$AD/AB = DE/BC$$

$$3/8 = DE/4.8$$

$$DE = 1.8 \text{ cm}$$

2. In the given figure, $PQ \parallel AB$; $CQ = 4.8 \text{ cm}$ $QB = 3.6 \text{ cm}$ and $AB = 6.3 \text{ cm}$. Find:

(i) CP/PA (ii) PQ (iii) If $AP = x$, then the value of AC in terms of x .

Solution:

(i) In $\triangle CPQ$ and $\triangle CAB$,

$\angle PCQ = \angle APQ$ [As $PQ \parallel AB$, corresponding angles are equal.]

$\angle C = \angle C$ [Common angle]

Hence, $\triangle CPQ \sim \triangle CAB$ by AA criterion for similarity

So, we have

$$CP/CA = CQ/CB$$

$$CP/CA = 4.8/8.4 = 4/7$$

$$\text{Thus, } CP/PA = 4/3$$

(ii) As, $\triangle CPQ \sim \triangle CAB$ by AA criterion for similarity

We have,

$$PQ/AB = CQ/CB$$

$$PQ/6.3 = 4.8/8.4$$

$$PQ = 3.6 \text{ cm}$$

(iii) As, $\triangle CPQ \sim \triangle CAB$ by AA criterion for similarity

We have,

$$CP/AC = CQ/CB$$

$$CP/AC = 4.8/8.4 = 4/7$$

So, if AC is 7 parts and CP is 4 parts, then PA is 3 parts.

$$\text{Hence, } AC = 7/3 \times PA = (7/3)x$$

3. A line PQ is drawn parallel to the side BC of $\triangle ABC$ which cuts side AB at P and side AC at Q. If AB = 9.0 cm, CA = 6.0 cm and AQ = 4.2 cm, find the length of AP.

Solution:

In $\triangle APQ$ and $\triangle ABC$,

$$\angle APQ = \angle ABC \text{ [As } PQ \parallel BC, \text{ corresponding angles are equal.]}$$

$$\angle PAQ = \angle BAC \text{ [Common angle]}$$

Hence, $\triangle APQ \sim \triangle ABC$ by AA criterion for similarity

So, we have

$$AP/AB = AQ/AC$$

$$AP/9 = 4.2/6$$

Thus,

$$AP = 6.3 \text{ cm}$$

4. In $\triangle ABC$, D and E are the points on sides AB and AC respectively.

Find whether $DE \parallel BC$, if

(i) AB = 9cm, AD = 4cm, AE = 6cm and EC = 7.5cm.

(ii) AB = 6.3 cm, EC = 11.0 cm, AD = 0.8 cm and EA = 1.6 cm.

(i) In $\triangle ADE$ and $\triangle ABC$,

$$AE/EC = 6/7.5 = 4/5$$

$$AD/BD = 4/5 \text{ [BD = AB - AD = 9 - 4 = 5 cm]}$$

$$\text{So, } AE/EC = AD/BD$$

Therefore, $DE \parallel BC$ by the converse of BPT.

(ii) In $\triangle ADE$ and $\triangle ABC$,

$$AE/EC = 1.6/11 = 0.8/5.5$$

$$AD/BD = 0.8/5.5 \text{ [BD = AB - AD = 6.3 - 0.8 = 5.5 cm]}$$

$$\text{So, } AE/EC = AD/BD$$

Therefore, $DE \parallel BC$ by the converse of BPT.

5. In the given figure, $\triangle ABC \sim \triangle ADE$. If $AE: EC = 4: 7$ and $DE = 6.6$ cm, find BC . If 'x' be the length of the perpendicular from A to DE , find the length of perpendicular from A to BC in terms of 'x'.

Solution:

Given,

$$\triangle ABC \sim \triangle ADE$$

So, we have

$$AE/AC = DE/BC$$

$$4/11 = 6.6/BC$$

$$BC = (11 \times 6.6)/4 = 18.15 \text{ cm}$$

And, also

As $\triangle ABC \sim \triangle ADE$, we have

$$\angle ABC = \angle ADE \text{ and } \angle ACB = \angle AED$$

So, $DE \parallel BC$

And, $AB/AD = AC/AE = 11/4$ [Since, $AE/EC = 4/7$]

In $\triangle ADP$ and $\triangle ABQ$,

$\angle ADP = \angle ABQ$ [As $DP \parallel BQ$, corresponding angles are equal.]

