



PRACHAND NEET



ONE SHOT



PHYSICS

Alternating Currents

TANUJ BANSAL SIR (TBS)



Topics *to be covered*

- 1 Average and RMS Current
- 2 LCR Series Circuit
- 3 Resonance, Quality Factor
- 4 Transformer

चलिए शुरू करते हैं



TBS Army – Tanuj Sir

TANUJ SIR

JOIN MY OFFICIAL TELEGRAM CHANNEL

Physics Wallah



PRACHAND SERIES

TELEGRAM CHANNEL



@PW_YAKEENDROPPER



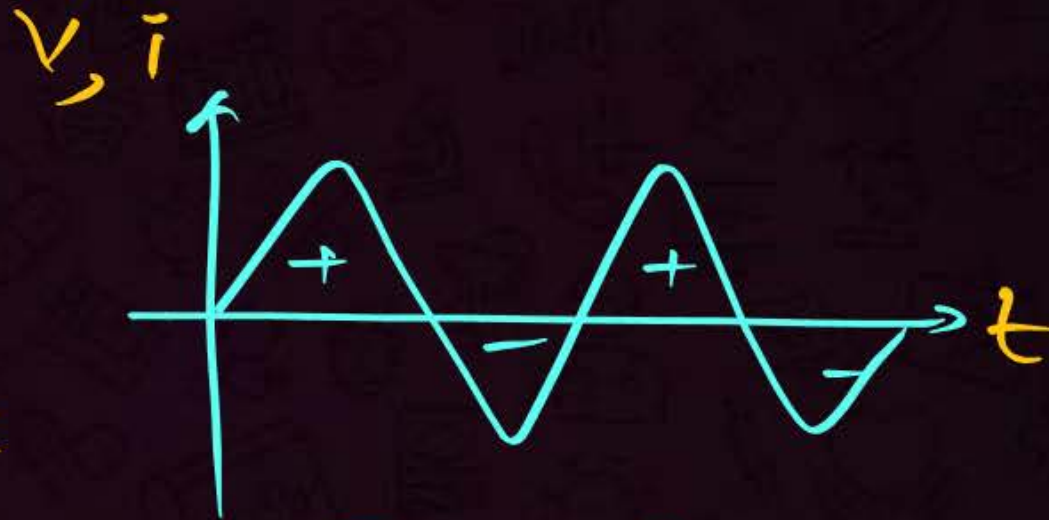
Alternating Current (AC)



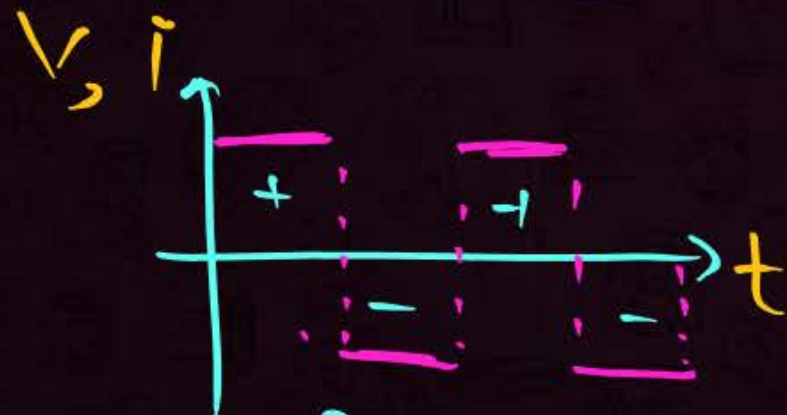
The current which changes its direction after a regular interval of time is called alternating current.



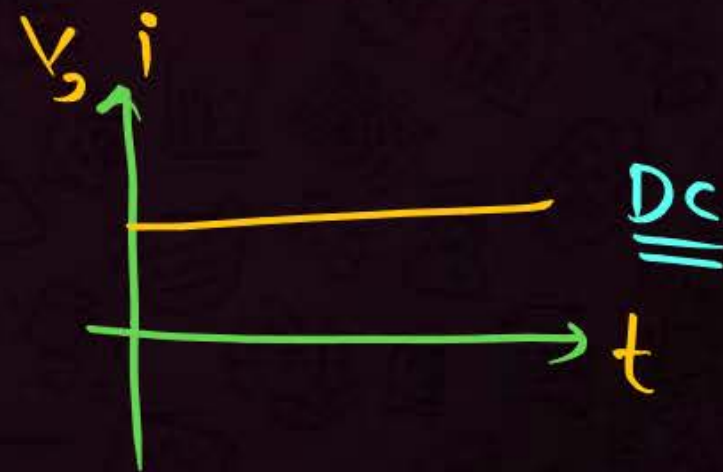
Sinusoidal AC



Triangular Wave AC



Square wave AC



DC



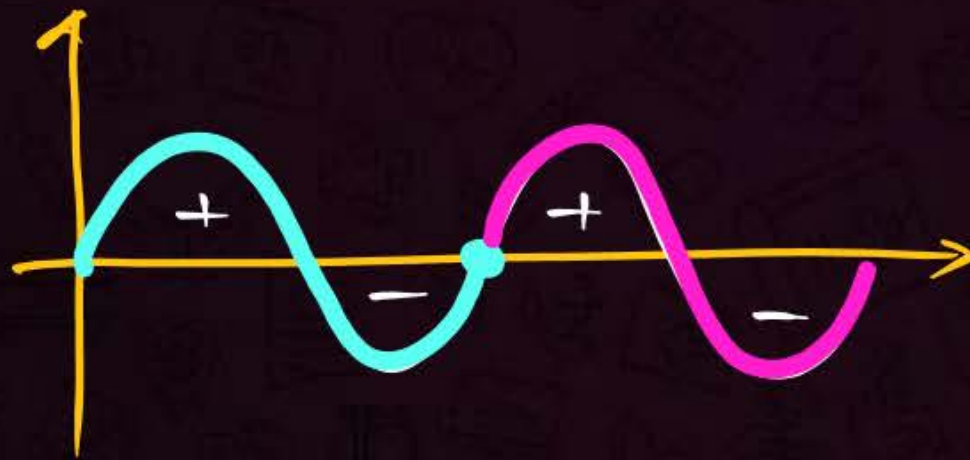
DC



Home Supply of Alternating Current



→ AC Generator
→ Sinusoidal AC



India $\rightarrow 50 \text{ Hz} = f$

USA $\rightarrow 60 \text{ Hz} = f$

Ques Home supply $\omega = ?$

$$\omega = 2\pi f = 2\pi \times 50 \\ = 100\pi \text{ rad/sec}$$

Ques Time period $T = ?$

$$T = \frac{1}{f} = \frac{1}{50} \text{ sec} = \frac{2}{100} \text{ sec} \\ = 0.02 \text{ sec.}$$

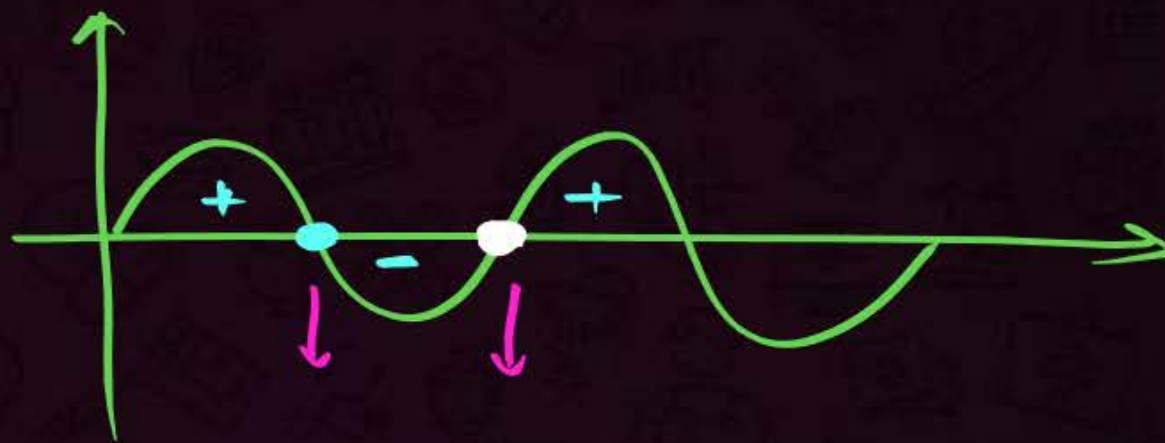
How many times in Indian home supply, the current changes its direction in 1 second?

A) 2

B) 50

C) 1

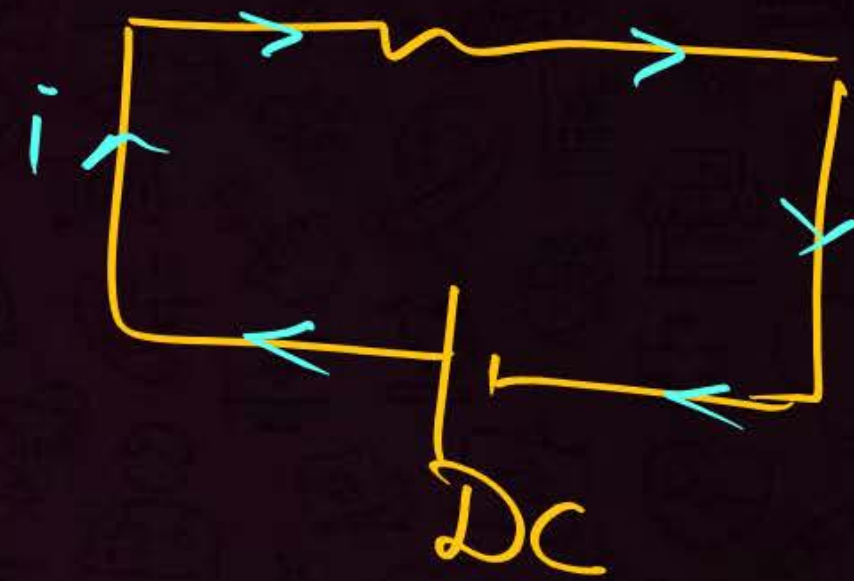
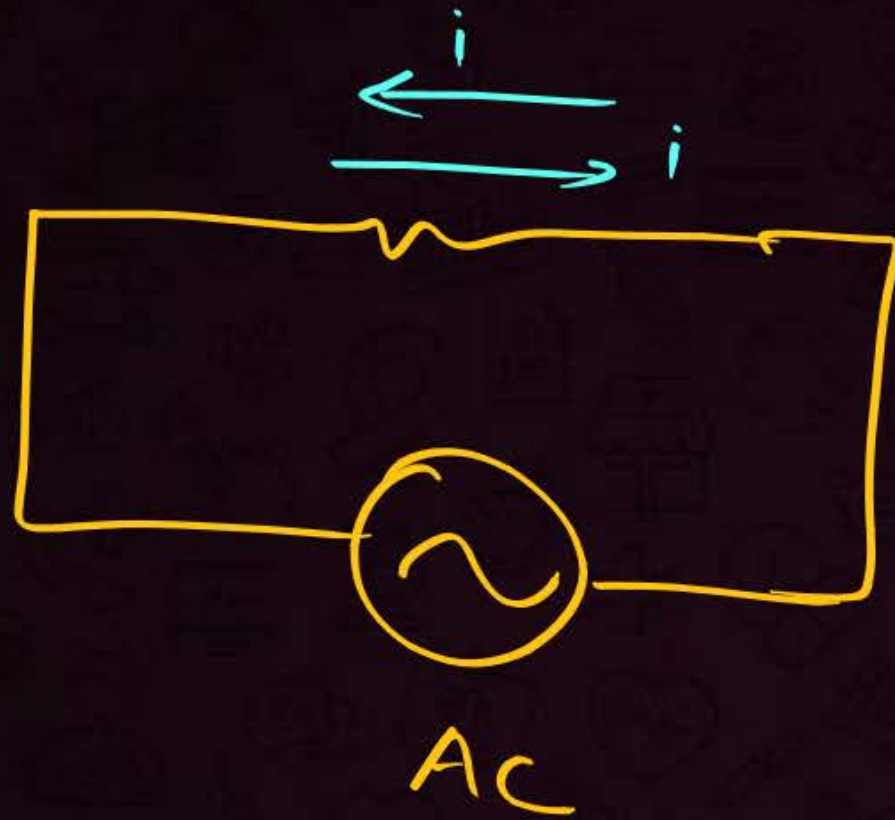
D) 100



1 cycle \rightarrow 2 change

50 cycle \Rightarrow 100 change

Feel of AC:



QUESTION



The current flowing through an ac circuit is given by $I = 5\sin(120\pi t)$ A How long will the current take to reach the peak value starting from zero? [27 June, 2022 (S-I)]

(JEE Mains)

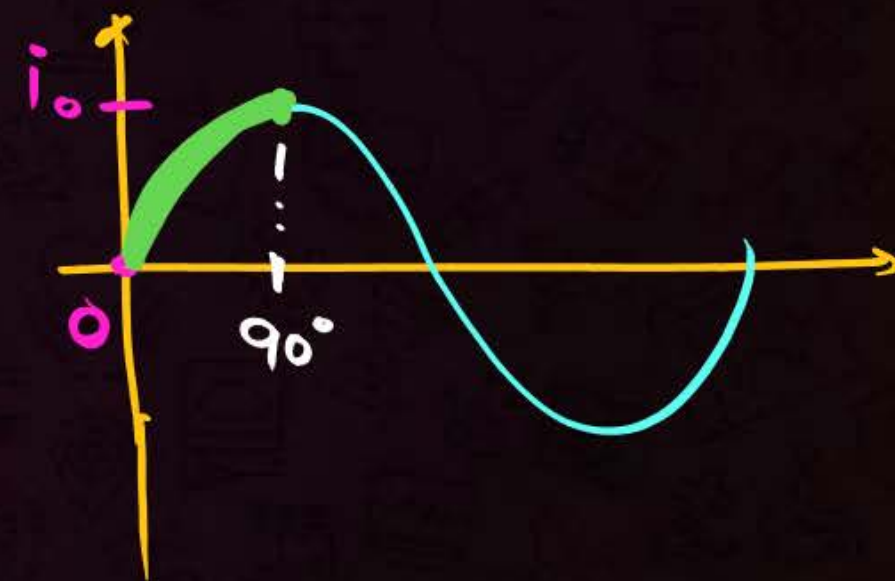
- 1 $1/60$ s
- 2 60 s
- 3 $1/120$ s
- 4 $1/240$ s

$$i = i_0 \sin \omega t$$

time t max/peak value

Put $i = i_0$

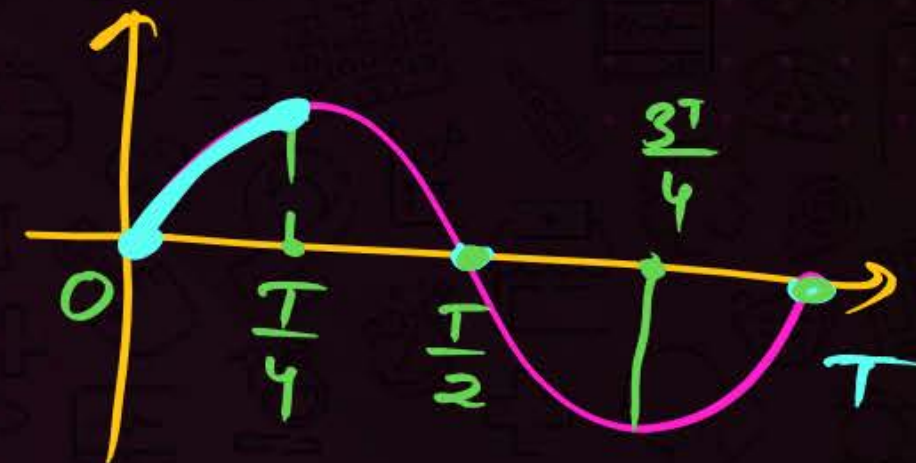
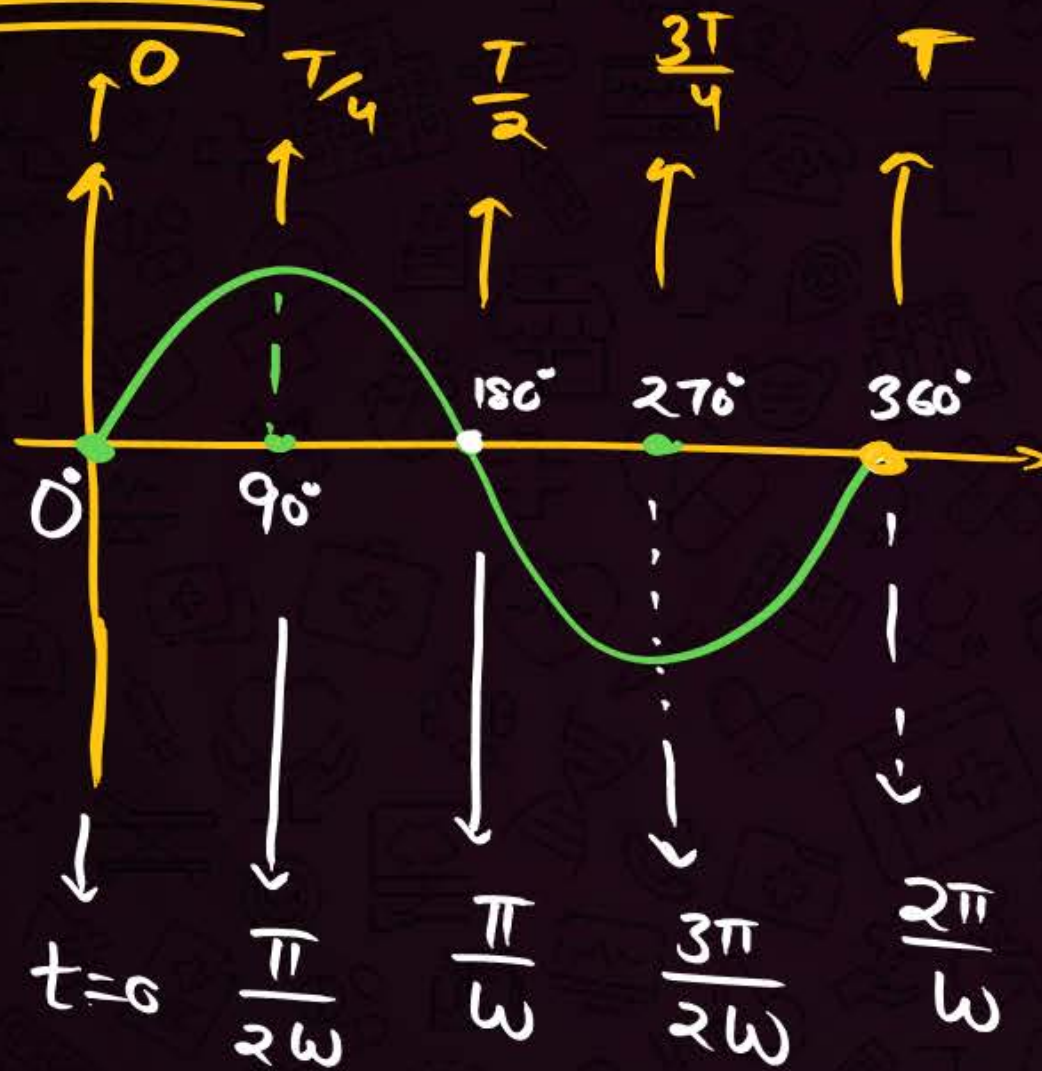
$$i_0 = i_0 \sin \omega t$$



$$\sin \omega t = 1$$
$$\omega t = \frac{\pi}{2}$$
$$t = \frac{\pi}{2\omega} = \frac{\pi}{2 \times 120\pi} = \frac{1}{240} \text{ sec.}$$

SHM
Waves
Wave Optics
AC

TBS Feel



Ques Time period of AC \Rightarrow 2 sec

Find time taken to reach max value from zero.

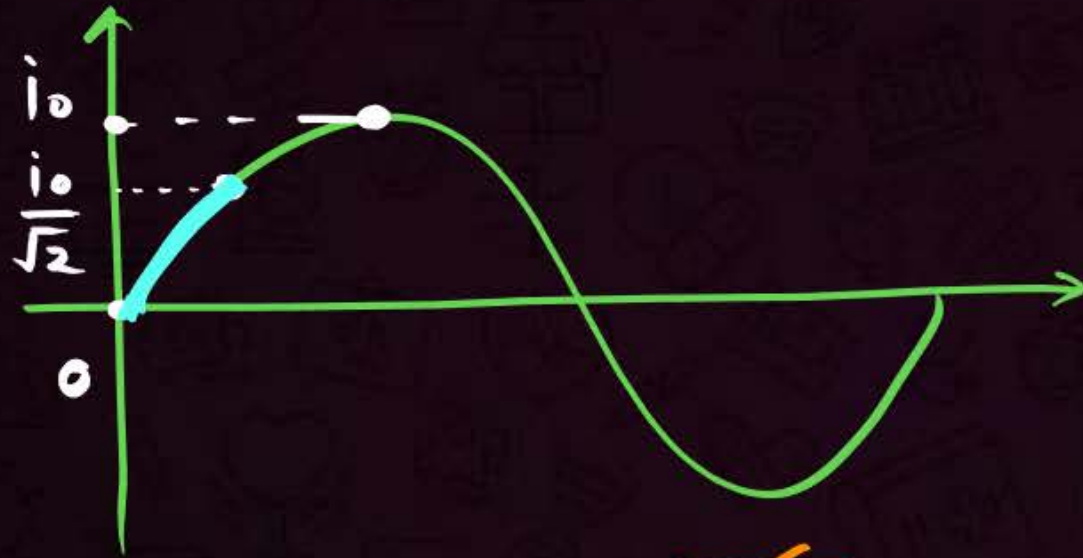
$$\rightarrow \frac{T}{4} = \frac{2}{4} = \frac{1}{2} = 0.5 \text{ sec}$$

QUESTION



$$\rightarrow T = \frac{1}{50}$$

The time required for the 50 Hz sinusoidal source alternating current to reach its rms value from zero is



Normal 2 inday

$$i = i_0 \sin \omega t$$

$$\frac{i_0}{\sqrt{2}} = i_0 \sin \omega t$$

$$\sin \omega t = \frac{1}{\sqrt{2}}$$

$$\omega t = \frac{\pi}{4}$$

$$t = \frac{\pi}{4\omega} = \frac{T}{8} = \frac{1}{50 \times 8} = \frac{1}{400} \text{ sec}$$

Age Agea.

$$i_{rms} = \frac{i_0}{\sqrt{2}}$$

$$\rightarrow 45^\circ = \frac{\pi}{4}$$

$$T = \frac{2\pi}{\omega}$$

$$\omega = \frac{2\pi}{T}$$

$$\omega = 2\pi f$$

$$t = \frac{\pi}{4 \times \frac{2\pi}{T}}$$

$$t = \frac{T}{8}$$

TBS Mantos
Zindagi

$$\Rightarrow i_{rms} = \frac{i_0}{\sqrt{2}}$$

$$\frac{1}{\sqrt{2}} \Rightarrow 45^\circ = \frac{\pi}{4}$$

$$t = \frac{\pi}{4\omega} = \frac{1}{8}$$

Ques

Time taken from zero to $\frac{i_0}{2}$.