$\angle APD = \angle AQB$ [As $DP \parallel BQ$, corresponding angles are equal.]

Hence, $\triangle ADP \sim \triangle ABQ$ by AA criterion for similarity

$AD/AB = AP/AQ$

$4/11 = x/AQ$

Thus,

$AQ = (11/4)x$

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Exercise 15(C)

1. (i) The ratio between the corresponding sides of two similar triangles is 2: 5. Find the ratio between the areas of these triangles.

(ii) Areas of two similar triangles are 98 sq. cm and 128 sq. cm. Find the ratio between the lengths of their corresponding sides.

Solution:

We know that,

The ratio of the areas of two similar triangles is equal to the ratio of squares of their corresponding sides.

So,

(i) The required ratio is given by,

$$\frac{2^2}{5^2} = \frac{4}{25}$$

(ii) The required ratio is given by,

$$\sqrt[3]{\frac{98}{128}} = \sqrt[3]{\frac{49}{64}} = \frac{7}{8}$$

2. A line PQ is drawn parallel to the base BC of ΔABC which meets sides AB and AC at points P and Q respectively. If $AP = \frac{1}{3} PB$; find the value of:

(i) Area of ΔABC / Area of ΔAPQ

(ii) Area of ΔAPQ / Area of Trapezium PBCQ

Solution:

Given, $AP = \frac{1}{3} PB$

So, $AP/PB = 1/3$

In ΔAPQ and ΔABC ,

As $PQ \parallel BC$, corresponding angles are equal

$\angle APQ = \angle ABC$ and $\angle AQP = \angle ACB$

Hence, $\Delta APQ \sim \Delta ABC$ by AA criterion for similarity

So,

(i) Area of ΔABC / Area of $\Delta APQ = AB^2/ AP^2 = 4^2/1^2 = 16: 1$

[$AP/PB = 1/3$ so, $AB/AP = 4/1$]

(ii) Area of ΔAPQ /Area of Trapezium PBCQ = Area of ΔAPQ /(Area of ΔABC – Area of ΔAPQ)
 $= 1/ (16/ 1) = 1: 16$

3. The perimeters of two similar triangles are 30 cm and 24 cm. If one side of the first triangle is 12 cm, determine the corresponding side of the second triangle.

Solution:

Let $\Delta ABC \sim \Delta DEF$

So, $AB/DE = BC/EF = AC/DF = (AB + BC + AC)/ (DE + EF + DF)$

$= \text{Perimeter of } \Delta ABC / \text{Perimeter of } \Delta DEF$

$\text{Perimeter of } \Delta ABC / \text{Perimeter of } \Delta DEF = AB/DE$

$30/24 = 12/DE$

$$DE = 9.6 \text{ cm}$$

4. In the given figure, AX: XB = 3: 5.

Find:

(i) the length of BC, if the length of XY is 18 cm.

(ii) the ratio between the areas of trapezium XBCY and triangle ABC.

Solution:

$$\text{Given, } AX/XB = 3/5 \Rightarrow AX/AB = 3/8 \dots (1)$$

(i) In ΔAXY and ΔABC ,

As $XY \parallel BC$, corresponding angles are equal.

$$\angle AXY = \angle ABC \text{ and } \angle AYX = \angle ACB$$

Hence, $\Delta AXY \sim \Delta ABC$ by AA criterion for similarity.

So, we have

$$AX/AB = XY/BC$$

$$3/8 = 18/BC$$

$$BC = 48 \text{ cm}$$

$$(ii) \text{ Area of } \Delta AXY / \text{Area of } \Delta ABC = AX^2 / AB^2 = 9/64$$

$$(\text{Area of } \Delta ABC - \text{Area of } \Delta AXY) / \text{Area of } \Delta ABC = (64 - 9) / 64 = 55/64$$

$$\text{Area of trapezium XBCY} / \text{Area of } \Delta ABC = 55/64$$

5. ABC is a triangle. PQ is a line segment intersecting AB in P and AC in Q such that $PQ \parallel BC$ and divides triangle ABC into two parts equal in area. Find the value of ratio BP: AB.