A) $\frac{\pi}{2\omega}$

B) $\frac{\pi}{4\omega}$

~~C) $\frac{\pi}{6\omega}$~~

D) $\frac{\pi}{3\omega}$

$$\sin \theta = \frac{1}{2}$$

$$\theta = 30^\circ = \frac{\pi}{6}$$

$$t = \frac{\pi}{6\omega}$$

$$\begin{aligned} & 30 \times \frac{\pi}{180} \\ &= \frac{\pi}{6} \end{aligned}$$

Ques time taken from 0 to $\frac{\sqrt{3}i_0}{2}$

A) $\frac{\pi}{6\omega}$

B) $\frac{\pi}{4\omega}$

C) $\frac{\pi}{2\omega}$

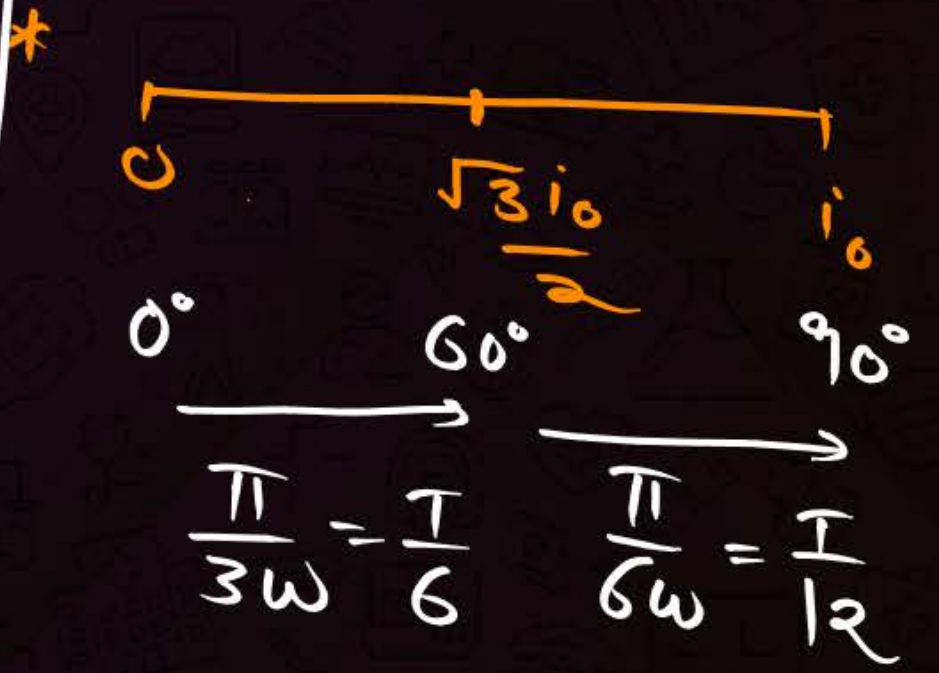
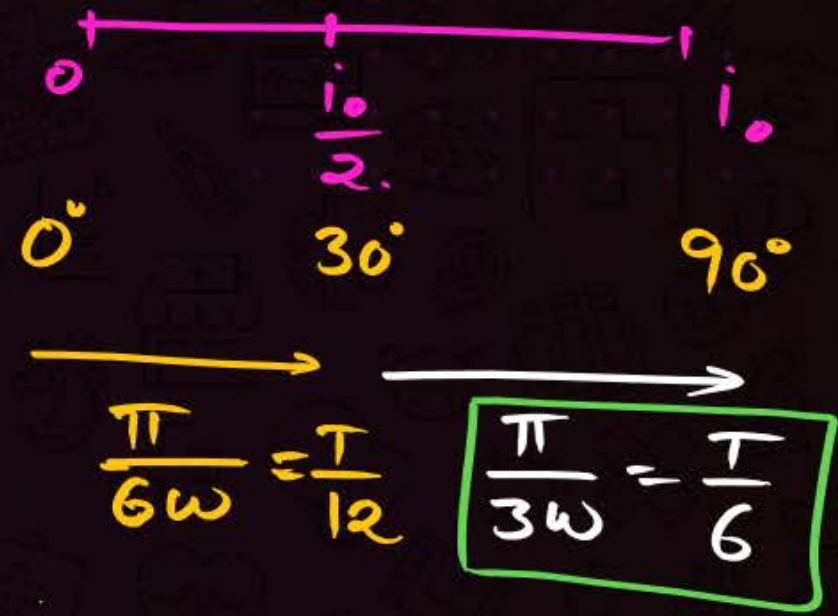
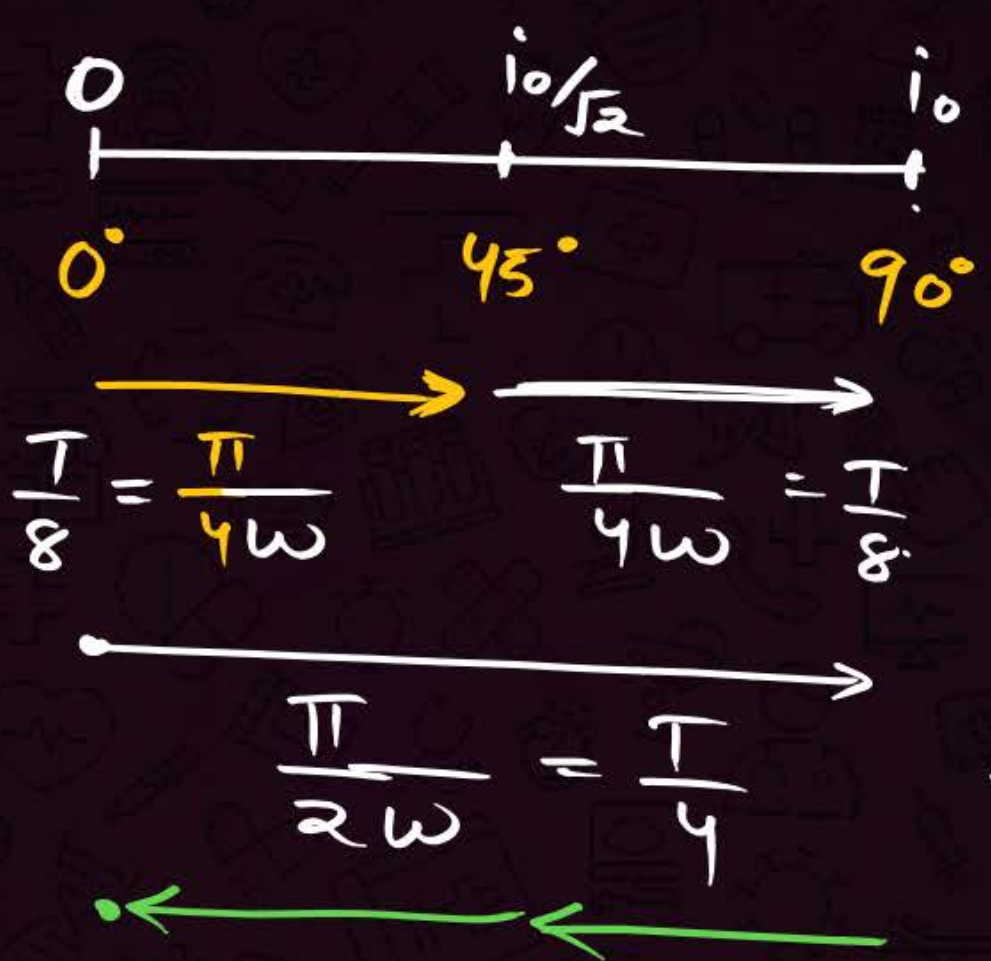
D) None

$$\sin \theta = \frac{\sqrt{3}}{2}$$

$$\theta = 60^\circ = \frac{\pi}{3}$$

$$t = \frac{\pi}{3\omega}$$

TBS Summary



QUESTION



An alternating voltage $v(t) = 220 \sin 100\pi t$ volt is applied to a purely resistive load of $50\ \Omega$. The time taken for the current to rise from half of the peak value to the peak value is:

[8 April, 2019 (S-I)]

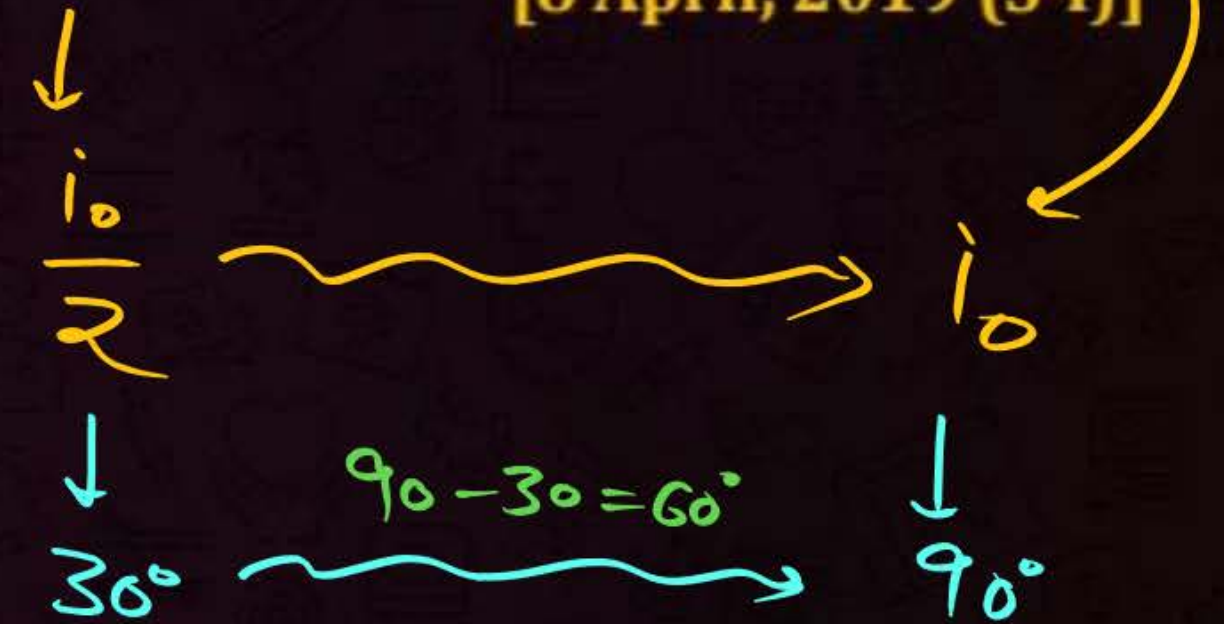
1 2.2 ms

2 5 ms

3 3.3 ms

4 7.2 ms

$$\begin{aligned} \frac{\pi}{3\omega} \\ \frac{\pi}{3 \times 100\pi} &= \frac{1}{300} \text{ sec} \\ &= \frac{1}{300} \times 1000 \\ &= \frac{10}{3} = 3.33 \text{ ms.} \end{aligned}$$

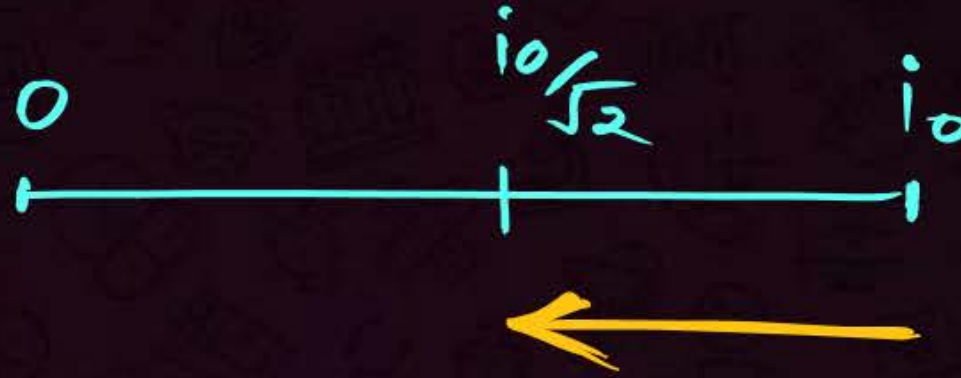


QUESTION



A resistance of $40\ \Omega$ is connected to a source of alternating current rated 220 V, 50 Hz. Find the time taken by the current to change from its maximum value to the rms value:

[24 June, 2022 (S-I)]



$$t = \frac{\pi}{4\omega} = \frac{T}{8} = \frac{1}{8f} = \frac{1}{8 \times 50}$$

$$= \frac{1}{400} \text{ sec} = \frac{1000}{400} = \frac{5}{2} = 2.5 \text{ ms}$$

1 2.5 ms

2 1.25 ms

3 2.5 s

4 0.25 s

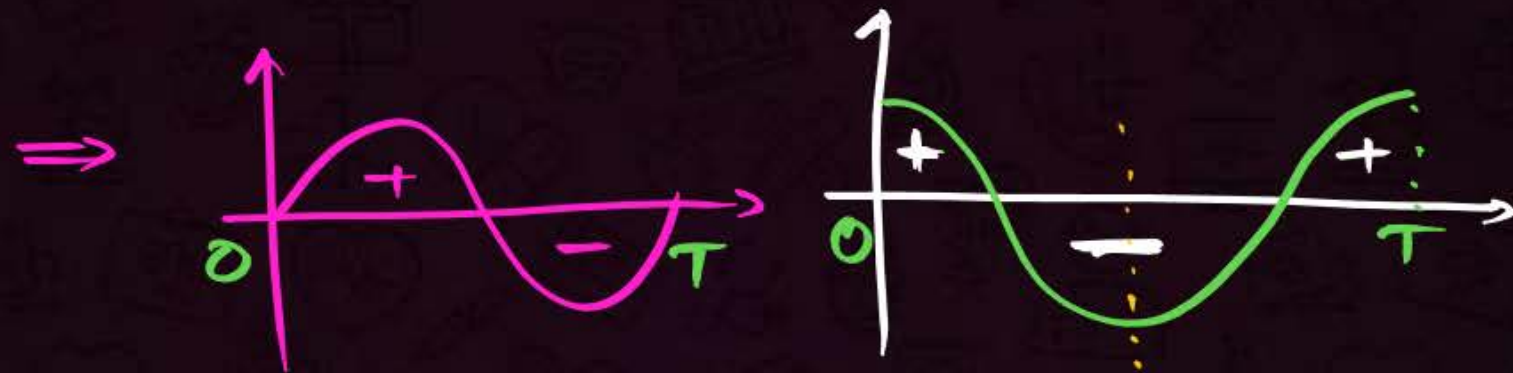


TBS Mathematical Shortcuts



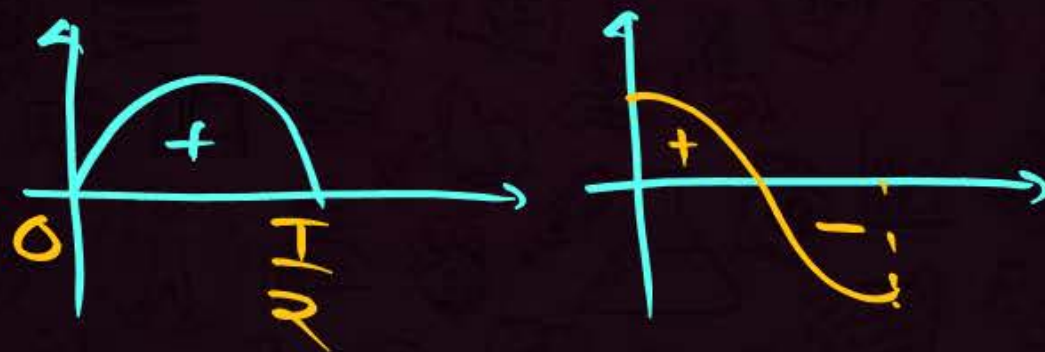
$$i_{av} = \langle i \rangle, \quad V_{av} = \langle V \rangle, \quad P_{av} = \langle P \rangle$$

① Full cycle
(0 to T)



$$\langle \sin \omega t \rangle = \langle \cos \omega t \rangle = \langle \sin 2\omega t \rangle = \langle \cos 2\omega t \rangle = 0$$

② Half cycle
(0 to $\frac{T}{2}$)



$$\langle \sin \omega t \rangle = \frac{2}{\pi}$$
$$\langle \cos \omega t \rangle = 0$$

③ Full cycle

$$\langle \sin^2 \omega t \rangle = \langle \cos^2 \omega t \rangle = \frac{1}{2}$$



Average Current



$$i_{av} = \langle i \rangle = \frac{\text{Total charge flow}}{\text{Total time}}$$

(mean)

② If $i \rightarrow$ variable

eg $\div i = 2t$

$i = i_0 \sin \omega t$

$$q = \int i dt$$

* Total charge

① If $i = \text{const} \Rightarrow q = i \times t$

eg $i = 3A$

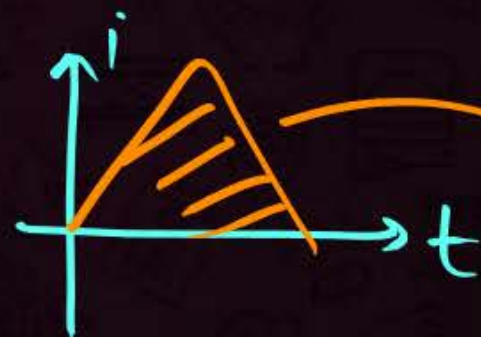
$t = 5$

$$q = i \times t$$

$$= 3 \times 5$$

$$= 15C$$

③ Graph \Rightarrow $i-t$ graph (given)



Area = under
 $i-t$ graph

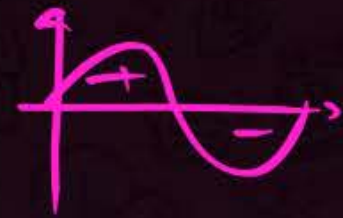
\Downarrow
Total charge
flow.

Average Current in Sinusoidal AC

$$i_{av} = \frac{\int i dt}{\int dt}$$

Here $i = i_0 \sin \omega t$

Full cycle



$$i_{av} = \langle i \rangle = \langle i_0 \sin \omega t \rangle$$

$$= i_0 \langle \sin \omega t \rangle$$

$$i_{av} = i_0 \times 0 = 0 \quad \boxed{i_{av} = 0}$$

Half Cycle
(0 to $\frac{T}{2}$)

\Rightarrow

$$i_{av} = i_0 \langle \sin \omega t \rangle$$

$$\boxed{i_{av} = \frac{2i_0}{\pi} = 0.637 i_0}$$



Root Mean Square Current (rms)

→ virtual or effective current.