Solution:

It's given that,

$$\text{Ar}(\Delta APQ) = \frac{1}{2} \text{Ar}(\Delta ABC)$$

$$\text{Ar}(\Delta APQ) / \text{Ar}(\Delta ABC) = \frac{1}{2}$$

$$AP^2 / AB^2 = \frac{1}{2}$$

$$AP/AB = 1/\sqrt{2}$$

$$(AB - BP)/AB = 1/\sqrt{2}$$

$$1 - (BP/AB) = 1/\sqrt{2}$$

$$BP/AB = 1 - 1/\sqrt{2}$$

Thus,

$$\frac{BP}{AB} = \frac{\sqrt{2} - 1}{\sqrt{2}} = \frac{2 - \sqrt{2}}{2} \quad [\text{Multiplying by } \sqrt{2} \text{ in both numerator \& denominator}]$$

6. In the given triangle PQR, LM is parallel to QR and PM: MR = 3: 4.

Calculate the value of ratio:

(i) PL/PQ and then LM/QR

(ii) Area of ΔLMN / Area of ΔMNR

(iii) Area of ΔLQM / Area of ΔLQN

Solution:

(i) In ΔPLM and ΔPQR ,

As $LM \parallel QR$, corresponding angles are equal.

$$\angle PLM = \angle PQR$$

$$\angle PML = \angle PRQ$$

Hence, $\Delta PLM \sim \Delta PQR$ by AA criterion for similarity.

So, we have

$$PM/PR = LM/QR$$

$$3/7 = LM/QR \quad [\text{Since, } PM/MR = 3/4 \Rightarrow PM/PR = 3/7]$$

And, by BPT we have

$$PL/LQ = PM/MR = 3/4$$

$$LQ/PL = 4/3$$

$$1 + (LQ/PL) = 1 + 4/3$$

$$(PL + LQ)/PL = (3 + 4)/3$$

$$PQ/PL = 7/3$$

$$\text{Hence, } PL/PQ = 3/7$$

(ii) As ΔLMN and ΔMNR have common vertex at M and their bases LN and NR are along the same straight line

$$\text{Hence, } \text{Ar } (\Delta LMN)/\text{Ar } (\Delta RNQ) = LN/NR$$

Now, in ΔLMN and ΔRNQ we have,

$$\angle NLM = \angle NRQ \text{ [Alternate angles]}$$

$$\angle LMN = \angle NQR \text{ [Alternate angles]}$$

Thus, $\Delta LNM \sim \Delta RNQ$ by AA criterion for similarity.

So,

$$MN/QN = LN/NR = LM/QR = 3/7$$

Therefore,

$$\text{Ar } (\Delta LMN)/\text{Ar } (\Delta MNR) = LN/NR = 3/7$$

(iii) As ΔLQM and ΔLQN have common vertex at L and their bases QM and QN are along the same straight line.

$$\text{Area of } \Delta LQM/\text{Area of } \Delta LQN = QM/QN = 10/7$$

$$[\text{Since, } MN/QN = 3/7 \Rightarrow QM/QN = 10/7]$$

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Exercise 15(D)

1. A triangle ABC has been enlarged by scale factor $m = 2.5$ to the triangle $A' B' C'$
Calculate:

(i) the length of AB, if $A' B' = 6$ cm.

(ii) the length of $C' A'$ if $CA = 4$ cm.

Solution:

Given that, ΔABC has been enlarged by scale factor m of 2.5 to $\Delta A'B'C'$.

(i) $A'B' = 6 \text{ cm}$

So,

$$AB(2.5) = A'B' = 6 \text{ cm}$$

$$AB = 2.4 \text{ cm}$$

(ii) $CA = 4 \text{ cm}$

We know that,

$$CA(2.5) = C'A'$$

$$C'A' = 4 \times 2.5 = 10 \text{ cm}$$

2. A triangle LMN has been reduced by scale factor 0.8 to the triangle L' M' N'. Calculate:

(i) the length of M' N', if MN = 8 cm.

(ii) the length of LM, if L' M' = 5.4 cm.

Solution:

Given, ΔLMN has been reduced by a scale factor $m = 0.8$ to $\Delta L'M'N'$.

(i) $MN = 8 \text{ cm}$

So, $MN (0.8) = M'N'$

$$(8)(0.8) = M'N'$$

$$M'N' = 6.4 \text{ cm}$$

(ii) $L'M' = 5.4 \text{ cm}$

So, $LM (0.8) = L'M'$

$$LM (0.8) = 5.4$$

$$LM = 6.75 \text{ cm}$$

3. A triangle ABC is enlarged, about the point O as centre of enlargement, and the scale factor is 3. Find:

(i) $A'B'$, if $AB = 4$ cm.