Meaning → $i_1, i_2, i_3, \dots, i_n$.

$$i_{rms} = \sqrt{\frac{i_1^2 + i_2^2 + \dots + i_n^2}{n}}$$

$$i_{rms} = \sqrt{\frac{\int i^2 dt}{\int dt}}$$

$$* i = i_0 \sin \omega t$$

$$* i_{rms} = \sqrt{\langle i^2 \rangle}$$

$$* i_{rms} = \sqrt{\langle i_0^2 \sin^2 \omega t \rangle}$$

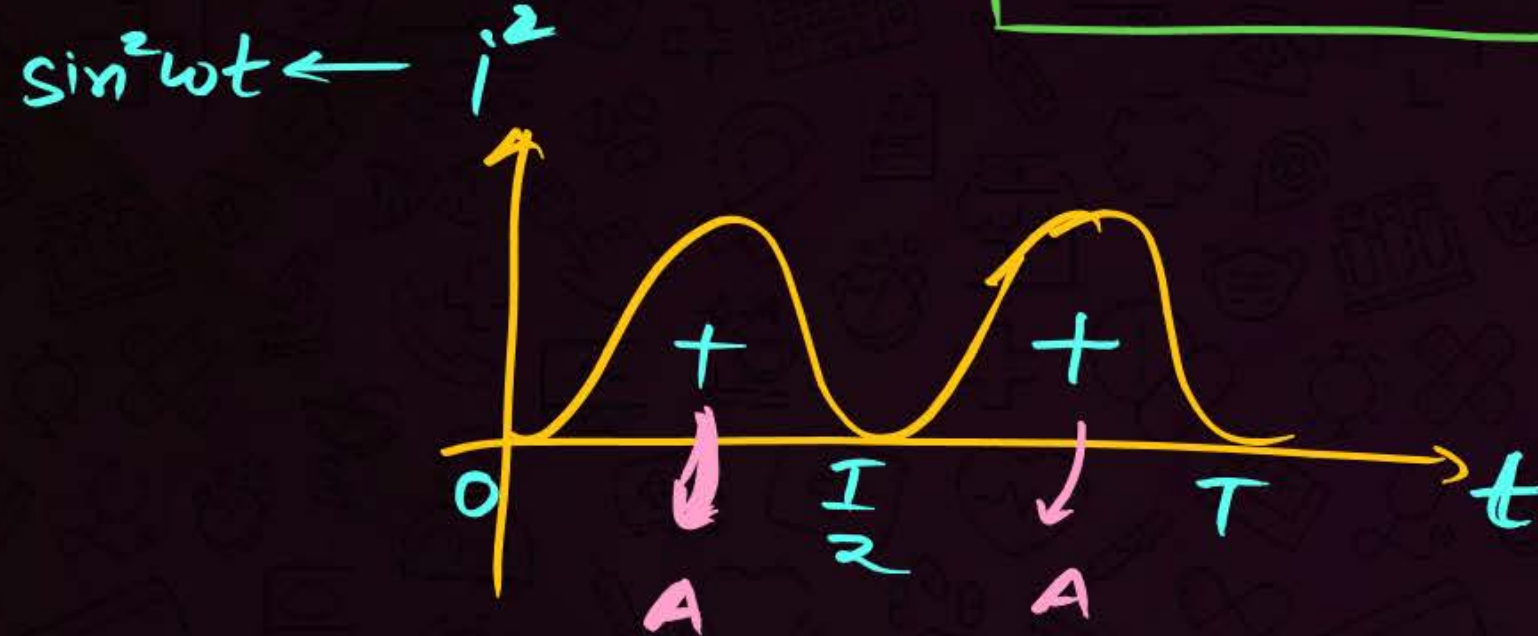
$$i_{rms} = \sqrt{i_0^2 \langle \sin^2 \omega t \rangle}$$

$$i_{rms} = \sqrt{i_0^2 \times \frac{1}{2}} = \boxed{\frac{i_0}{\sqrt{2}} = 0.707 i_0}$$

* Full cycle $\rightarrow i_{rms} = \frac{i_0}{\sqrt{2}}$

Given $i = i_0 \sin \omega t$

i_{rms} in Half cycle
(0 to $\frac{T}{2}$)



Full cycle $\rightarrow \sqrt{\frac{2A}{T}}$

* $V_{rms} = \frac{V_0}{\sqrt{2}}, V_{av} = \frac{2V_0}{\pi}$

Half cycle $\sqrt{\frac{A}{T/2}} = \sqrt{\frac{2A}{T}}$

* TBS Note: If nothing mentioned, then assume rms value

$i_{rms} = \frac{i_0}{\sqrt{2}}$

Home Supply

$$V_{rms} = 220V$$

Ques Peak Value of voltage
in Home supply. (V_0)

$$V_{rms} = \frac{V_0}{\sqrt{2}} = 220$$

$$V_0 = 220\sqrt{2}$$

$$V_0 \approx 311V$$



Form Factor

$$\frac{i_{\text{rms}}}{i_{\text{av}}} = \frac{i_0/\sqrt{2}}{2i_0/\pi} = 1.11$$



TBS Note



- The average value is related to the charge flow.
- The RMS value is related to the heat produced in a circuit.

$$\rightarrow H = i^2 R t \Rightarrow H \propto i^2$$

$$\rightarrow H = \int i^2 R dt$$

More Examples on Average and Rms Values



Ques

$$i = \underbrace{3}_{\text{DC}} + \underbrace{4 \sin \omega t}_{\text{AC}}$$

a) $i_{av} (\text{0 to } T) \Rightarrow \bar{i}_{av} = \langle 3 + 4 \sin \omega t \rangle$

$$= \langle 3 \rangle + \langle 4 \sin \omega t \rangle$$
$$= 3 + 4 \langle \sin \omega t \rangle$$
$$= 3 + 4 \times 0 = 3 + 0 = 3A$$

b) $i_{av} (0 \text{ to } \frac{T}{2}) \rightarrow \bar{i}_{av} = 3 + 4 \times \frac{2}{\pi} = \left(3 + \frac{8}{\pi} \right) A$

ques

$$i = 4 + 3\pi \sin \omega t$$

$$i_{av} \longrightarrow a) 0 \text{ to } T \longrightarrow 4 + 3\pi \times 0 = 4 + 0 = 4A$$

$$b) 0 \text{ to } \frac{T}{2} \Rightarrow 4 + 3\cancel{\pi} \times \frac{2}{\cancel{\pi}} = 4 + 6 = \underline{\underline{10A}}$$

Ques $i = 3 + 4 \sin \omega t$

i_{rms} (0 to T)

$$i_{rms} = \sqrt{\langle i^2 \rangle} = \sqrt{\langle (3 + 4 \sin \omega t)^2 \rangle}$$

$$= \sqrt{\langle 3^2 + 4^2 \sin^2 \omega t + 2 \times 3 \times 4 \sin \omega t \rangle}$$

$$= \sqrt{\langle 9 + 16 \sin^2 \omega t + 24 \sin \omega t \rangle}$$

$$= \sqrt{9 + 16 \times \frac{1}{2} + 24 \times 0} = \sqrt{9 + \frac{16}{2}} = \sqrt{9 + 8} = \sqrt{17} \text{ A}$$

TBS

$$i = a + b \sin \omega t$$

$$i_{rms} = \sqrt{\frac{a^2 + b^2}{2}}$$

ques

$$i = 5 + 4 \sin \omega t$$

$$i_{rms} = ?$$

$$i_{rms} = \sqrt{\frac{5^2 + 4^2}{2}}$$

$$= \sqrt{25 + \frac{16}{2}}$$

$$= \sqrt{25 + 8} = 33 \text{ A}$$

ques
JEE
Main

$$i = \sqrt{42} \sin \omega t + \underline{10}$$

$i_{rms} = ?$

A) 11

b) 10

c) 7

D) None

$$\sqrt{\frac{10^2 + (\sqrt{42})^2}{2}}$$

$$= \sqrt{\frac{100 + 42}{2}}$$

$$= \sqrt{100 + 21}$$

$$= \sqrt{121} = 11$$

QUESTION



An alternating current is given by $I = \underline{I_1 \cos \omega t} + \underline{I_2 \sin \omega t}$. The RMS value of current is given by

1 $\frac{I_1 + I_2}{\sqrt{2}}$

2 $\frac{(I_1 + I_2)^2}{2}$

3 $\sqrt{\frac{I_1^2 + I_2^2}{2}}$

4 $\frac{\sqrt{I_1^2 + I_2^2}}{2}$ ✗

↓
PYQ
↓
NET
↓
JES Mains
(Blunt Base)
↓
JES Advanced

TBS $i = a \sin \omega t + b \cos \omega t$

Ques $i_0 = ?$
→ $\sqrt{a^2 + b^2}$

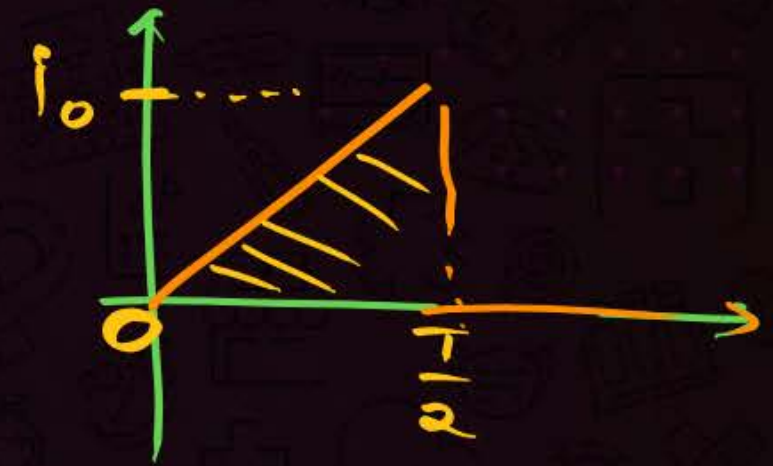
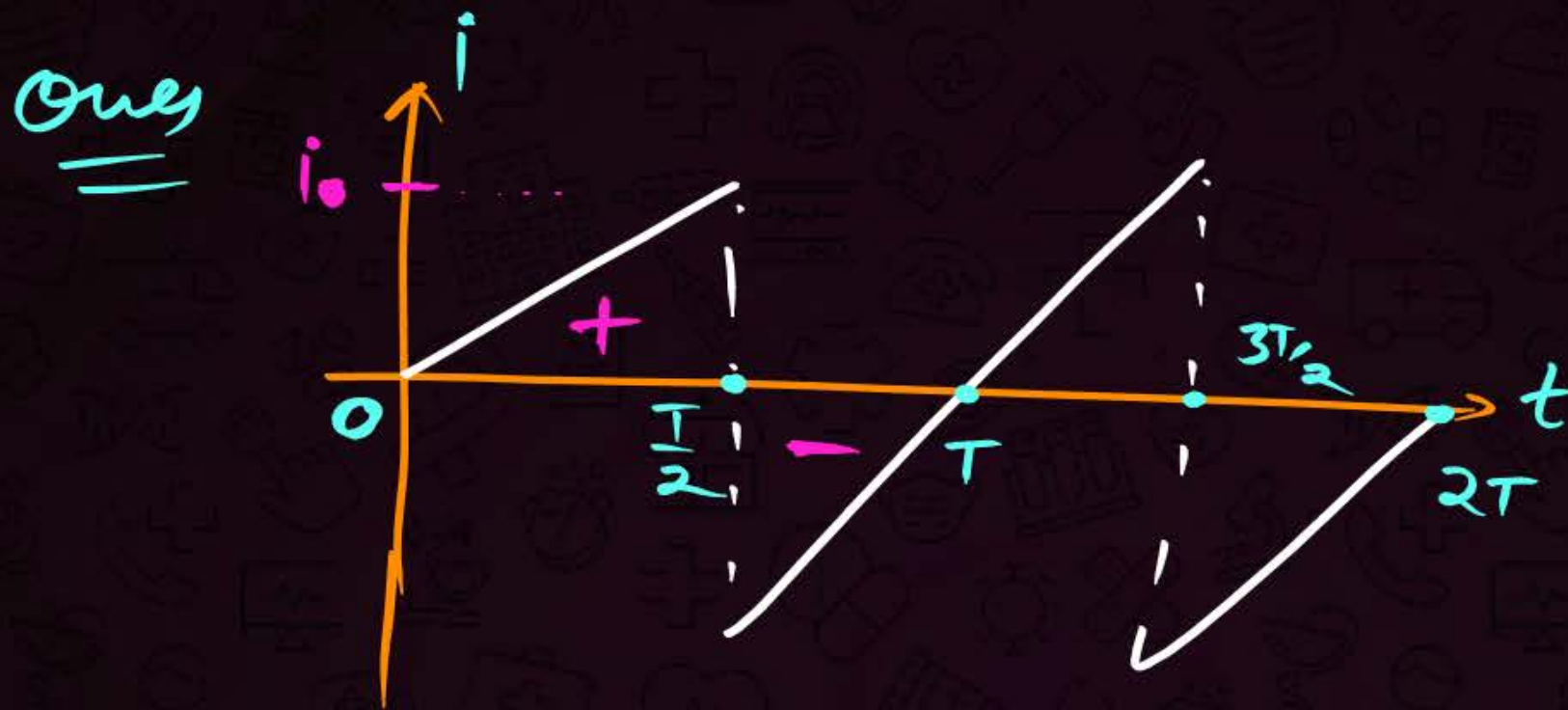
$$i_{rms} = \sqrt{\frac{a^2}{2} + \frac{b^2}{2}} = \sqrt{\frac{a^2 + b^2}{2}}$$

Ques $i = 3 \sin \omega t + 4 \cos \omega t$

$$I_0 = ? \Rightarrow \sqrt{3^2 + 4^2} = 5$$

$$I_{rms} = ? \longrightarrow \frac{5}{\sqrt{2}}$$

SHM \rightarrow Amplitude $\Rightarrow 5$



$$\text{Area} = \frac{1}{2} \times \frac{T}{2} \times i_0$$

$$i_{av} = \frac{\frac{1}{2} \times \frac{T}{2} \times i_0}{\frac{T}{2}} = \frac{i_0}{2}$$

a) $i_{av} (0 \text{ to } T) \rightarrow \text{zero}$

b) $i_{av} (0 \text{ to } T/2)$

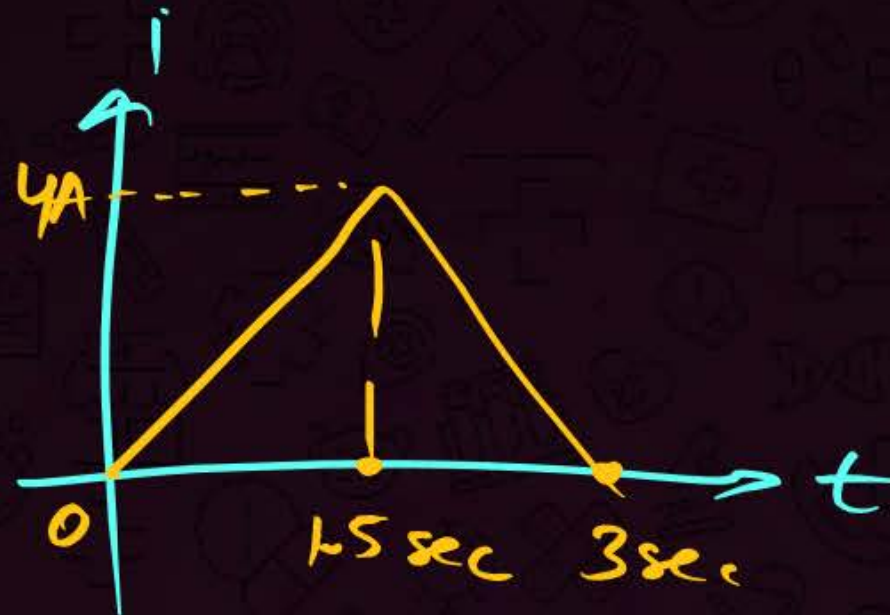
c) $i_{rms} (0 \text{ to } T)$

\downarrow
 $0 \text{ to } T/2$

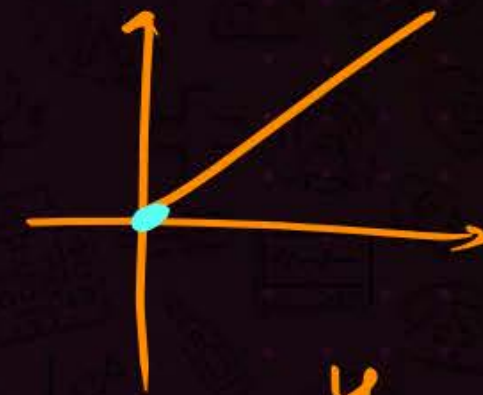
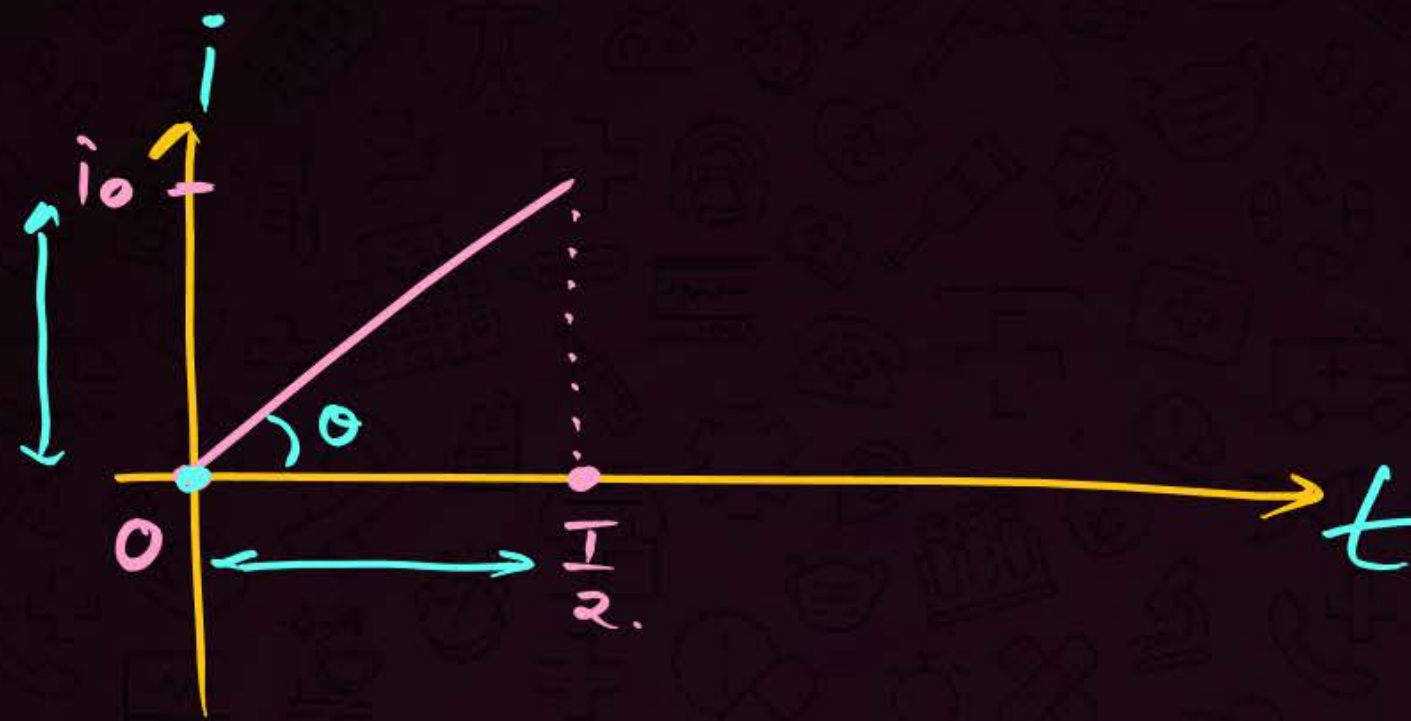
TBS \rightarrow St. line graph

$$i_{av} = \frac{0 + i_0}{2} = \frac{i_0}{2}$$

only



$$i_{av} \Rightarrow \frac{0 + 4}{2} = \boxed{2A} \text{ Ans}$$



$$y = mx$$

$$i = \frac{2i_0}{T} t$$

$$i_{rms} = \sqrt{\frac{\int i^2 dt}{\int dt}} = \sqrt{\frac{\int_0^{T/2} \left(\frac{2i_0}{T} t\right)^2 dt}{\int_0^{T/2} dt}} = \frac{i_0}{\sqrt{3}}$$

$\tan \theta = \frac{i_0}{T/2} = \frac{2i_0}{T}$

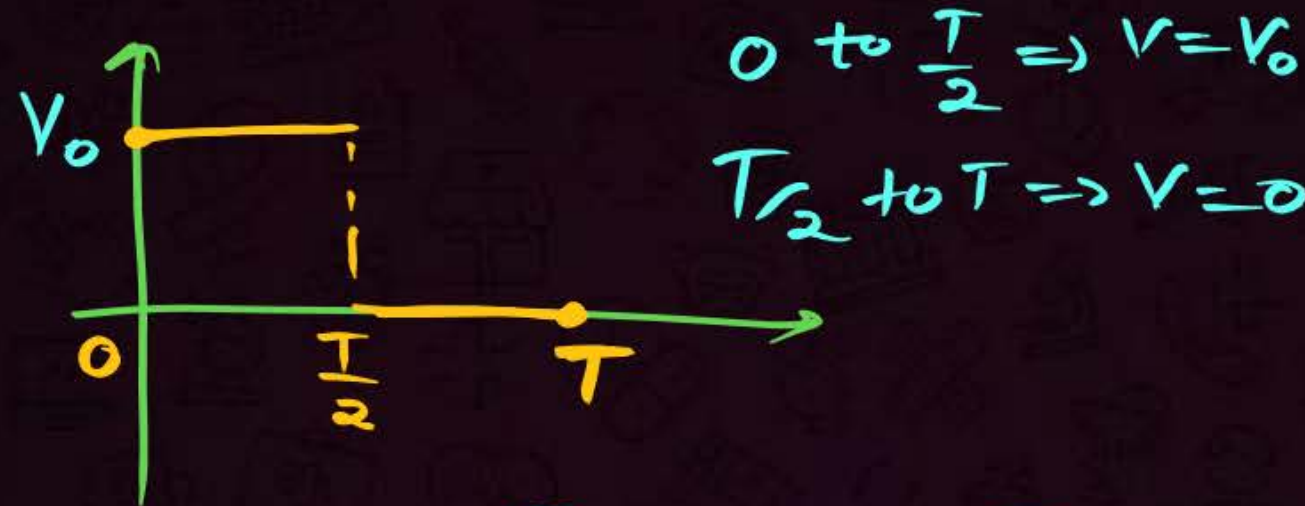
Learn

QUESTION

The r.m.s. value of potential difference V shown in the figure is

(2011)

- 1 $V_0/\sqrt{3}$
- 2 V_0
- 3 $V_0/\sqrt{2}$
- 4 $V_0/2$



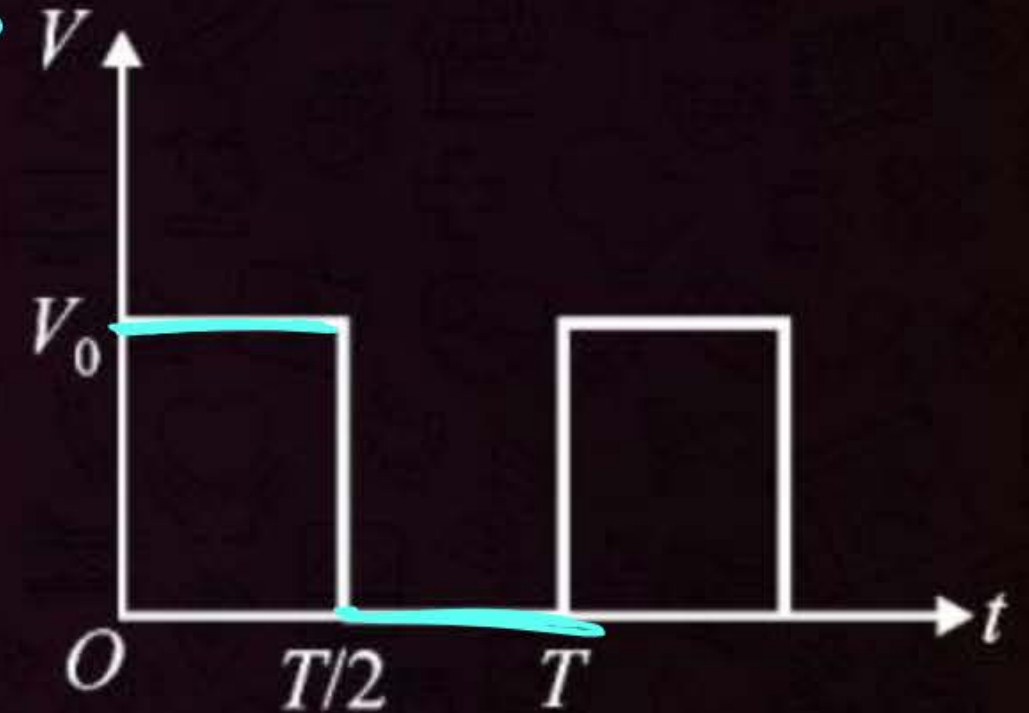
$$0 \text{ to } \frac{T}{2} \Rightarrow V = V_0$$

$$T/2 \text{ to } T \Rightarrow V = 0$$

$$\int V^2 dt = \int_0^{T/2} V_0^2 dt + \int_{T/2}^T 0^2 dt$$

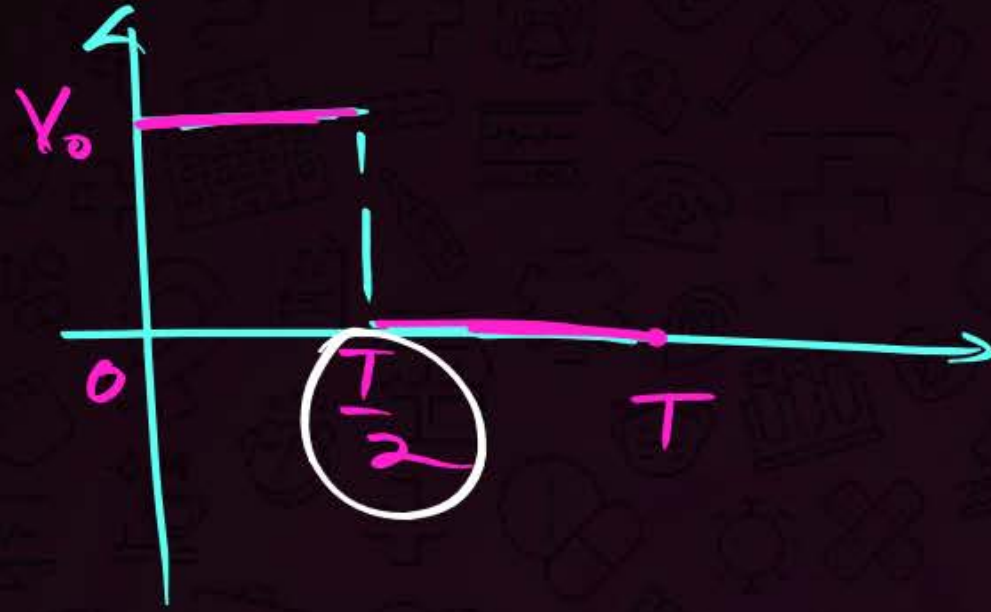
$$= V_0^2 \int_0^{T/2} dt + 0$$

$$= V_0^2 \times [t]_0^{T/2} = V_0^2 \times \frac{T}{2}$$



$$\begin{aligned}
 V_{rms} &= \sqrt{\frac{\int_0^T V^2 dt}{\int_0^T dt}} = \sqrt{\frac{\int_0^{T/2} V_0^2 dt + \int_{T/2}^T 0^2 dt}{\int_0^T dt}} \\
 &= \sqrt{\frac{V_0^2 T/2}{T}} = \sqrt{\frac{V_0^2}{2}} = \frac{V_0}{\sqrt{2}}
 \end{aligned}$$

Soch



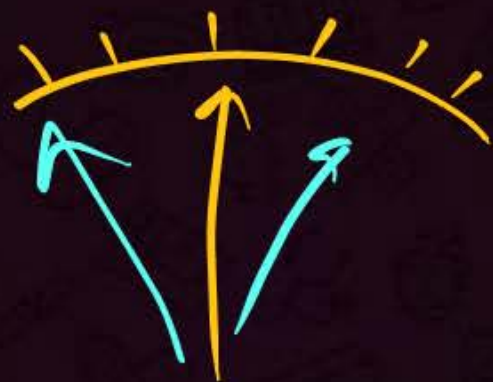
$$V_{rms} = \sqrt{\frac{V_0^2 \times \frac{T}{2}}{T}} = \frac{V_0}{\sqrt{2}}$$



Measurement of AC



AC current \rightarrow Normal Ammeter \rightarrow DC \checkmark
 \rightarrow AC \times



$$\Rightarrow i_{av} = 0$$

\rightarrow due to inertia

AC Ammeter
(Hot wire)

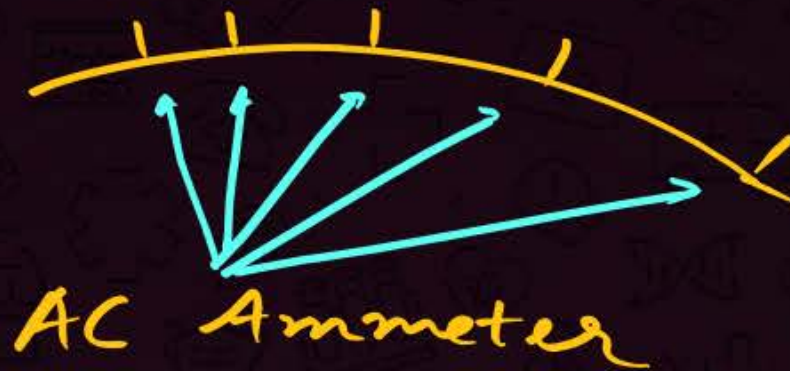


i_{rms} reading \equiv

$$H = \int i^2 R dt \rightarrow \text{always +ve}$$

Assertion
Reason

TBS
Note
=



→ Division gap constant X

→ $H \propto i^2$ ✓

$H \propto i$ X

$$\begin{array}{rcl} 1^2 & = & 1 \\ 2^2 & = & 4 \\ 3^2 & = & 9 \\ 4^2 & = & 16 \\ 5^2 & = & 25 \end{array} \quad \begin{array}{l} \downarrow 3 \\ \downarrow 5 \\ \downarrow 7 \\ \downarrow 9 \end{array}$$

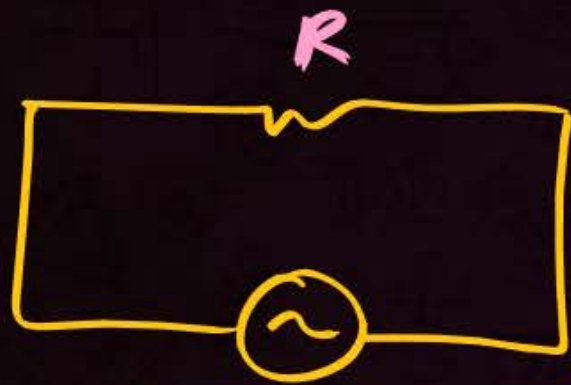
Farak
Constant X



AC Source connected to Resistor



→ Purely Resistive circuit



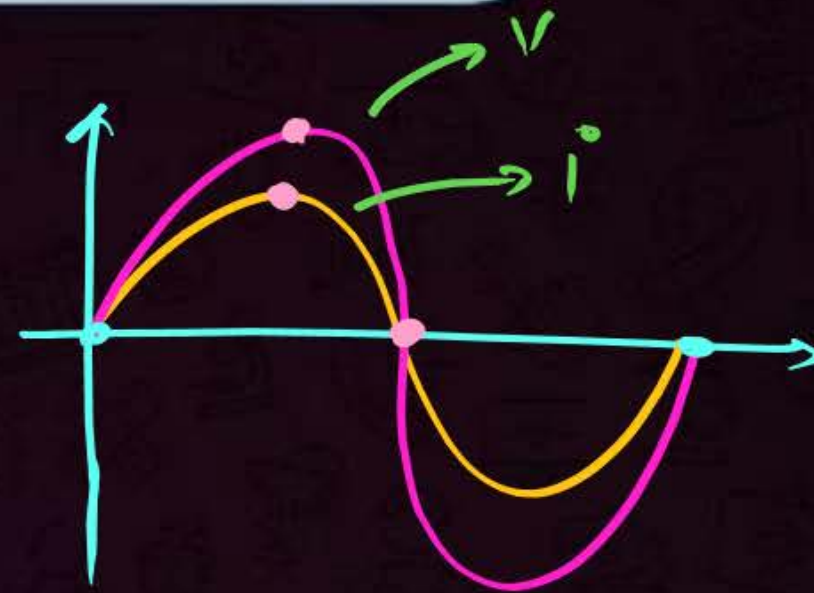
$$V = V_0 \sin \omega t \rightarrow \text{given.}$$

$$i = i_0 \sin \omega t$$

$$i_0 = \frac{V_0}{R}$$

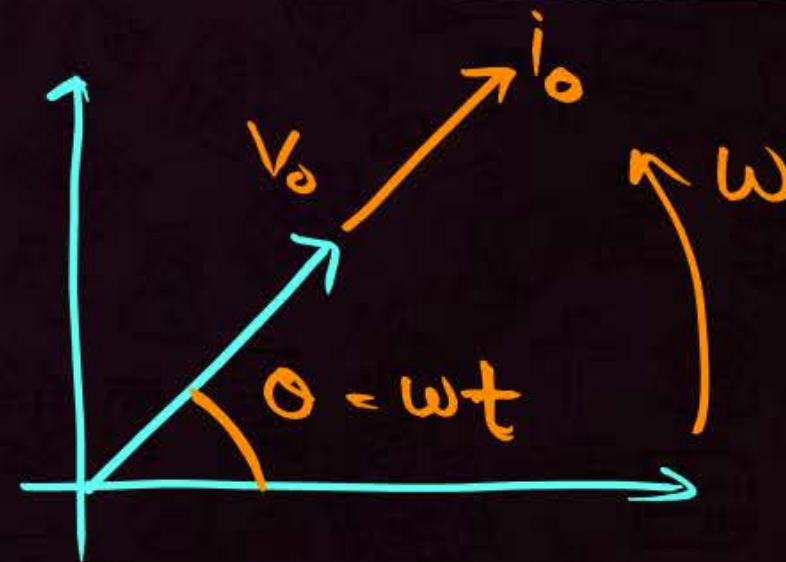
$$i_{rms} = \frac{V_{rms}}{R}$$

• V & i are in same phase



⇒ values max/min attained at same time =

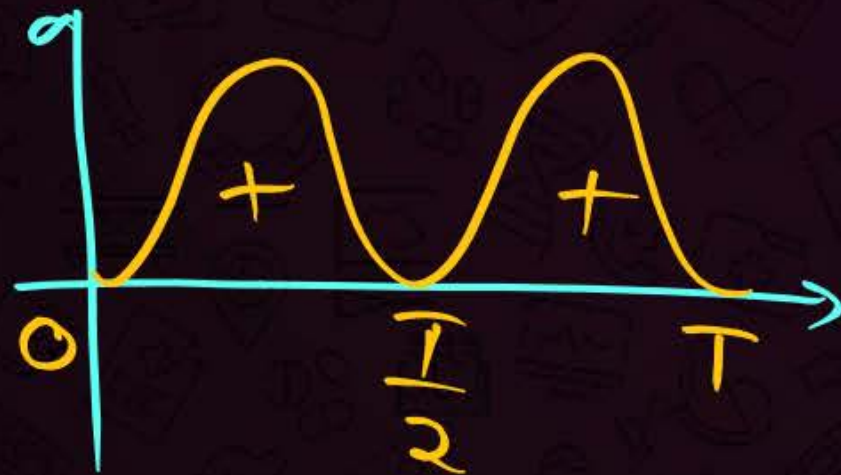
* Phasor diagram (Vector)



$$P = Vi$$

$$P = V_o \sin \omega t \quad i_o \sin \omega t$$

$$P = V_o i_o \sin^2 \omega t$$



$$P_{av} = V_o i_o \times \frac{1}{2}$$

$$P_{av} = \frac{V_o i_o}{2} \rightarrow \frac{V_o}{\sqrt{2}} \times \frac{i_o}{\sqrt{2}}$$

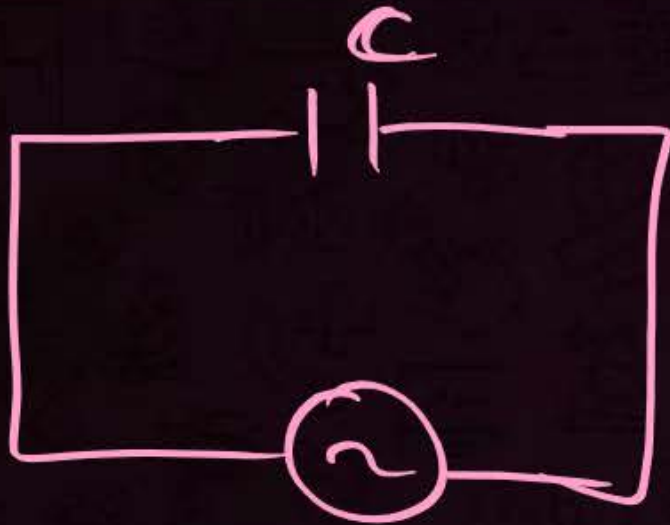
$$P_{av} = V_{rms} i_{rms}$$

$$P_{av} = i_{rms}^2 R = \frac{V_{rms}^2}{R}$$



AC Source connected to Capacitor

Purely Capacitive circuit



* same phase x

* i leads V by $90^\circ \left(\frac{\pi}{2}\right)$

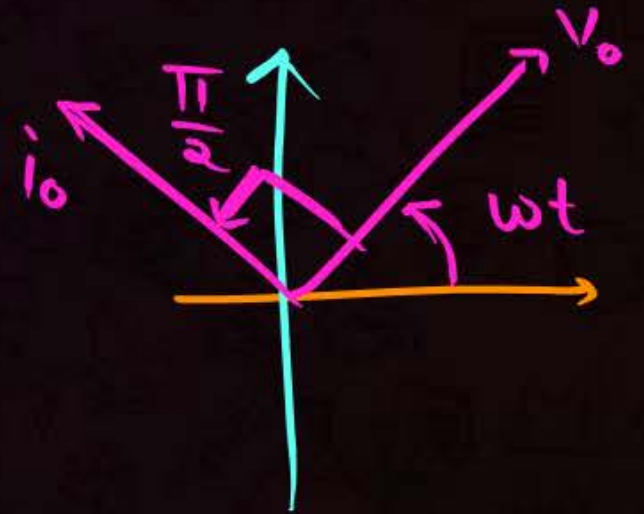
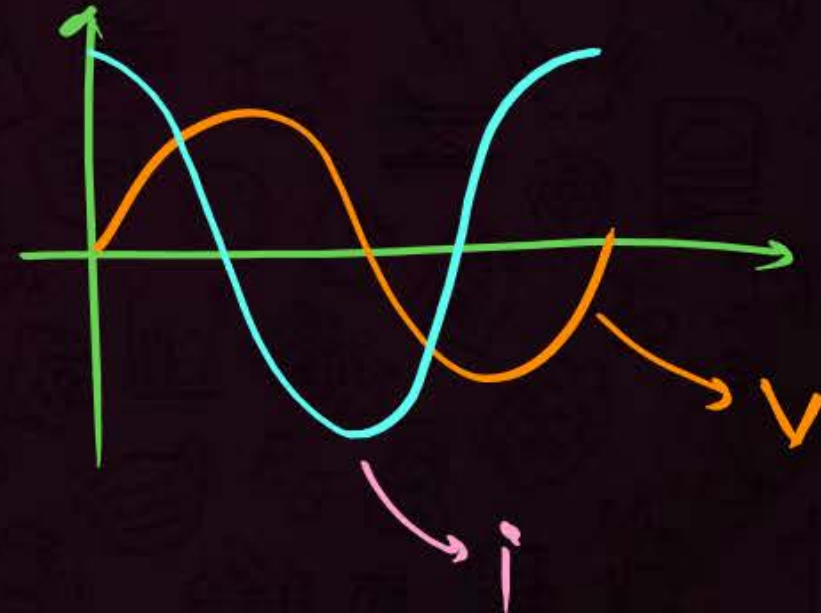
* V lags i by $90^\circ \left(\frac{\pi}{2}\right)$

* $V = V_0 \sin \omega t$ → given.

$$i = i_0 \cos \omega t$$

$$i = i_0 \sin \left(\omega t + \frac{\pi}{2} \right)$$

*



$$P = V i$$

$$P = V_0 \sin \omega t \cdot i_0 \cos \omega t$$

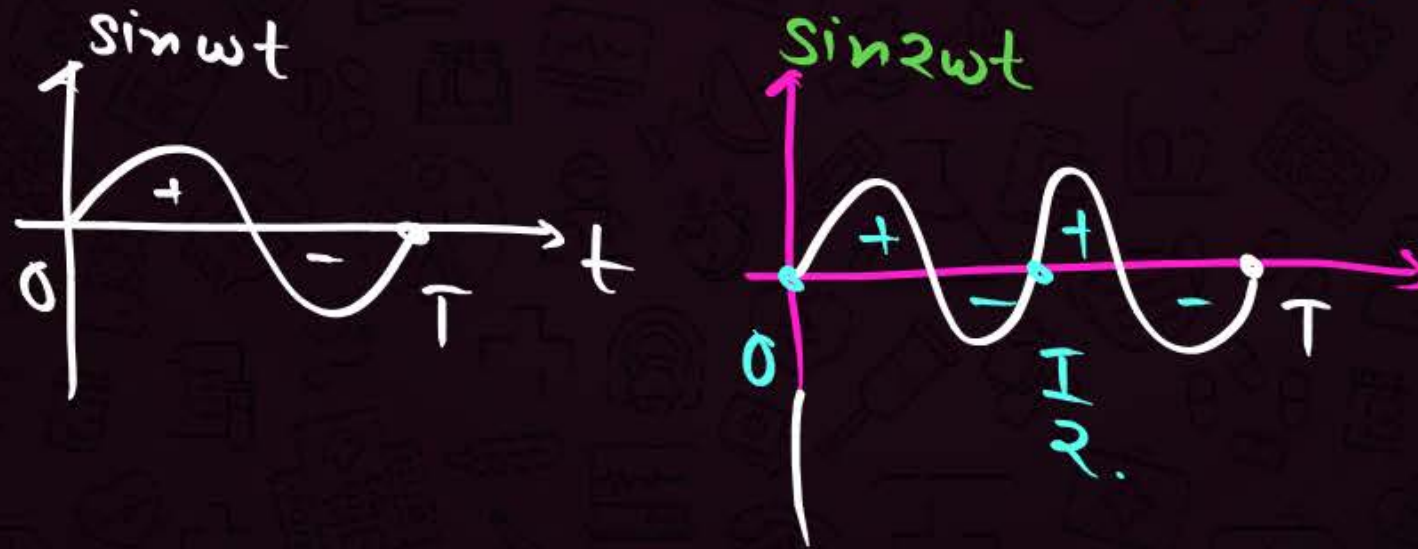
$$P = V_0 i_0 \frac{\sin \omega t \cos \omega t \times 2}{2}$$

$$P = \frac{V_0 i_0}{2} \sin 2\omega t \longrightarrow P_{av} = 0$$

$$\therefore \langle \sin 2\omega t \rangle = 0$$

Ques $P_{av} = 0$
(Full cycle)

Ques $P_{av} = ?$
(Half cycle)
↓
 $P_{av} = 0$



$$i_o = \frac{V_o}{X_c}$$

$$I_{rms} = \frac{V_{rms}}{X_c}$$

$X_c \rightarrow$ capacitive reactance.

\rightarrow resistance of capacitor

$$X_c = \frac{1}{\omega C} = \frac{1}{2\pi f C}$$

Ques If ω is doubled,
 X_c becomes half.

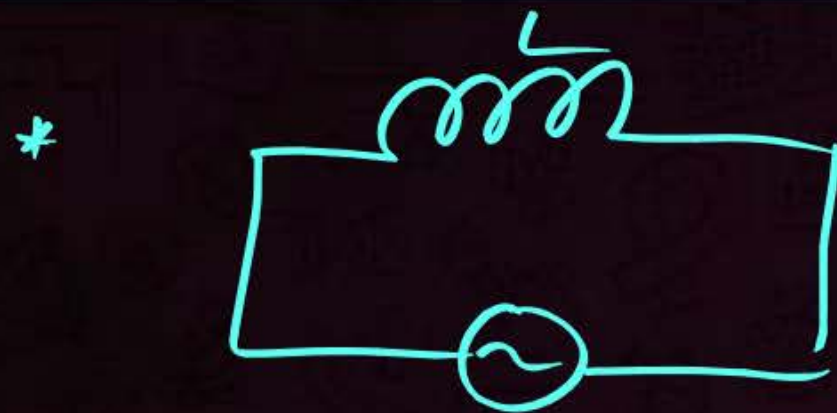
$$X_c \propto \frac{1}{\omega}$$

$\swarrow \times 2$ $\searrow 2\omega$



AC Source connected to Inductor

→ Purely inductive circuit



Given. $V = V_0 \sin \omega t$

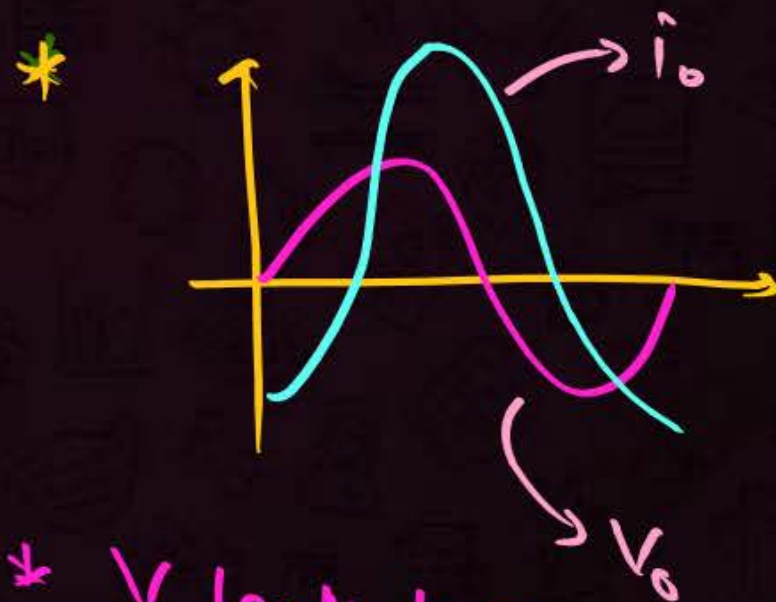
$$i = i_0 \sin\left(\omega t - \frac{\pi}{2}\right)$$
$$i = -i_0 \cos \omega t$$

* $i_0 = \frac{V_0}{X_L}$, $i_{rms} = \frac{V_{rms}}{X_L}$

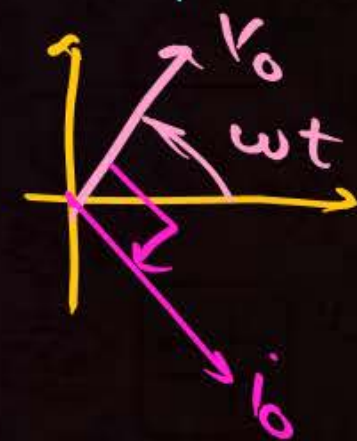
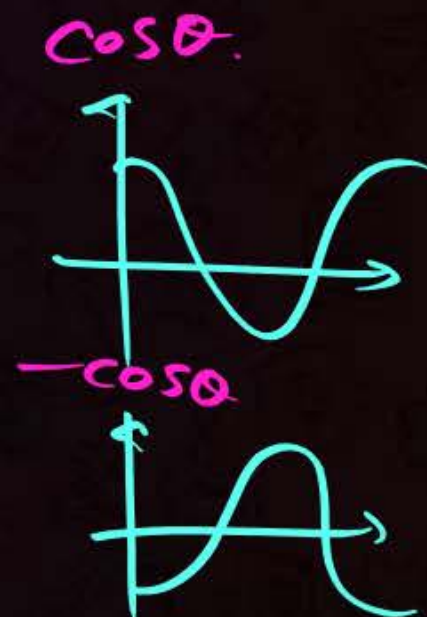
* $X_L \rightarrow$ inductive reactance.