(ii) BC , if $B'C' = 15$ cm.

(iii) OA , if $OA' = 6$ cm

(iv) OC' , if $OC = 21$ cm

Also, state the value of:

(a) OB'/OB (b) $C'A'/CA$

Solution:

Given that, ΔABC is enlarged and the scale factor $m = 3$ to the $\Delta A'B'C'$.

(i) $AB = 4$ cm

So, $AB(3) = A'B'$

$(4)(3) = A'B'$

$A'B' = 12$ cm

(ii) $B'C' = 15$ cm

So, $BC(3) = B'C'$

$BC(3) = 15$

$BC = 5$ cm

(iii) $OA' = 6$ cm

So, $OA(3) = OA'$

$OA(3) = 6$

$OA = 2$ cm

(iv) $OC = 21$ cm

So, $OC(3) = OC'$

$21 \times 3 = OC'$

$OC' = 63$ cm

The ratio of the lengths of the two corresponding sides of two triangles.

ΔABC is enlarged and the scale factor $m = 3$ to the $\Delta A'B'C'$

Hence,

(a) $OB'/OB = 3$

(b) $C'A'/CA = 3$

ICSE Class 10 Maths Selina Solutions Chapter 15

Exercise 15(E)

1. In the following figure, XY is parallel to BC , $AX = 9$ cm, $XB = 4.5$ cm and $BC = 18$ cm.

Find:

(i) AY/YC (ii) YC/AC (iii) XY

Solution:

Given, $XY \parallel BC$.

So, In ΔAXY and ΔABC

$$\angle AXY = \angle ABC \text{ [Corresponding angles]}$$

$$\angle AYX = \angle ACB \text{ [Corresponding angles]}$$

Hence, $\Delta AXY \sim \Delta ABC$ by AA criterion for similarity.

As corresponding sides of similar triangles are proportional, we have

(i) $AX/AB = AY/AC$

$$9/13.5 = AY/AC$$

$$AY/YC = 9 / 4.5$$

$$AY/YC = 2$$

$$AY/YC = 2/1$$

(ii) We have,

$$AX/AB = AY/AC$$

$$9/13.5 = AY/AC$$

$$YC/AC = 4.5/13.5 = 1/3$$

(iii) As, $\triangle AXY \sim \triangle ABC$

$$AX/AB = XY/BC$$

$$9/13.5 = XY/18$$

$$XY = (9 \times 18) / 13.5 = 12 \text{ cm}$$

2. In the following figure, ABCD to a trapezium with $AB \parallel DC$. If $AB = 9 \text{ cm}$, $DC = 18 \text{ cm}$, $CF = 13.5 \text{ cm}$, $AP = 6 \text{ cm}$ and $BE = 15 \text{ cm}$,

Calculate:

(i) EC (ii) AF (iii) PE

Solution:

(i) In $\triangle AEB$ and $\triangle FEC$,

$$\angle AEB = \angle FEC \text{ [Vertically opposite angles]}$$

$$\angle BAE = \angle CFE \text{ [Since, } AB \parallel DC \text{]}$$

Hence, $\triangle AEB \sim \triangle FEC$ by AA criterion for similarity.

So, we have

$$AE/FE = BE/EC = AB/FC$$

$$15/EC = 9/13.5$$

$$EC = 22.5 \text{ cm}$$

(ii) In $\triangle APB$ and $\triangle FPD$,

$$\angle APB = \angle FPD \text{ [Vertically opposite angles]}$$

$$\angle BAP = \angle DFP \text{ [Since, } AB \parallel DF \text{]}$$

Hence, $\triangle APB \sim \triangle FPD$ by AA criterion for similarity.