* $X_L = \omega L = 2\pi f L$

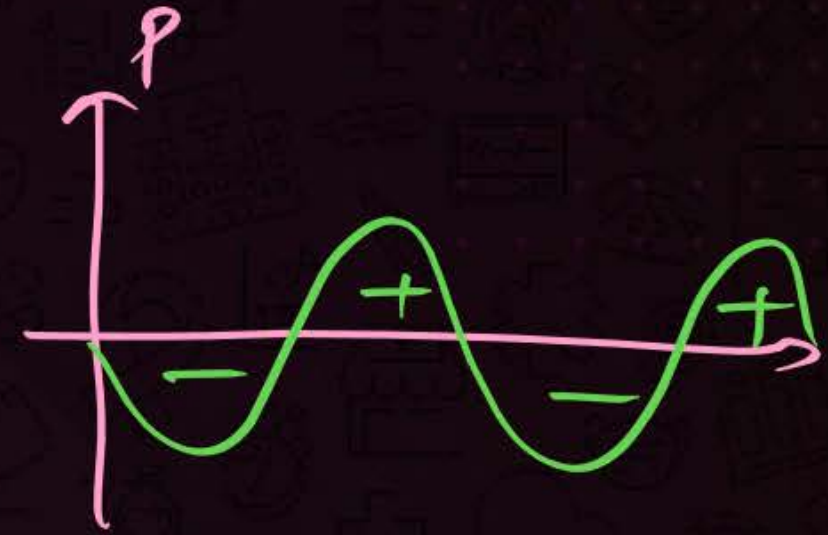
* $X_L \propto \omega$



* V leads by 90°
i lags by 90°



*
$$P = -\frac{V_o I_o}{2} \sin 2\omega t$$



* $P_{av} = 0 \rightarrow$ full cycle.
 \searrow Half cycle

QUESTION



In an AC circuit containing only capacitance, the current

(AIIMS 1997)

- 1 leads the voltage by 180° ~~X~~
- 2 lags the voltage by 90° ~~X~~
- 3 leads the voltage by 90° ✓
- 4 remains in phase with the voltage. ~~X~~

QUESTION



A small signal voltage $V(t) = V_0 \sin \omega t$ is applied across an ideal capacitor C

(NEET 2016)

same phase

- 1 Current $I(t)$ (is in phase) with voltage $V(t)$.
X
- 2 Current $I(t)$ leads voltage $V(t)$ by 180° .
✓ X
- 3 Current $I(t)$ lags voltage $V(t)$ by 90° .
X
- 4 Over a full cycle the capacitor C does not consume any energy from the voltage source.
✓

$$P_{av} = 0$$

QUESTION



In an A.C. circuit, an alternating voltage $e = 200\sqrt{2} \sin(100t)$ volt is connected to capacitor of capacity $1 \mu\text{F}$. The r.m.s. value of current in the circuit is **(2011)**

- 1 10 mA
- 2 100 mA
- 3 200 mA
- ☒ 4 20 mA

$$\begin{aligned}
 V_0 &= 200\sqrt{2} \quad \xrightarrow{\quad} \quad V_{\text{rms}} = \frac{200\sqrt{2}}{\sqrt{2}} = 200 \\
 \omega &= 100 \\
 C &= 1 \mu\text{F} = 10^{-6} \text{ F} \\
 X_C &= \frac{1}{\omega C} = \frac{1}{100 \times 10^{-6}} \\
 &= \frac{10^6}{100} = 10^4 \Omega \\
 I_{\text{rms}} &= \frac{V_{\text{rms}}}{X_C} = \frac{200}{10^4} \\
 &= \frac{2}{100} \text{ A} = \frac{2}{100} \times 1000 \text{ mA} = 20 \text{ mA}
 \end{aligned}$$

QUESTION



A $40\ \mu\text{F}$ capacitor is connected to a 200 V, 50 Hz ac supply. The r.m.s. value of the current in the circuit is, nearly (NEET 2020)

$\rightarrow V_{\text{rms}} = 200\text{ V}$

- 1 1.7 A
- 2 2.05 A
- ☒ 3 2.5 A
- 4 25.1 A

$$i_{\text{rms}} = \frac{200}{X_c}$$

$$X_c = \frac{1}{\omega C} = \frac{1}{2\pi f C}$$

$$= \frac{1}{2\pi \times 50 \times 40 \times 10^{-6}}$$

$$X_c = \frac{10^4}{2\pi \times 50 \times 40} = \frac{10^4}{40\pi} = \frac{10^3}{4\pi}$$

$$i_{\text{rms}} = \frac{200 \times 4\pi}{10^3} = \frac{4\pi}{5} = \frac{4 \times 3.14}{5} = \frac{12.56}{5} = 2.5 \dots$$

QUESTION



Assertion: No power loss associated with pure capacitor in ac circuit.

~~**Reason:**~~ No current is flowing in this circuit.

(AIIMS 2007)

$i \neq 0$

$P_{av} = 0$

- 1 Assertion (A) is True, Reason (R) is True; Reason (R) is a correct explanation for Assertion (A)
- 2 Assertion (A) is True, Reason (R) is True; Reason (R) is not a correct explanation for Assertion (A)
- 3 ☒ Assertion (A) is True, Reason (R) is False.
- 4 Assertion (A) is False, Reason (R) is True.

Assertion: The alternating current lags behind the e.m.f. by a phase angle of $\pi/2$, when AC flows through an inductor.

Reason: The inductive reactance increases as the frequency of AC source decreases.

$$X_L = \omega L = 2\pi f L \quad (X_L \propto f) \quad f \downarrow \Rightarrow X_L \downarrow$$

(AIIMS 2008)

- 1 Assertion (A) is True, Reason (R) is True; Reason (R) is a correct explanation for Assertion (A)
- 2 Assertion (A) is True, Reason (R) is True; Reason (R) is not a correct explanation for Assertion (A)
- 3 Assertion (A) is True, Reason (R) is False.
- 4 Assertion (A) is False, Reason (R) is True.

QUESTION



The reactance of an inductance of 0.01 H to a 50 Hz A.C. is

[AIIMS 1995]

- 1 1.04 Ω
- 2 6.28 Ω
- 3 0.59 Ω
- 4 3.14 Ω

$$\begin{aligned} X_L &= \omega L = 2\pi f L \\ &= 2\pi \times 50 \times \frac{1}{100} \\ &= \pi = 3.14 \Omega \end{aligned}$$

Statement-I: If the frequency of alternating current in an ac circuit consisting of an inductance coil is increased then current gets decreased.

Statement-II: The current is inversely proportional to frequency of alternating current in purely inductive circuit.

- 1** Both Statement-I and Statement-II are correct
- 2** Both Statement-I and Statement-II are incorrect
- 3** Statement-I is correct and Statement-II incorrect
- 4** Statement-I is incorrect and Statement-II is correct

$$i_0 = \frac{V_0}{X_L} = \frac{V_0}{2\pi f L} \Rightarrow i_0 \propto \frac{1}{f}$$

$$f \uparrow \Rightarrow i_0 \downarrow$$

QUESTION



HW

If R , X_L and X_C represent resistance, inductive reactance and capacitive reactance. Then which of the following is dimensionless:

[31 Jan, 2023 (S-I)]

- 1 RX_LX_C
- 2 $\frac{R}{\sqrt{X_LX_C}}$
- 3 $\frac{R}{X_LX_C}$
- 4 $R\frac{X_L}{X_C}$

Ques

Purely Capacitive

$$-30 + 90 = 60$$

$$110 - 90 = 20$$

$$V = V_0 \sin(\omega t + \underline{30^\circ}) \Rightarrow \dot{I} = i_0 \sin(\omega t + 120^\circ) \checkmark$$

$$V = V_0 \sin(\omega t - 30^\circ) \Rightarrow \dot{I} = i_0 \sin(\omega t + 60^\circ)$$

$$\dot{I} = i_0 \sin(\omega t + 110^\circ) \Rightarrow V = V_0 \sin(\omega t + 20^\circ)$$

Ques

Purely inductive

$$\begin{aligned} 70 - 90 \\ = -20^\circ \end{aligned}$$

$$V = V_0 \sin(\omega t + 70^\circ) \Rightarrow \dot{I} = i_0 \sin(\omega t - 20^\circ)$$

$$i = i_0 \sin(\omega t - 40^\circ) \Rightarrow V = V_0 \sin(\omega t + 50^\circ)$$

$$\begin{aligned} -40 + 90 \\ = 50^\circ \end{aligned}$$

QUESTION



The equation of current in a purely inductive circuit is $5 \sin(49\pi t - 30^\circ)$. If the inductance is 30 mH then the equation for the voltage across the inductor, will be:

{Let $\pi = \frac{22}{7}$ }

$\rightarrow V$ leads by 90°

[28 July, 2022 (S-I)]

(JEE Mains)

$-30^\circ + 90^\circ = \underline{\underline{60^\circ}}$

~~1~~ $1.47 \sin(49\pi t - 30^\circ)$

~~2~~ $1.47 \sin(49\pi t + 60^\circ)$

~~3~~ $23.1 \sin(49\pi t - 30^\circ)$

4 $23.1 \sin(49\pi t + 60^\circ)$

$i_0 = 5$

$X_L = \omega L = 49\pi \times 30 \times 10^{-3}$
 $= 49 \times \frac{22}{7} \times \frac{30}{1000}$

$i_0 = \frac{V_0}{X_L}$

$= \frac{462}{100} = 4.62$

$V_0 = i_0 X_L = 5 \times 4.62 = 23.1$



Watt-less Currents



The current in purely capacitive and purely inductive circuits are called wattless currents since they consume no power.

$$\left. \begin{matrix} X_C \\ X_L \end{matrix} \right\} \rightarrow i \rightarrow \text{wattless}$$



Variation of Reactance with frequency



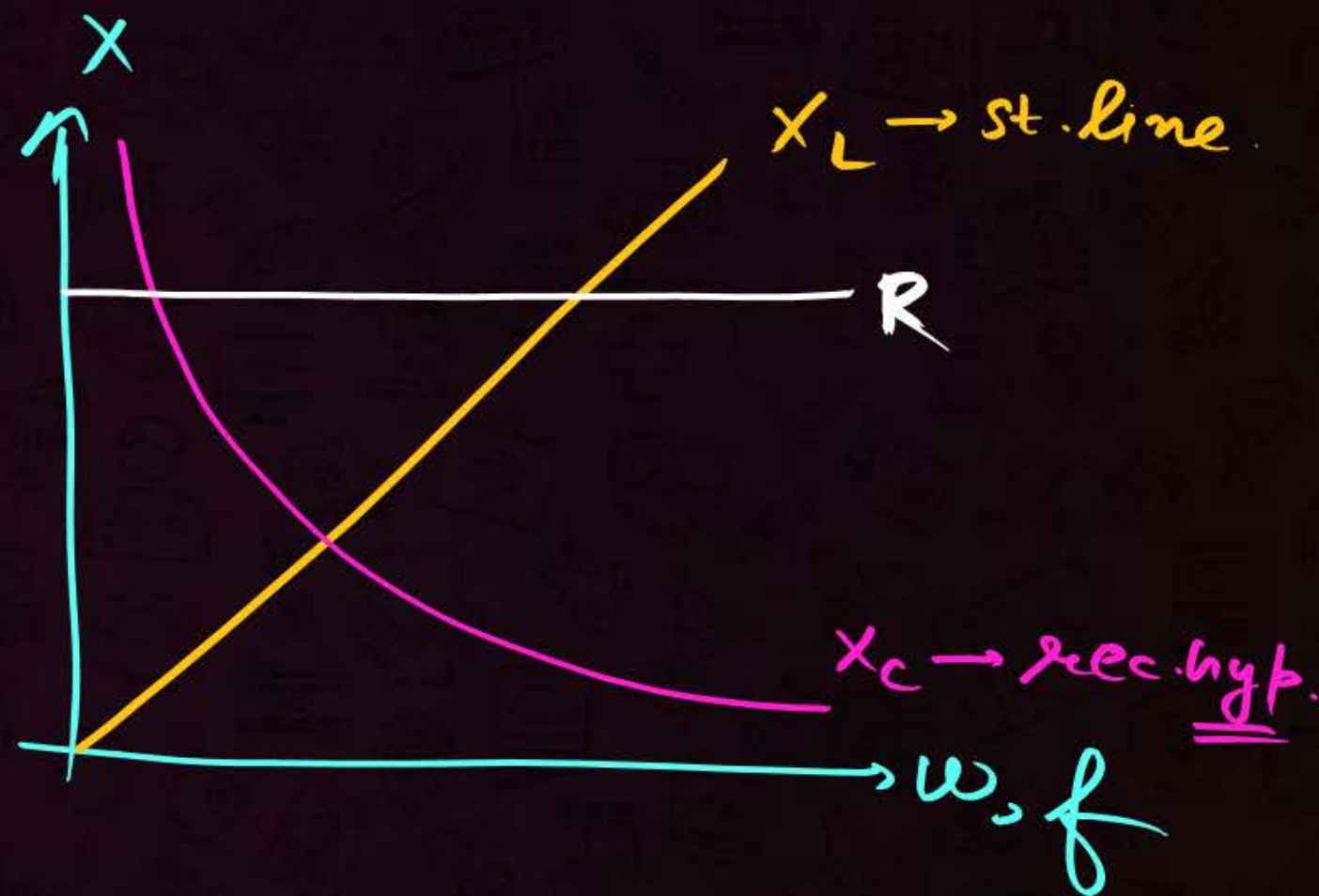
- $X_L = \omega L = 2\pi f L$

$$X_L \propto \omega \text{ or } X_L \propto f$$

- $X_C = \frac{1}{\omega C} = \frac{1}{2\pi f C}$

$$X_C \propto \frac{1}{\omega} \text{ or } X_C \propto \frac{1}{f}$$

- $R \rightarrow$ independent of ω or f



QUESTION



The reactance of a capacitor of capacitance C is X . If both the frequency and capacitance be doubled, then new reactance will be **[CBSE AIPMT 2001]**

- 1 X
- 2 $2X$
- 3 $4X$
- ☒ 4 $X/4$

$$X_C = \frac{1}{2\pi f C}$$

$$X_C' = \frac{1}{2\pi \times \underline{2f} \times \underline{2C}} = \frac{X_C}{4}$$



High pass and Low pass filter



DC circuit $\Rightarrow f=0$

High f AC $\Rightarrow f \rightarrow \infty$

Capacitor

$$X_C \propto \frac{1}{f}$$

DC $\rightarrow f=0 \Rightarrow \boxed{X_C \rightarrow \infty}$

AC $\rightarrow f \rightarrow \infty \Rightarrow \boxed{X_C \rightarrow 0}$

blocks DC, allows AC

* High pass filter

Inductor $X_L \propto f$

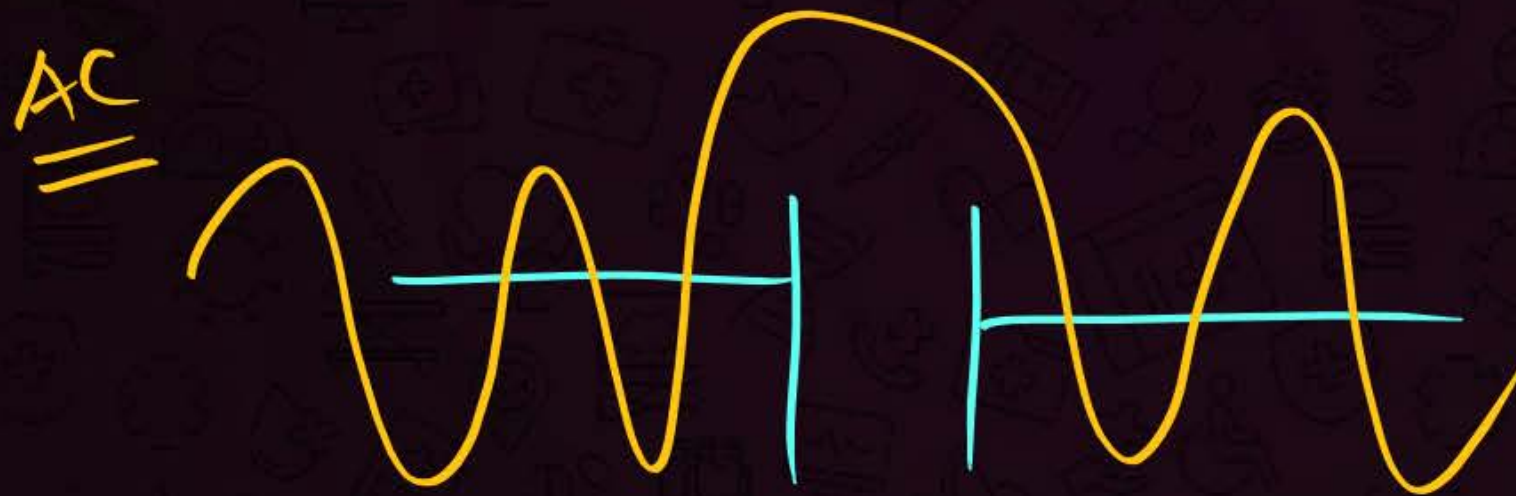
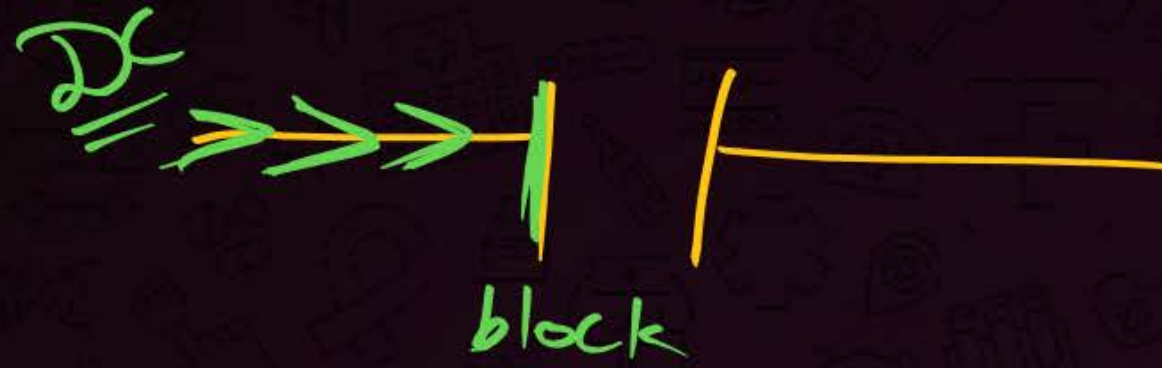
DC $\rightarrow f=0 \rightarrow X_L=0$

AC $\rightarrow f \rightarrow \infty \Rightarrow X_L \rightarrow \infty$

Blocks AC, allows DC.

Low pass filter

Bkanti



Statement-I : Capacitor serves as a block for dc and offers an easy path to ac.

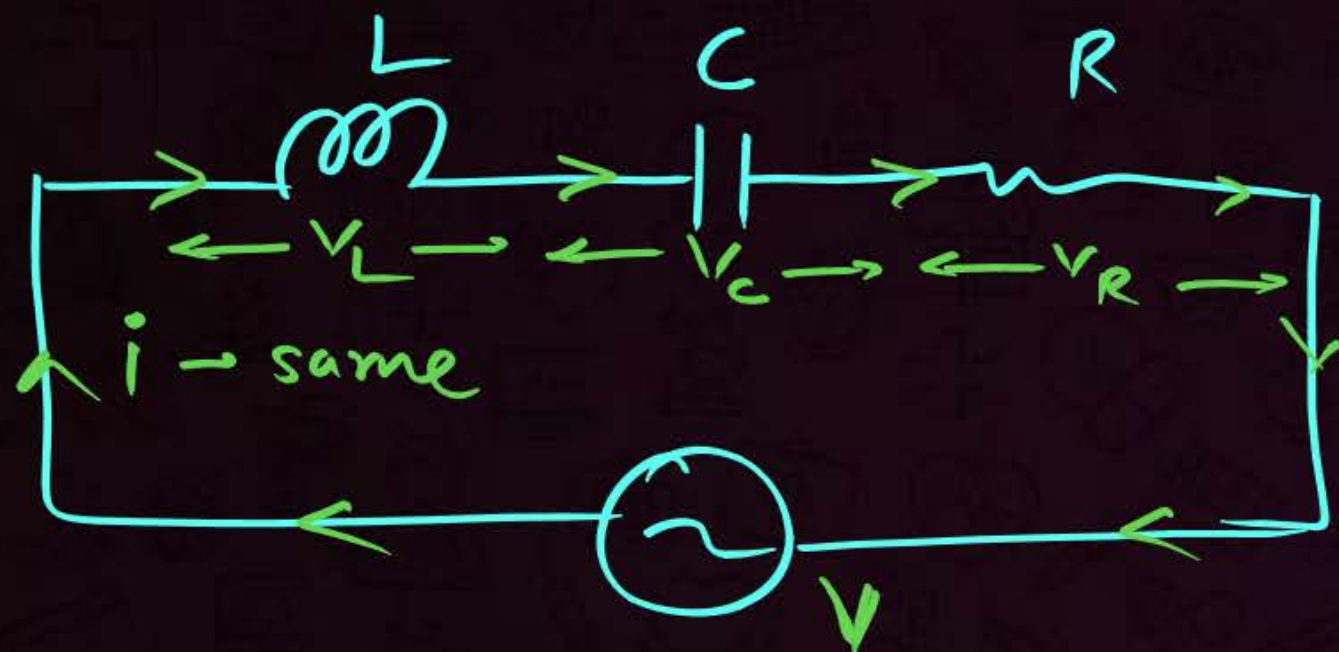
Statement-II : Capacitive reactance is inversely proportional to frequency.

$$X_c \propto \frac{1}{f}$$

- 1** Both Statement-I and Statement-II are correct
- 2** Both Statement-I and Statement-II are incorrect
- 3** Statement-I is correct and Statement-II incorrect
- 4** Statement-I is incorrect and Statement-II is correct



Series LCR Circuit with AC



$$i = i_0 \sin \omega t \text{ (given)}$$

* $V_L, V_C, V_R, V \Rightarrow$ voltages at instant t .