So, we have

$$AP/FP = AB/FD$$

$$6/FP = 9/31.5$$

$$FP = 21 \text{ cm}$$

$$\text{So, } AF = AP + PF = 6 + 21 = 27 \text{ cm}$$

(iii) We already have, $\triangle AEB \sim \triangle FEC$

So,

$$AE/FE = BE/CE = AB/FC$$

$$AE/FE = 9/13.5$$

$$(AF - EF)/FE = 9/13.5$$

$$AF/EF - 1 = 9/13.5$$

$$27/EF = 9/13.5 + 1 = 22.5/13.5$$

$$EF = (27 \times 13.5)/22.5 = 16.2 \text{ cm}$$

$$\text{Now, } PE = PF - EF = 21 - 16.2 = 4.8 \text{ cm}$$

3. In the following figure, AB, CD and EF are perpendicular to the straight line BDF.

If AB = x and; CD = z unit and EF = y unit, prove that:

$$1/x + 1/y = 1/z$$

Solution:

In $\triangle FDC$ and $\triangle FBA$,

$$\angle FDC = \angle FBA \text{ [As } DC \parallel AB]$$

$$\angle DFC = \angle BFA \text{ [common angle]}$$

Hence, $\triangle FDC \sim \triangle FBA$ by AA criterion for similarity.

So, we have

$$DC/AB = DF/BF$$

$$z/x = DF/BF \dots (1)$$

In $\triangle BDC$ and $\triangle BFE$,

$$\angle BDC = \angle BFE \text{ [As } DC \parallel FE]$$

$$\angle DBC = \angle FBE \text{ [Common angle]}$$

Hence, $\triangle BDC \sim \triangle BFE$ by AA criterion for similarity.

So, we have

$$BD/BF = z/y \dots (2)$$

Now, adding (1) and (2), we get

$$BD/BF + DF/BF = z/y + z/x$$

$$1 = z/y + z/x$$

Thus,

$$1/z = 1/x + 1/y$$

– Hence Proved

4. Triangle ABC is similar to triangle PQR. If AD and PM are corresponding medians of the two triangles, prove that: $AB/PQ = AD/PM$.

Solution:

Given, $\triangle ABC \sim \triangle PQR$

AD and PM are the medians, so $BD = DC$ and $QM = MR$

So, we have

$$AB/PQ = BC/QR \text{ [Corresponding sides of similar triangles are proportional.]}$$

Then,

$$AB/PQ = (BC/2)/(QR/2) = BD/QM$$

$$\text{And, } \angle ABC = \angle PQR \text{ i.e. } \angle ABD = \angle PQM$$

Hence, $\triangle ABD \sim \triangle PQM$ by SAS criterion for similarity.

Thus,

$$AB/PQ = AD/PM.$$

5. Triangle ABC is similar to triangle PQR. If AD and PM are altitudes of the two triangles, prove that: $AB/PQ = AD/PM$.

Solution:

Given, $\triangle ABC \sim \triangle PQR$

So,

$$\angle ABC = \angle PQR \text{ i.e. } \angle ABD = \angle PQM$$

Also, $\angle ADB = \angle PMQ$ [Both are right angles]

Hence, $\triangle ABD \sim \triangle PQM$ by AA criterion for similarity.

Thus,

$$AB/PQ = AD/PM$$

6. Triangle ABC is similar to triangle PQR. If bisector of angle BAC meets BC at point D and bisector of angle QPR meets QR at point M, prove that: $AB/PQ = AD/PM$

Solution:

Given, $\triangle ABC \sim \triangle PQR$

And, AD and PM are the angle bisectors.

So,

$$\angle BAD = \angle QPM$$

Also, $\angle ABC = \angle PQR$ i.e. $\angle ABD = \angle PQM$

Hence, $\triangle ABD \sim \triangle PQM$ by AA criterion for similarity.

Thus,

$$AB/PQ = AD/PM$$

7. In the following figure, $\angle AXY = \angle AYX$. If $BX/AX = CY/AY$, show that triangle ABC is isosceles.

Solution:

Given,

$$\angle AXY = \angle AYX$$

So, $AX = AY$ [Sides opposite to equal angles are equal.]

Also, from BPT we have

$$BX/AX = CY/AY$$

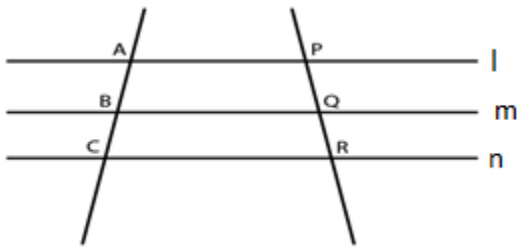
Thus,

$$AX + BX = AY + CY$$

So, $AB = AC$

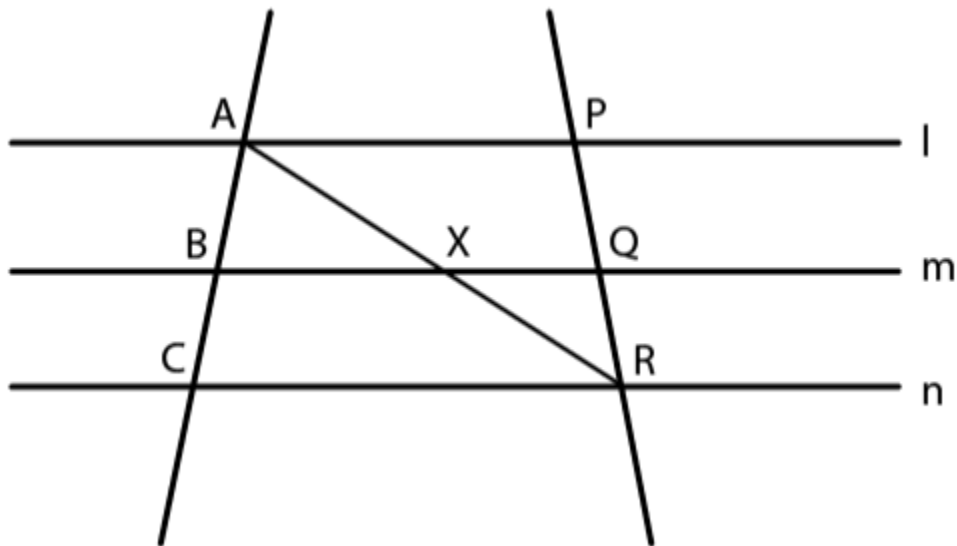
Therefore, $\triangle ABC$ is an isosceles triangle.

8. In the following diagram, lines l , m and n are parallel to each other. Two transversals p and q intersect the parallel lines at points A , B , C and P , Q , R as shown.



Prove that: $AB/BC = PQ/QR$

Solution:



Let join AR such that it intersects BQ at point X .

In $\triangle ACR$, $BX \parallel CR$. By BPT, we have

$$AB/BC = AX/XR \dots (1)$$

In $\triangle APR$, $XQ \parallel AP$. By BPT, we have

$$PQ/QR = AX/XR \dots (2)$$

From (1) and (2),

$$AB/BC = PQ/QR$$

– Hence Proved

9. In the following figure, $DE \parallel AC$ and $DC \parallel AP$. Prove that: $BE/EC = BC/CP$.

Solution:

Given, $DE \parallel AC$

So,

$$BE/EC = BD/DA \text{ [By BPT]}$$

And, $DC \parallel AP$

So,

$$BC/CP = BD/DA \text{ [By BPT]}$$

Therefore,

$$BE/EC = BC/CP$$

10. In the figure given below, $AB \parallel EF \parallel CD$. If $AB = 22.5$ cm, $EP = 7.5$ cm, $PC = 15$ cm and $DC = 27$ cm.

Calculate: (i) EF (ii) AC

Solution:

(i) In $\triangle PCD$ and $\triangle PEF$,

$$\angle CPD = \angle EPF \text{ [Vertically opposite angles]}$$

$$\angle DCE = \angle FEP \text{ [As } DC \parallel EF, \text{ alternate angles.]}$$

Hence, $\triangle PCD \sim \triangle PEF$ by AA criterion for similarity.

So, we have

$$27/EF = 15/7.5$$

Thus,

$$EF = 13.5$$

(ii) And, as $EF \parallel AB$

$\triangle CEF \sim \triangle CAB$ by AA criterion for similarity.

$$EC/AC = EF/AB$$

$$22.5/AC = 13.5/22.5$$

Thus, $AC = 37.5$ cm

11. In $\triangle ABC$, $\angle ABC = \angle DAC$, $AB = 8$ cm, $AC = 4$ cm and $AD = 5$ cm.

(i) Prove that $\triangle ACD$ is similar to $\triangle BCA$.

(ii) Find BC and CD

(iii) Find the area of $\triangle ACD$: area of $\triangle ABC$

Solution:

(i) In $\triangle ACD$ and $\triangle BCA$,

$$\angle DAC = \angle ABC \text{ [Given]}$$

$$\angle ACD = \angle BCA \text{ [Common angles]}$$

Hence, $\triangle ACD \sim \triangle BCA$ by AA criterion for similarity.