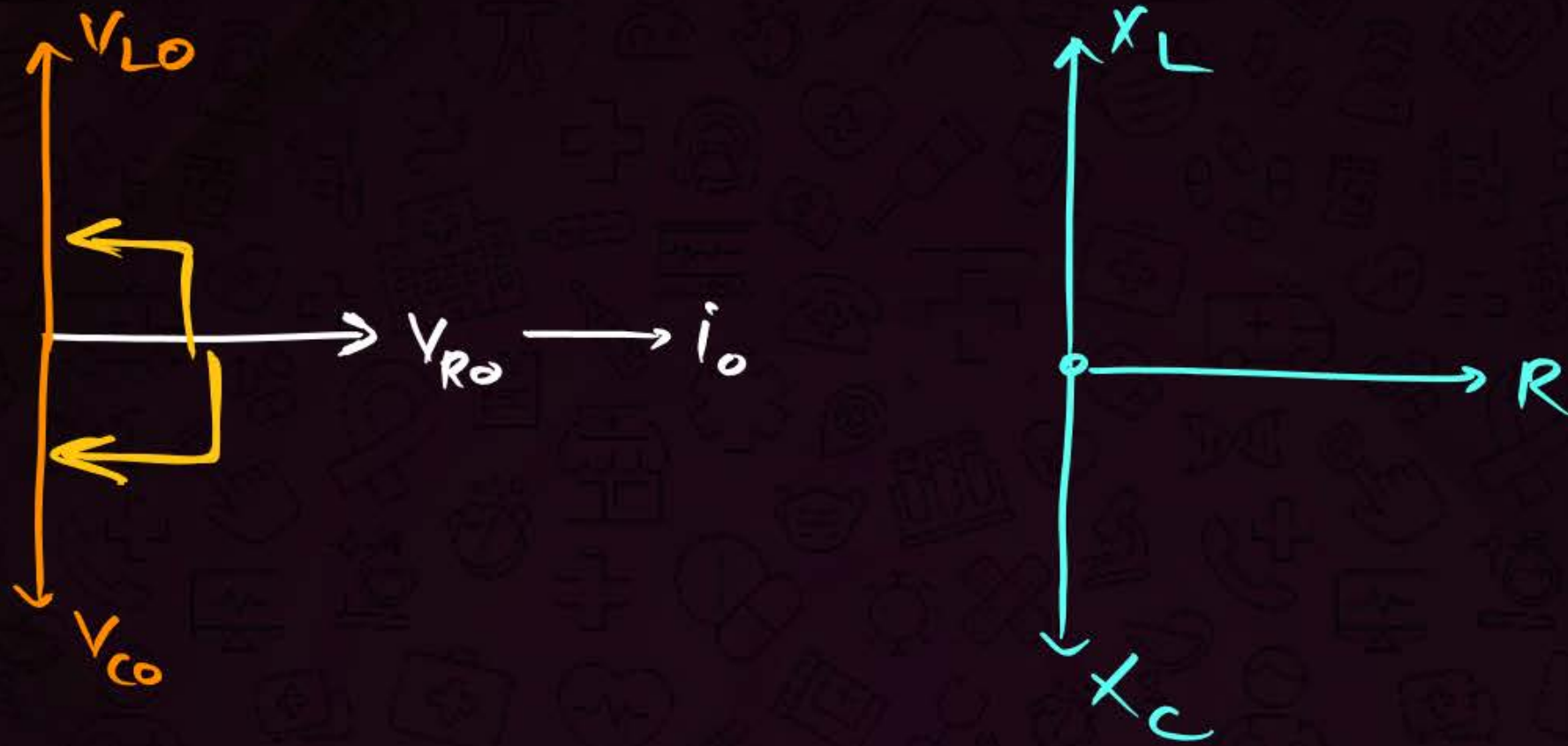
$$V_L + V_C + V_R = V$$

* $V_{L0} + V_{C0} + V_{R0} = V_0$ ✗

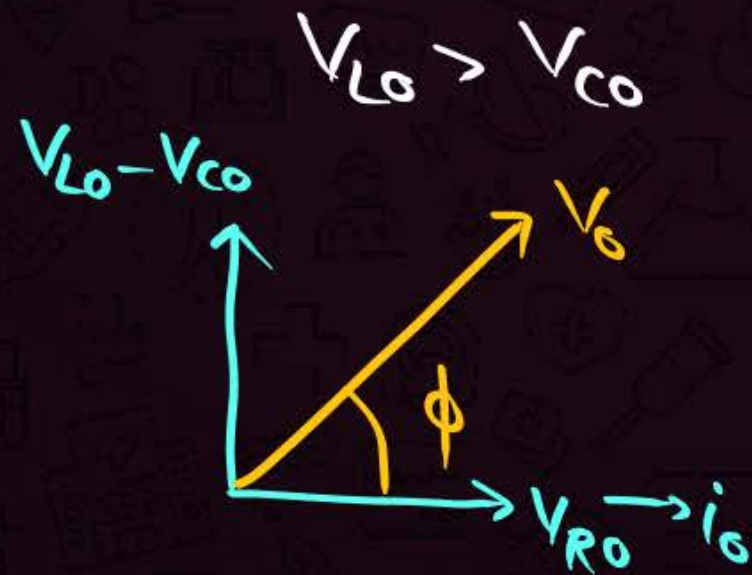
(maximum voltages
Can't be added directly)

* Added by Phasor (vector)

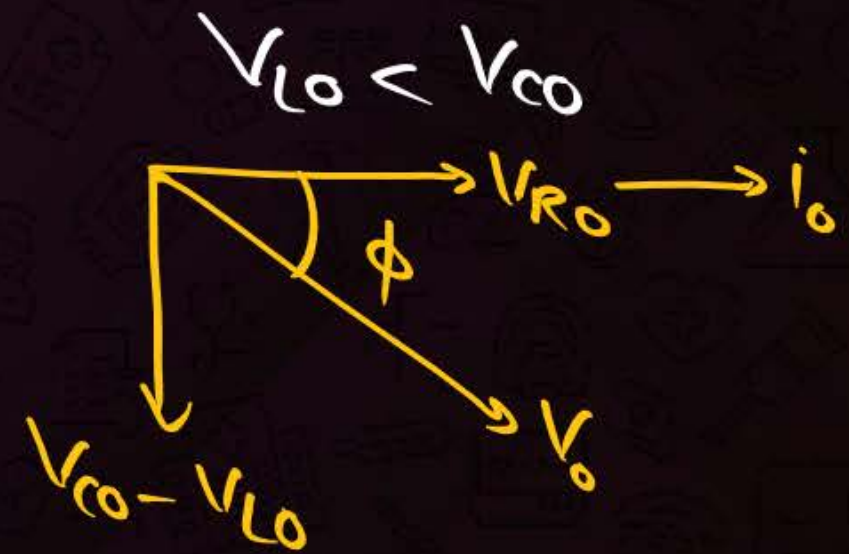
$$\vec{V}_{L0} + \vec{V}_{C0} + \vec{V}_{R0} = \vec{V}_0 \quad \checkmark$$



a) L dominated

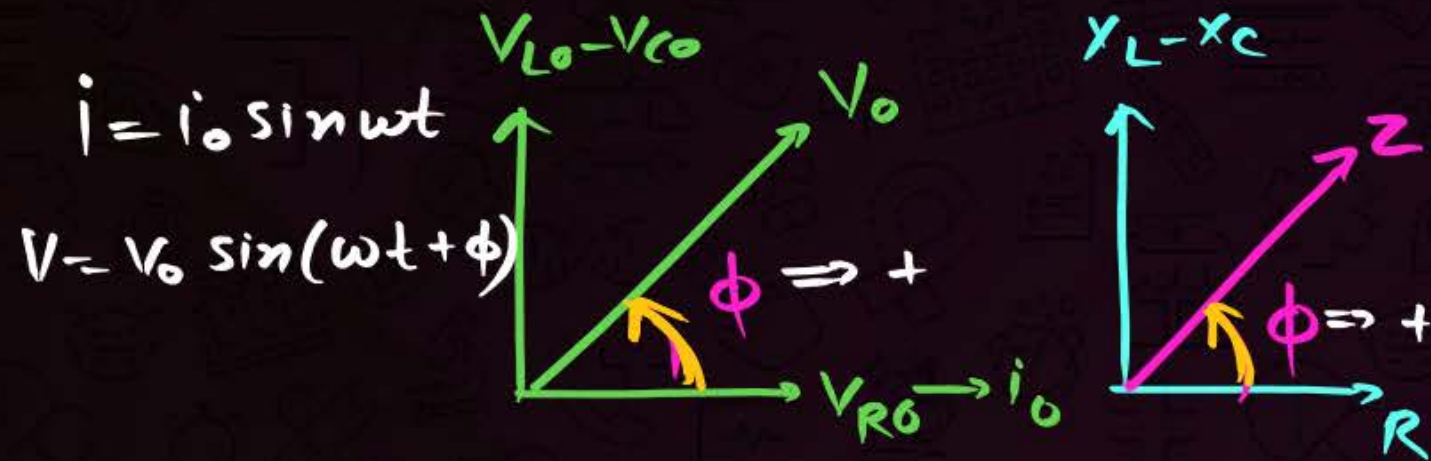


b) C dominated



a) L dominated

$$V_{L0} > V_{C0}, X_L > X_C$$



$$V_0 = \sqrt{(V_{L0} - V_{C0})^2 + V_{R0}^2}$$

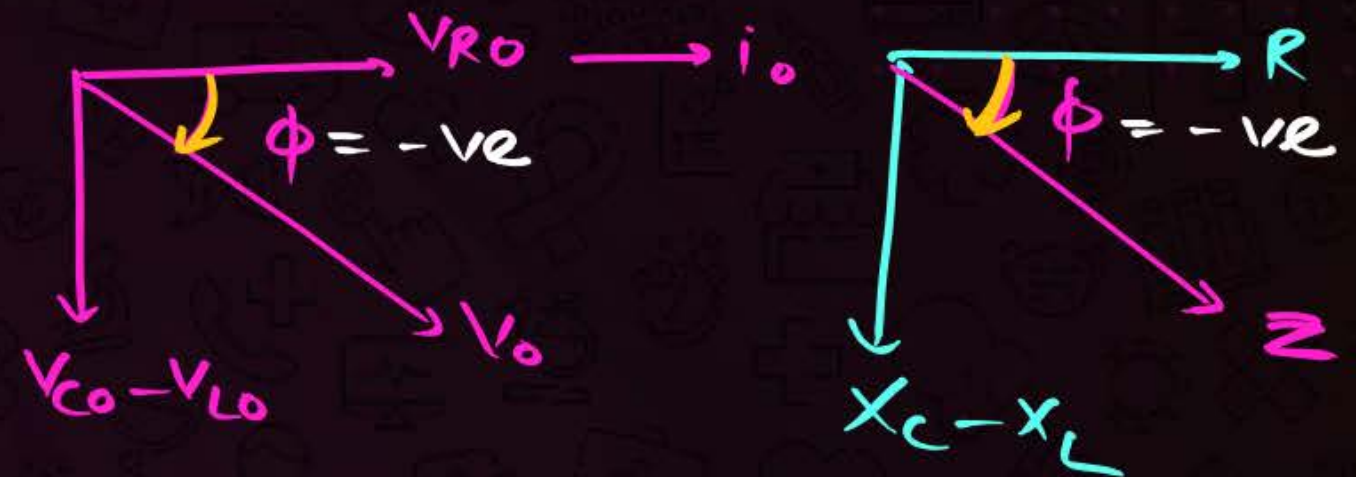
$$Z = \sqrt{(X_L - X_C)^2 + R^2}$$

V_0 leads i_0 by ϕ
 i_0 lags V_0 by ϕ

$$\tan \phi = \frac{V_{L0} - V_{C0}}{V_{R0}} = \frac{X_L - X_C}{R}$$

b) C dominated

$$V_{L0} < V_{C0}, X_L < X_C$$



$$V_0 = \sqrt{(V_{C0} - V_{L0})^2 + V_{R0}^2}$$

$$Z = \sqrt{(X_C - X_L)^2 + R^2}$$

$$i = i_0 \sin \omega t$$

$$V = V_0 \sin(\omega t - \phi)$$

- * i_0 leads V_0 by ϕ
- * V_0 lags i_0 by ϕ

$$\tan \phi = \frac{V_{C0} - V_{L0}}{V_{R0}} = \frac{X_C - X_L}{R}$$



Impedance



↓
 $Z \rightarrow$ net resistance of
series LCR circuit.

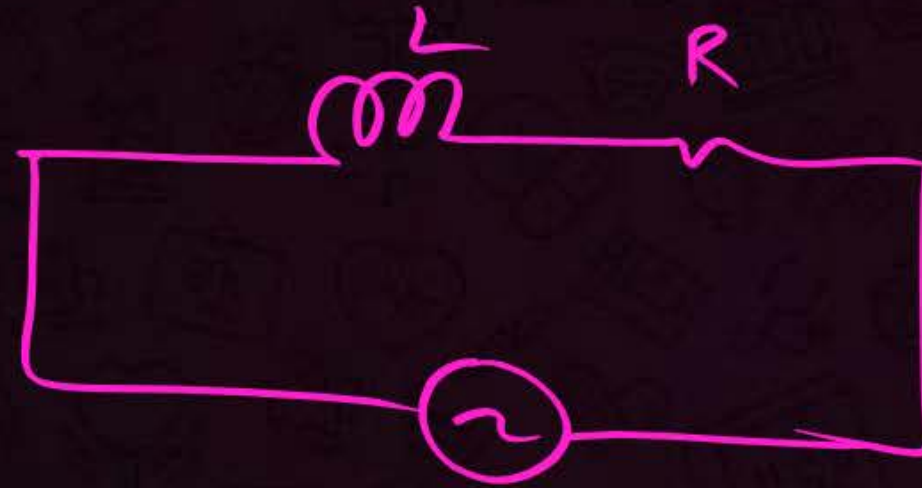
QUESTION



BPU

An A.C. voltage is applied to a resistance R and an inductor L in series. If R and the inductive reactance are both equal to $3\ \Omega$, the phase difference between the applied voltage and the current the circuit is (2011)

- 1 zero
- 2 $\pi/6$
- 3 $\pi/4$
- 4 $\pi/2$



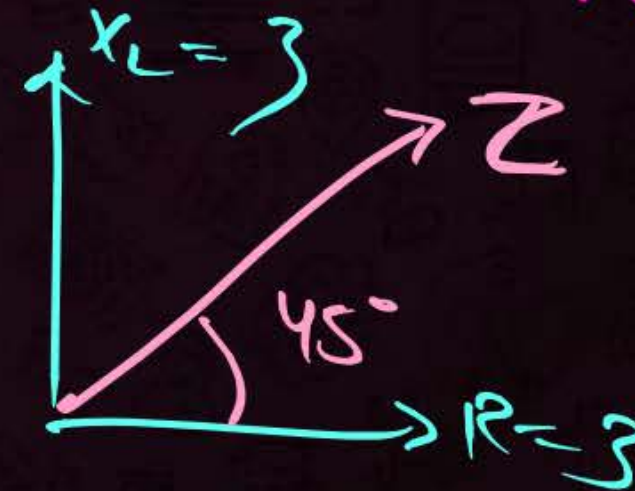
$$Z = 3\sqrt{2}$$

$$Z = \sqrt{3^2 + 3^2}$$

$$R = X_L = 3\ \Omega$$

$$\tan \phi = \frac{X_L - X_C}{R} = \frac{3 - 0}{3} = 1$$

$$\phi = 45^\circ = \frac{\pi}{4}$$



QUESTION



A resistor and a capacitor are connected in series with an a.c. source. If the potential drop, across the capacitor is 15 V and that across resistor is 20 V, the applied voltage is

☒ 1 25 V

☐ 2 40 V

☐ 3 5 V

☐ 4 12 V

$15 = V_R$ *rms value*

$V_C = 20$

$\sqrt{15^2 + 20^2} = \sqrt{225 + 400} = \sqrt{625} = 25$

QUESTION



Match List-I with List-II Choose the most appropriate answer from the options given below : [17 March, 2021 (S-II)]

1 A – ii, B – iii, C – iv, D – i

2 A – ii, B – iii, C – i, D – iv

3 A – i, B – iii, C – iv, D – ii

4 A – ii, B – iv, C – iii, D – i

List – I		List – II	
p	Phase difference between current and voltage in a purely <u>resistive</u> AC circuit	i (R)	$\pi/2$; current leads voltage
Q	Phase difference between current and voltage in a pure <u>inductive</u> AC circuit	ii	Zero
R	Phase difference between current and voltage in a pure capacitive AC circuit	iii	$\pi/2$; <u>current lags</u> voltage
s	Phase difference between current and voltage in an <u>LCR</u> series circuit	iv	$\tan^{-1}(X_C - X_L/R)$

QUESTION



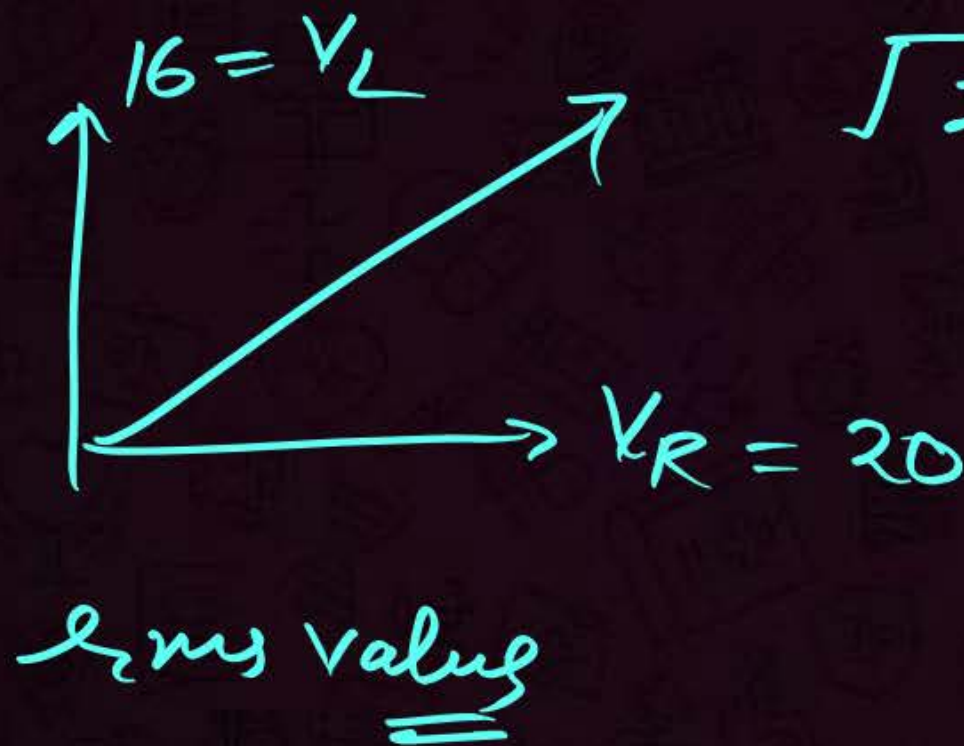
In an AC circuit the potential differences across an inductance and resistance joined in series are respectively 16 V and 20 V. The total potential difference of the source is

1 20.0 V

2 25.6 V

3 31.9 V

4 53.5 V



(AIIMS 2007)

$$\sqrt{20^2 + 16^2} = \sqrt{400 + 256}$$
$$= \sqrt{656}$$
$$= 25.6 \dots$$

Statement-I: When capacitive reactance is smaller than the inductive reactance in LCR ^{circuit} ~~current~~, e.m.f. leads the current.

Statement-II: The phase angle is the angle between the alternating e.m.f. and alternating current of the current. (ϕ)

$$X_L > X_C \Rightarrow \text{Voltage Lead}$$

- 1** Both Statement-I and Statement-II are correct
- 2** Both Statement-I and Statement-II are incorrect
- 3** Statement-I is correct and Statement-II incorrect
- 4** Statement-I is incorrect and Statement-II is correct

QUESTION



390

A series LCR circuit consists of $R = 80 \Omega$, $X_L = 100 \Omega$, and $X_C = 40 \Omega$. The input voltage is $2500 \cos(100 \pi t)$ V. The amplitude of current, in the circuit, is ___ A.