(ii) Since, $\triangle ACD \sim \triangle BCA$

We have,

$$AC/BC = CD/CA = AD/AB$$

$$4/BC = CD/4 = 5/8$$

$$4/BC = 5/8$$

$$\text{So, } BC = 32/5 = 6.4 \text{ cm}$$

And,

$$CD/4 = 5/8$$

$$\text{Thus, } CD = 20/8 = 2.5 \text{ cm}$$

(iii) As, $\triangle ACD \sim \triangle BCA$

We have,

$$\text{Ar}(\triangle ACD) / \text{Ar}(\triangle BCA) = AD^2 / AB^2 = 5^2 / 8^2$$

$$\text{Ar}(\triangle ACD) / \text{Ar}(\triangle BCA) = 25/64$$

12. In the given triangle P, Q and R are mid-points of sides AB, BC and AC respectively. Prove that triangle QRP is similar to triangle ABC.

Solution:

In $\triangle ABC$, as $PR \parallel BC$ by BPT we have

$$AP/PB = AR/RC$$

And, in $\triangle PAR$ and $\triangle BAC$,

$$\angle PAR = \angle BAC \text{ [Common]}$$

$$\angle APR = \angle ABC \text{ [Corresponding angles]}$$

Hence, $\triangle PAR \sim \triangle BAC$ by AA criterion for similarity

So, we have

$$PR/BC = AP/AB$$

$$PR/BC = \frac{1}{2} \text{ [Since, P is the mid-point of AB]}$$

$$PR = \frac{1}{2} BC$$

Similarly,

$$PQ = \frac{1}{2} AC$$

$$RQ = \frac{1}{2} AB$$

So,

$$PR/BC = PQ/AC = RQ/AB$$

Therefore,

$\triangle QRP \sim \triangle ABC$ by SSS similarity.

13. In the following figure, AD and CE are medians of $\triangle ABC$. DF is drawn parallel to CE. Prove that:

(i) $EF = FB$,

(ii) $AG:GD = 2:1$

Solution:

(i) In $\triangle BFD$ and $\triangle BEC$,

$\angle BFD = \angle BEC$ [Corresponding angles]

$\angle FBD = \angle EBC$ [Common]

Hence, $\triangle BFD \sim \triangle BEC$ by AA criterion for similarity.

So,

$$BF/BE = BD/BC$$

$$BF/BE = \frac{1}{2} \text{ [Since, D is the mid-point of BC]}$$

$$BE = 2BF$$

$$BF = FE = 2BF$$

Thus,

$$EF = FB$$

(ii) In $\triangle AFD$, $EG \parallel FD$ and using BPT we have

$$AE/EF = AG/GD \dots (1)$$

Now, $AE = EB$ [Since, E is the mid-point of AB]

$$AE = 2EF \text{ [As, } EF = FB, \text{ by (1)]}$$

So, from (1) we have

$$AG/GD = 2/1$$

Therefore, $AG:GD = 2:1$

14. Two similar triangles are equal in area. Prove that the triangles are congruent.

Solution:

Let's consider two similar triangles as $\triangle ABC \sim \triangle PQR$

So,

$$\text{Ar}(\triangle ABC) / \text{Ar}(\triangle PQR) = (AB/PQ)^2 = (BC/QR)^2 = (AC/PR)^2$$

Since,

Area of $\triangle ABC$ = Area of $\triangle PQR$ [Given]

Hence,

$$AB = PQ$$

$$BC = QR$$

$$AC = PR$$

So, as the respective sides of two similar triangles are all of same length.

We can conclude that,

$$\triangle ABC \cong \triangle PQR \text{ [By SSS rule]}$$

– Hence Proved

15. The ratio between the altitudes of two similar triangles is 3: 5; write the ratio between their:

(i) medians. (ii) perimeters. (iii) areas.

Solution:

The ratio between the altitudes of two similar triangles is same as the ratio between their sides.

So,

(i) The ratio between the medians of two similar triangles is same as the ratio between their sides.

Thus, the required ratio = 3: 5

(ii) The ratio between the perimeters of two similar triangles is same as the ratio between their sides.

Thus, the required ratio = 3: 5

(iii) The ratio between the areas of two similar triangles is same as the square of the ratio between their corresponding sides.

Thus, the required ratio = $(3)^2: (5)^2 = 9: 25$

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