[31 Jan, 2023 (S-II)]

A) 250

~~B) 25~~

C) 2.5

D) None

$$i_0 = \frac{V_0}{Z}$$

$i_0 = ?$

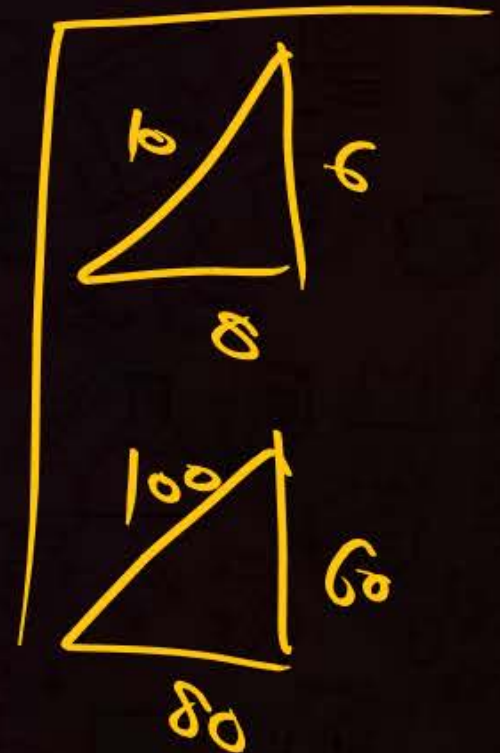
$$Z = \sqrt{(100 - 40)^2 + 80^2}$$

$$= \sqrt{60^2 + 80^2}$$

$$= 100$$

$$i_{rms} = \frac{V_{rms}}{Z}$$

$$i_0 = \frac{2500}{100} = 25$$



QUESTION



How

In a given series LCR circuit $R = 4 \Omega$, $X_L = 5 \Omega$ and $X_C = 8 \Omega$, the current

(AIIMS 2012)

- 1** leads the voltage by $\tan^{-1} (3/4)$
- 2** leads the voltage by $\tan^{-1} (5/8)$
- 3** lags the voltage by $\tan^{-1} (3/4)$
- 4** lags the voltage by $\tan^{-1} (5/8)$

QUESTION



A coil has resistance 30 ohm and inductive reactance 20 ohm at 50 Hz frequency. If an A.C. source, of 200 volt 100 Hz, is connected across the coil, the current in the coil will be (2011)

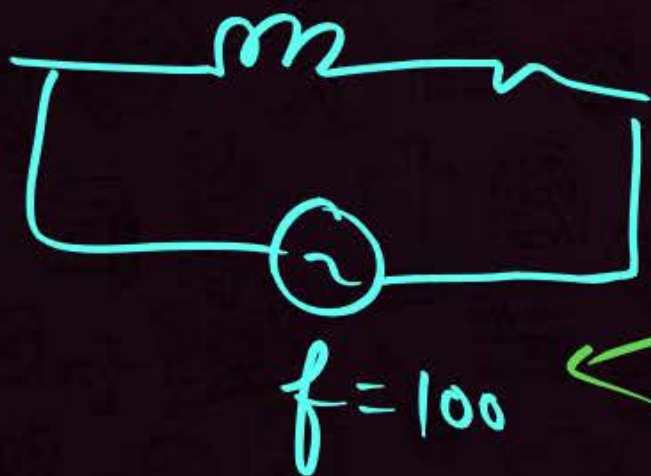
$$R = 30 \Omega$$

$$X_L = 20 \Omega \text{ at } 50 \text{ Hz} \Rightarrow \underline{X_L \propto f}$$

$$V_{rms} = 200 \text{ V}$$

$$f = 100 \text{ Hz}$$

$$X_L = 40 \Omega$$



$$i_{rms} = \frac{V_{rms}}{Z}$$

$$Z = \sqrt{30^2 + 40^2} = 50$$

$$i_{rms} = \frac{200}{50} = 4 \text{ A}$$

1 $20/\sqrt{13} \text{ A}$

2 2.0 A

3 4.0 A

4 8.0 A

QUESTION

HW



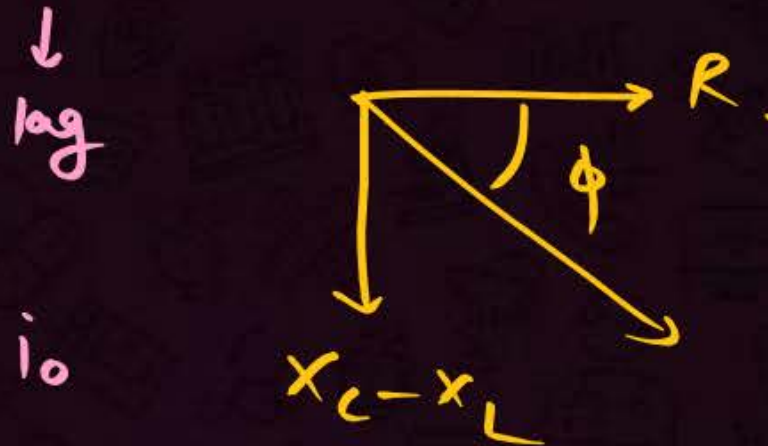
In a circuit L, C and R are connected in series with an alternating voltage source of frequency f . The current leads the voltage by 45° . The value of C is (2005)

1 $\frac{1}{2\pi f(2\pi fL + R)}$

2 $\frac{1}{2\pi f(2\pi fL - R)}$

3 $\frac{1}{\pi f(2\pi fL - R)}$

4 $\frac{1}{\pi f(2\pi fL + R)}$



$$-1 = \frac{X_L - X_C}{R}$$

$$\tan \phi = \frac{X_C - X_L}{R} = +1$$

$$X_C = R + X_L$$

$$X_C = R + 2\pi fL$$

$$\frac{1}{2\pi fC} = R + 2\pi fL$$

$$\frac{1}{2\pi f(R + 2\pi fL)} = C$$

QUESTION



If Wattless current flows in the AC circuit, then the circuit is:

[25 June, 2022 (S-I)]

(JEE Mains)
=

- 1 Purely Resistive circuit ✗
- 2 Purely Inductive circuit ✓
- 3 LCR series circuit ✗
- 4 RC series circuit only ✗



Power consumed in series LCR circuit



$$i = i_0 \sin \omega t$$

$$V = V_0 \sin(\omega t + \phi)$$

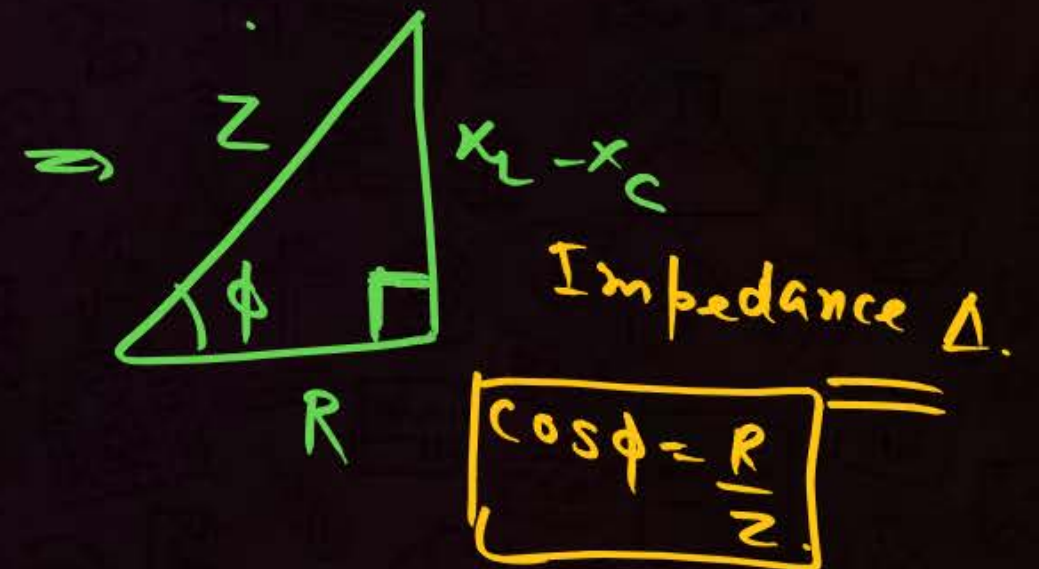
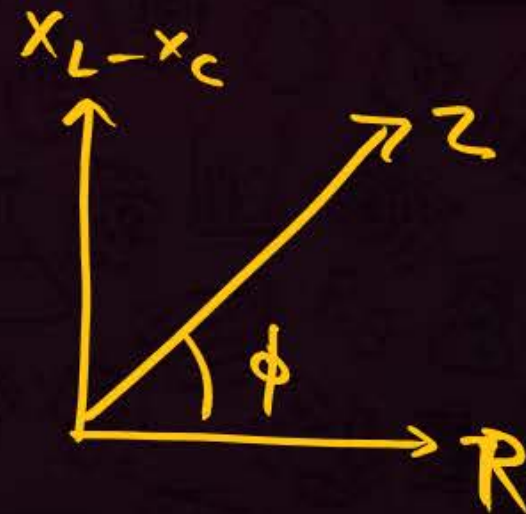
$$P_{av} = \frac{V_0 i_0}{2} \cos \phi$$

series LCR.

$$* P_{av} = \frac{V_0}{\sqrt{2}} \times \frac{i_0}{\sqrt{2}} \cos \phi$$

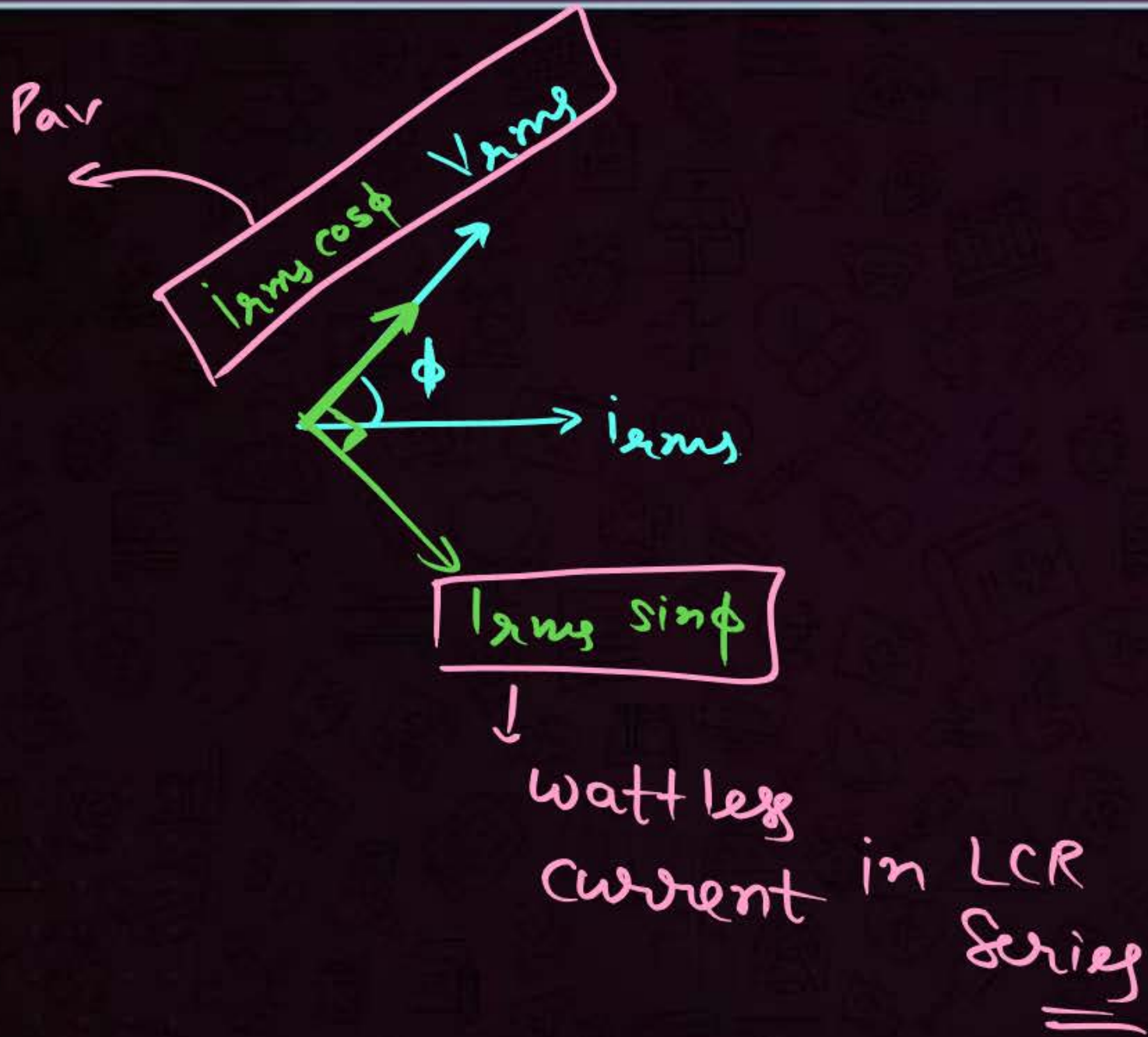
$$P_{av} = \underbrace{V_{rms}} \times \underbrace{i_{rms}} \times \underbrace{\cos \phi}$$

True power Apparent power power factor





Watt-less current in series LCR circuit



Purely L or C

↓
Surge current

Wattless current

QUESTION



The power factor varies between

[AIIMS 1995]

- ☒ 1 0 to 1
- ☐ 2 2 and 2.5
- ☐ 3 1 to 2
- ☐ 4 3.5 to 5



$$\cos \phi = \frac{R}{Z}$$

$$\phi = 0^\circ \Rightarrow \cos \phi = 1$$

$$\phi = 90^\circ \Rightarrow \cos \phi = 0$$

QUESTION



In an a.c. circuit the e.m.f. (ε) and the current (i) at any instant are given respectively by $\varepsilon = E_0 \sin \omega t$, $i = I_0 \sin(\omega t - \phi)$. The average power in the circuit over one cycle of a.c. is (2008)

☒ $\frac{E_0 I_0}{2} \cos \phi$ (Formula)

$V_0 \rightarrow E_0$

☐ $E_0 I_0$

☐ $\frac{E_0 I_0}{2}$

☐ $\frac{E_0 I_0}{2} \sin \phi$

QUESTION



In an ac circuit, V and I are given by $V = 100 \sin(100t)$ volts,
 $I = 100 \sin\left(100t + \frac{\pi}{3}\right)$ mA. The power dissipated in circuit is

- 1 10^4 watt
- 2 10 watt
- 3 2.5 watt
- 4 5 watt

$$\phi = 60^\circ$$

$$i_0 = 100 \text{ mA} \\ = \frac{100}{1000} \text{ A}$$

$$P_{av} = \frac{100}{2} \times \frac{100}{1000} \times \cos 60^\circ$$

$$= \frac{10}{2} \times \frac{1}{2}$$

$$= \frac{10}{4} = 2.5 \text{ W}$$

QUESTION



In instantaneous values of alternating current and voltage in a circuit are given as $i = \frac{1}{\sqrt{2}} \sin(100\pi t)$ ampere, $e = \frac{1}{\sqrt{2}} \sin(100\pi t)$ volt. *Same phase.*

The average power in the watts consumed in the circuit is

- 1** $1/4$
- 2** $\sqrt{3}/4$
- 3** $1/2$
- 4** $1/8$

$$\begin{aligned} P_{av} &= \frac{\frac{1}{\sqrt{2}} \times \frac{1}{\sqrt{2}} \cos 0^\circ}{2} \\ &= \frac{1}{2 \times 2} \times 1 \\ &= \frac{1}{4} \end{aligned}$$

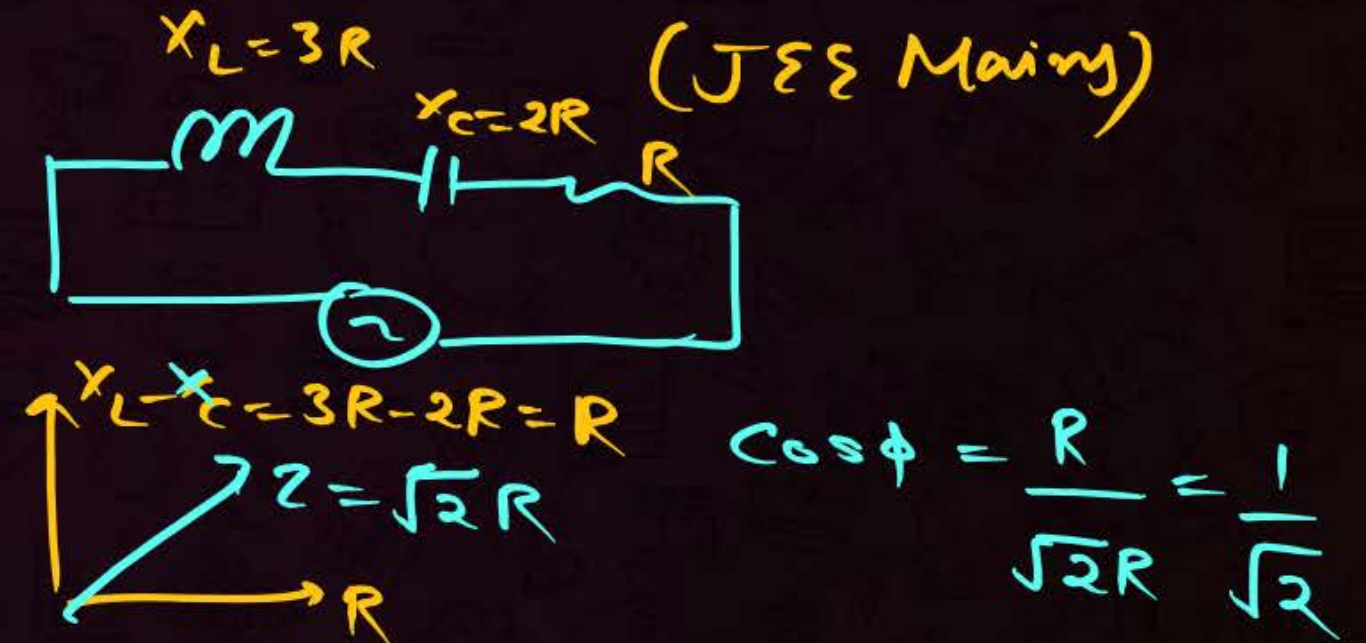
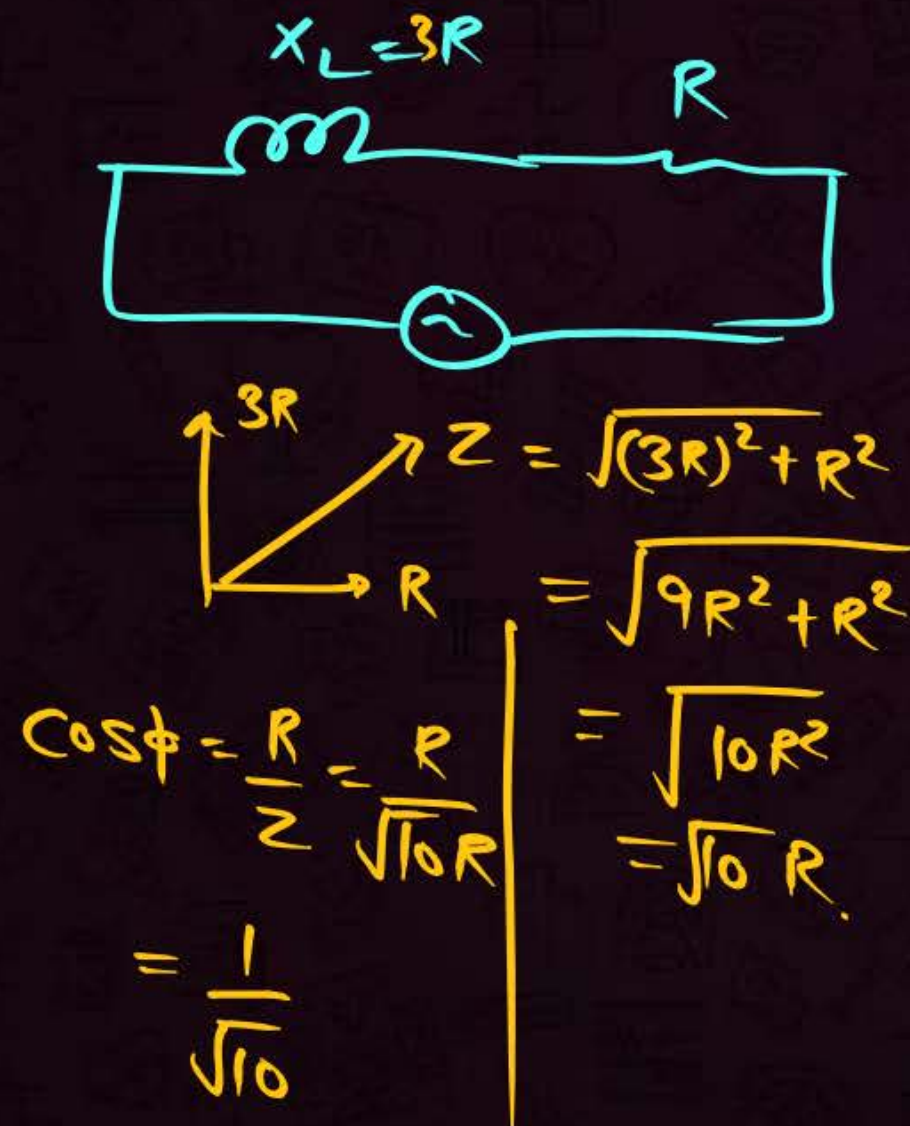
QUESTION



An ac circuit has an inductor and a resistor of resistance R in series, such that $X_L = 3R$. Now, a capacitor is added in series such that $X_C = 2R$. The ratio of new power factor with the old power factor of the circuit is $\sqrt{5}:x$. The value of x is _____

[27 Aug, 2021 (Shift-II)]

- A) 3
- B) 2
- ☒ C) 1
- D) None



$$\frac{1}{\sqrt{2}} = \frac{\sqrt{2}}{2} = \frac{\sqrt{5}}{1} \quad \text{↖}$$

QUESTION



HW

A coil of inductive reactance $31\ \Omega$ has a resistance of $8\ \Omega$. It is placed in series with a condenser of capacitive reactance $25\ \Omega$. The combination is connected to an A.C. source of 110 volt. The power factor of the circuit is **(2006)**

$\frac{R}{Z}$

1 0.80

2 0.33

3 0.56

4 0.64

QUESTION



The potential differences across the resistance, capacitance and inductance are 80 V, 40 V and 100 V respectively in an L-C-R circuit. The power factor of this circuit is

(2016)

1 1.0

2 0.4

3 0.5

4 0.8

$$\cos \phi = \frac{R}{Z} = \frac{V_{R0}}{V_0} = \frac{80}{100} = 0.8 = 0.80$$

$$100 - 40 = 60$$

r

QUESTION

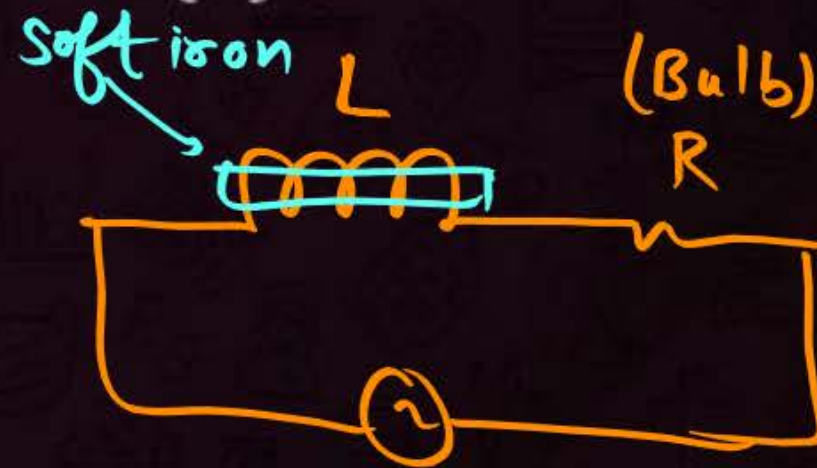


Assertion : A bulb connected in series with a solenoid is connected to ac source. If a soft iron core is introduced in the solenoid, the bulb will glow brighter.

Reason : On introducing soft iron core in the solenoid, the inductance ^{reactance} increases.

Power ↓

- 1 Assertion (A) is true, Reason (R) is true, Reason (R) is a correct explanation for assertion (A).
- 2 Assertion (A) is true, Reason (R) is true, Reason (R) is not a correct explanation for assertion (A).
- 3 Assertion (A) is true, Reason (R) is false.
- 4 Assertion (A) is false, Reason (R) is true.



soft iron
 $\mu_r \gg 1$

$$L = \frac{\mu_0 N^2 A}{l}$$

EMI ↑

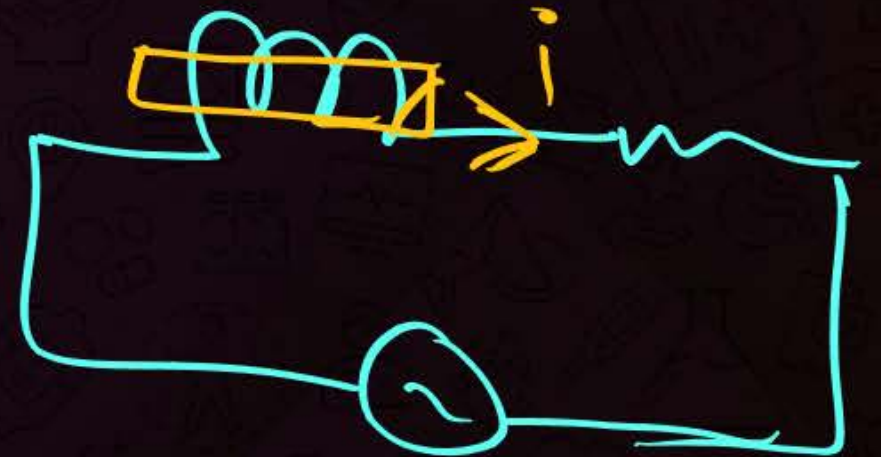
$$L = \mu_r \mu_0 \frac{N^2 A}{l}$$

$$L \uparrow \rightarrow X_L = \omega L$$

$\rightarrow X_L \uparrow$

$$i_0 = \frac{V_0}{Z} = \frac{V_0}{\sqrt{X_L^2 + R^2}}$$

$$X_L \uparrow \Rightarrow i_0 \downarrow$$





Resonance in LCR series circuit



↓
frequency match

$$Z = \sqrt{(X_L - X_C)^2 + R^2}$$

$$i_0 = \frac{V_0}{Z} \rightarrow 0 \Rightarrow \text{min}^m$$

↘ min

$$Z_{\min} = \sqrt{0^2 + R^2} = R.$$

$$Z_{\min} = R.$$

$$(i_0)_{\max} = \frac{V_0}{(Z)_{\min}} = \frac{V_0}{R}.$$

- $X_L - X_C = 0$

$$X_L = X_C$$

$$\omega L = \frac{1}{\omega C}$$

$$\omega^2 = \frac{1}{LC}$$

$$\omega = \frac{1}{\sqrt{LC}} = \omega_r$$

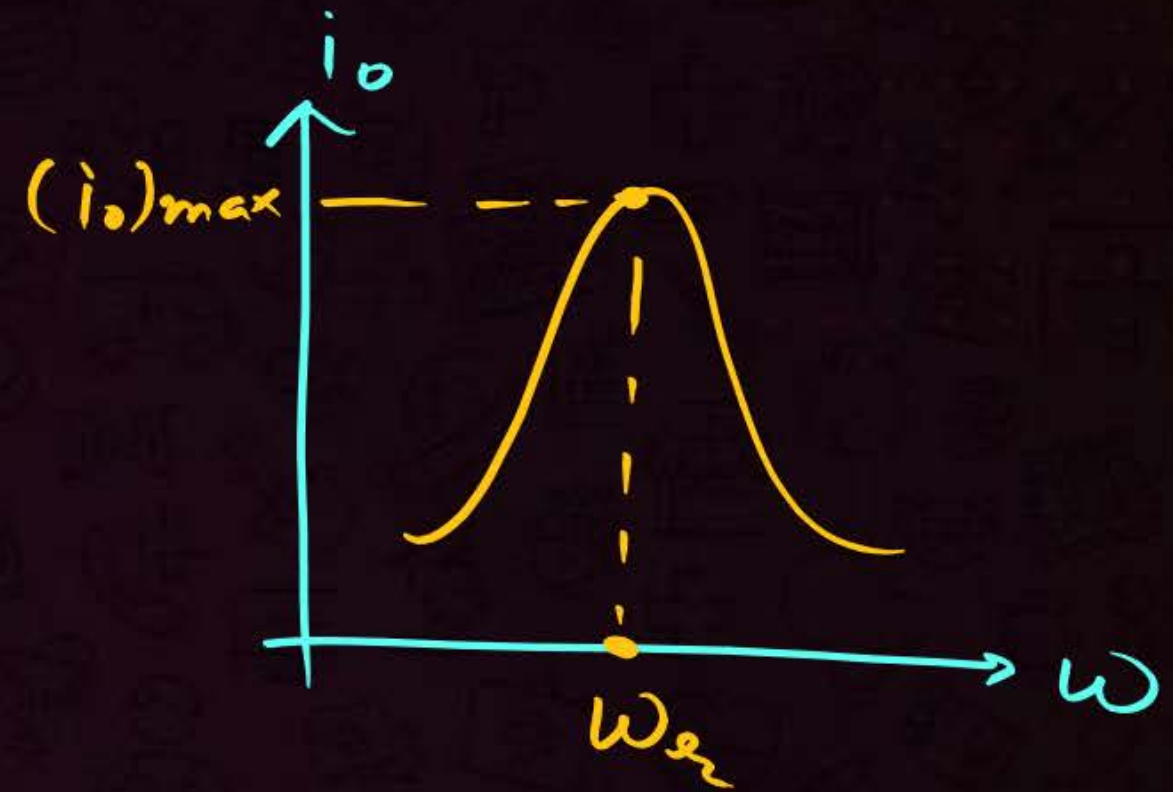
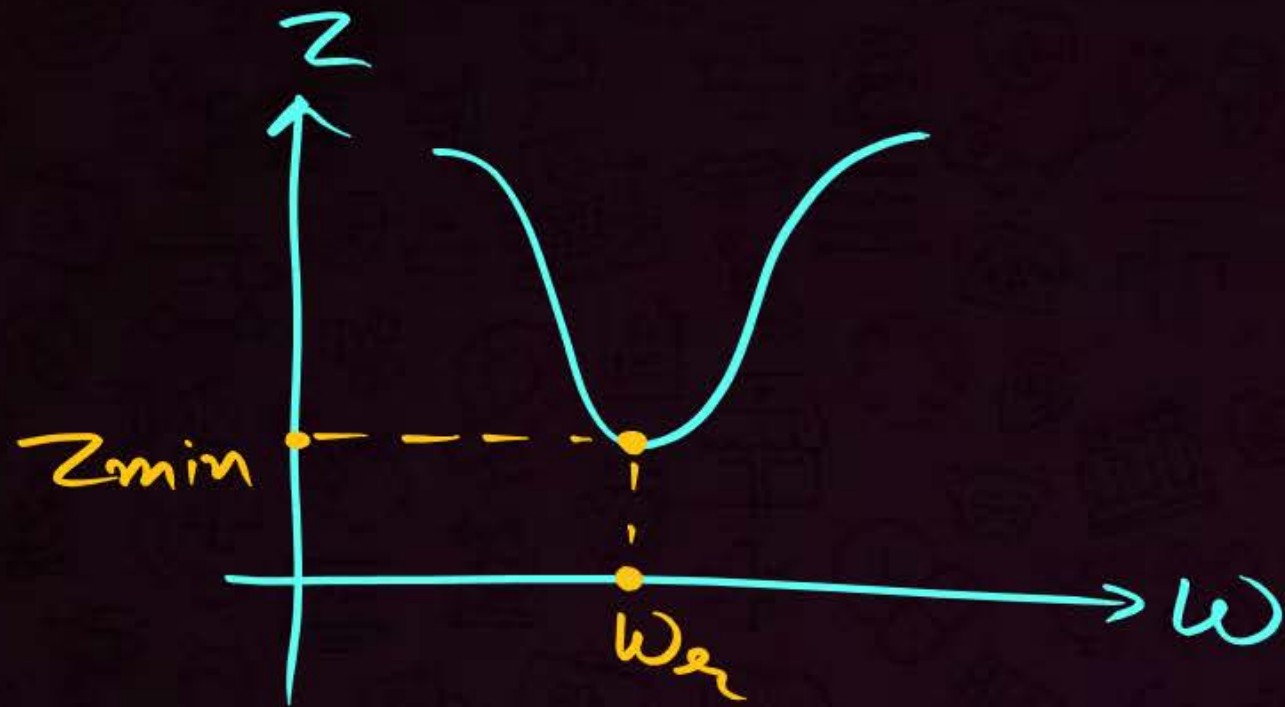
→ Resonance
angular
freq.

$$2\pi f_r = \frac{1}{\sqrt{LC}} \Rightarrow$$

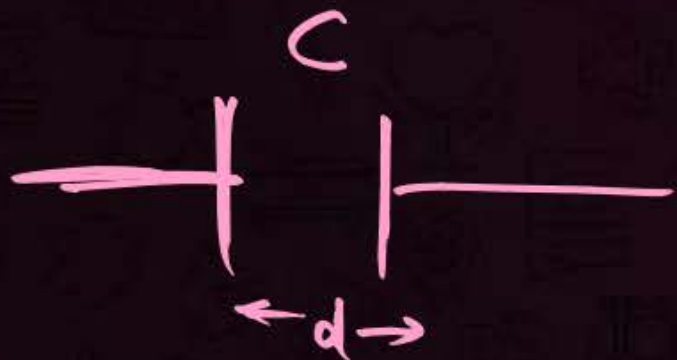
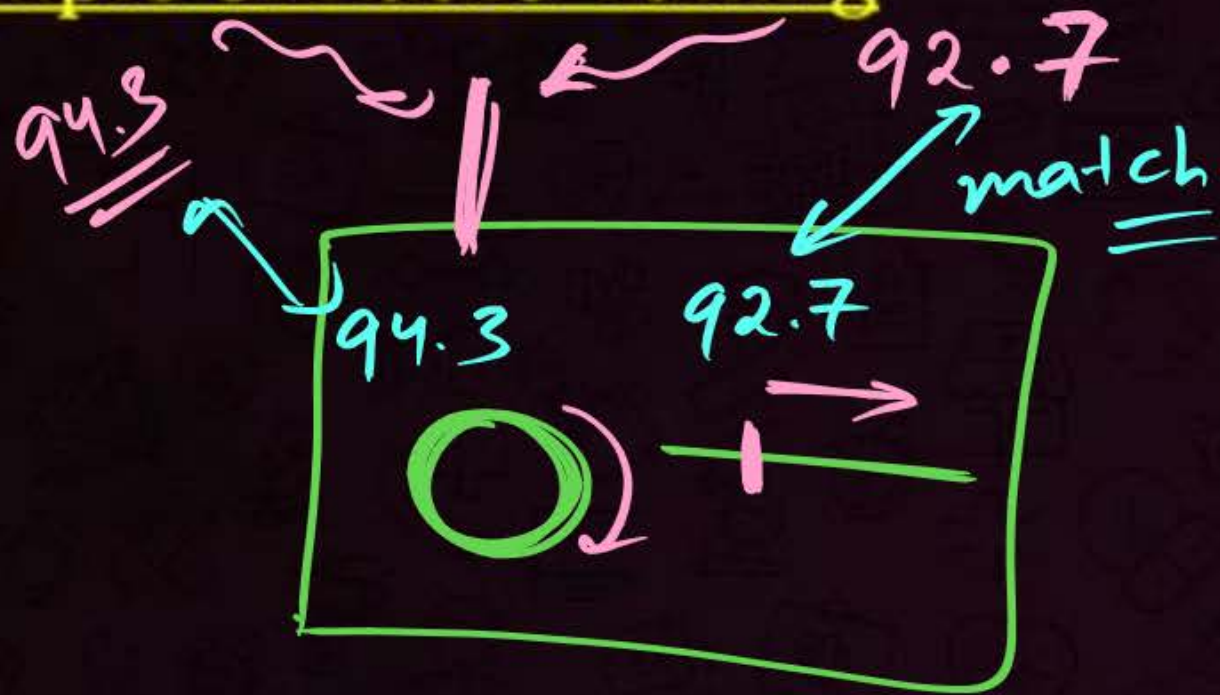
$$f_r = \frac{1}{2\pi\sqrt{LC}}$$

→ Resonance
freq.

Graph



Example of Radio Tuning



change \rightarrow C change

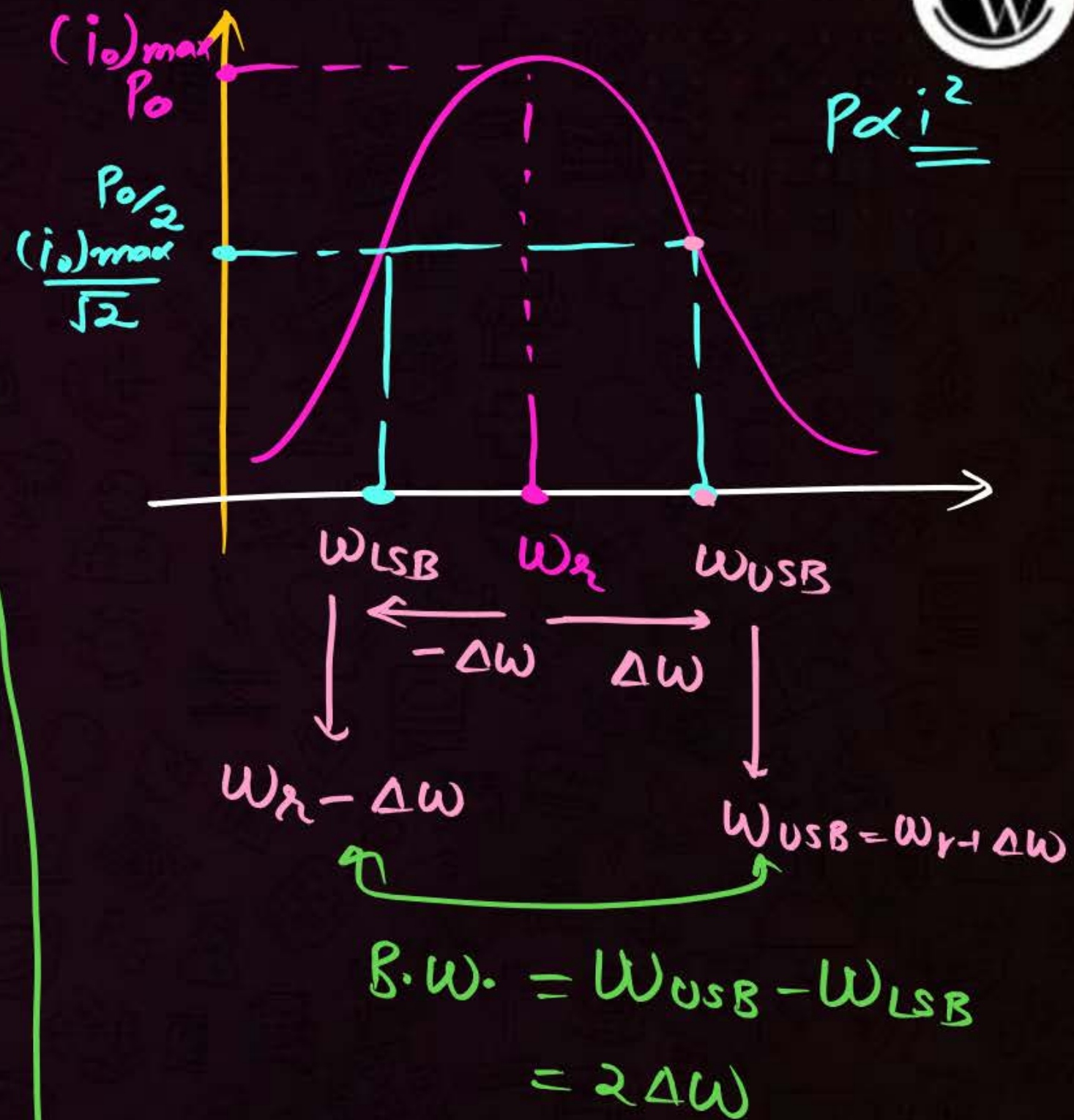
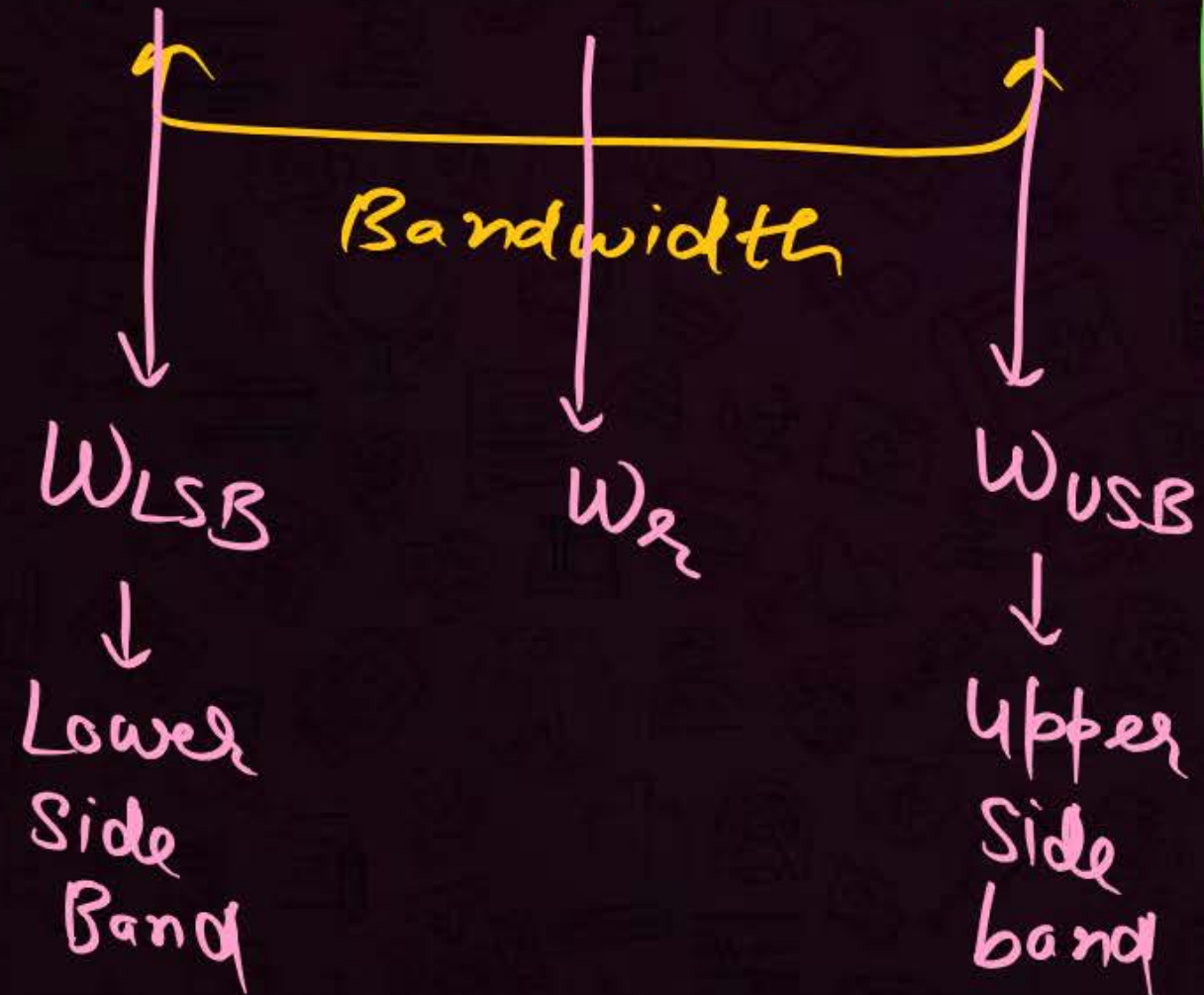
$\omega_r \rightarrow$ change

$$\omega_r = \frac{1}{\sqrt{LC}}$$

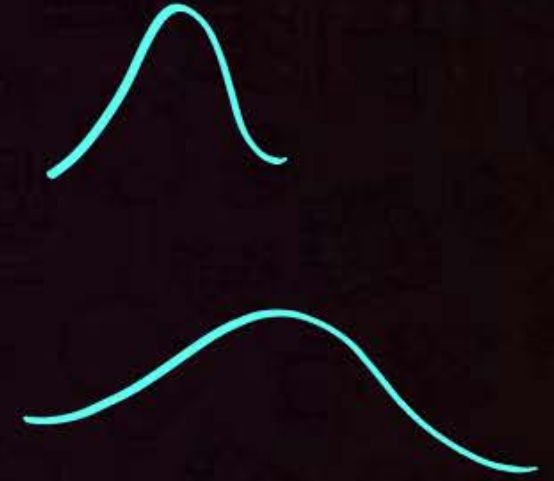
Bandwidth of a Circuit

eg: \div 92.7 MHz FM

eg: 92.5 — 92.7 — 92.9



Quality factor / Sharpness of a Circuit (Q)



$$Q = \boxed{\frac{\omega_r}{BW}} = \boxed{\frac{\omega_r}{2\Delta\omega}} = \frac{\omega_r}{R/L} = \boxed{\frac{\omega_r L}{R}} = \boxed{\frac{1}{R\omega_r C}} = \boxed{\frac{1}{R}\sqrt{\frac{L}{C}}}$$

$$B.W. = 2\Delta\omega = \frac{R}{L}$$

$$\text{Resonance} \Rightarrow X_L = X_C$$

$$\omega_r L = \frac{1}{\omega_r C}$$

QUESTION

In LCR circuit, the capacitance is changed from C to 4C. For the same resonant frequency, the inductance should be changed from L to

- 1 2L
- 2 L/2
- 3 ~~L/4~~
- 4 4L

$$\omega_r = \frac{1}{\sqrt{LC}}$$

same

~~L/4~~ → ~~4C~~

HW

What is the value of inductance L for which the current is maximum in a series LCR circuit with $C = 10 \mu\text{F}$ and $\omega = 1000 \text{ s}^{-1}$? (2007)

- 1 1 mH
- 2 cannot be calculated unless R is known
- 3 10 mH
- 4 100 mH.

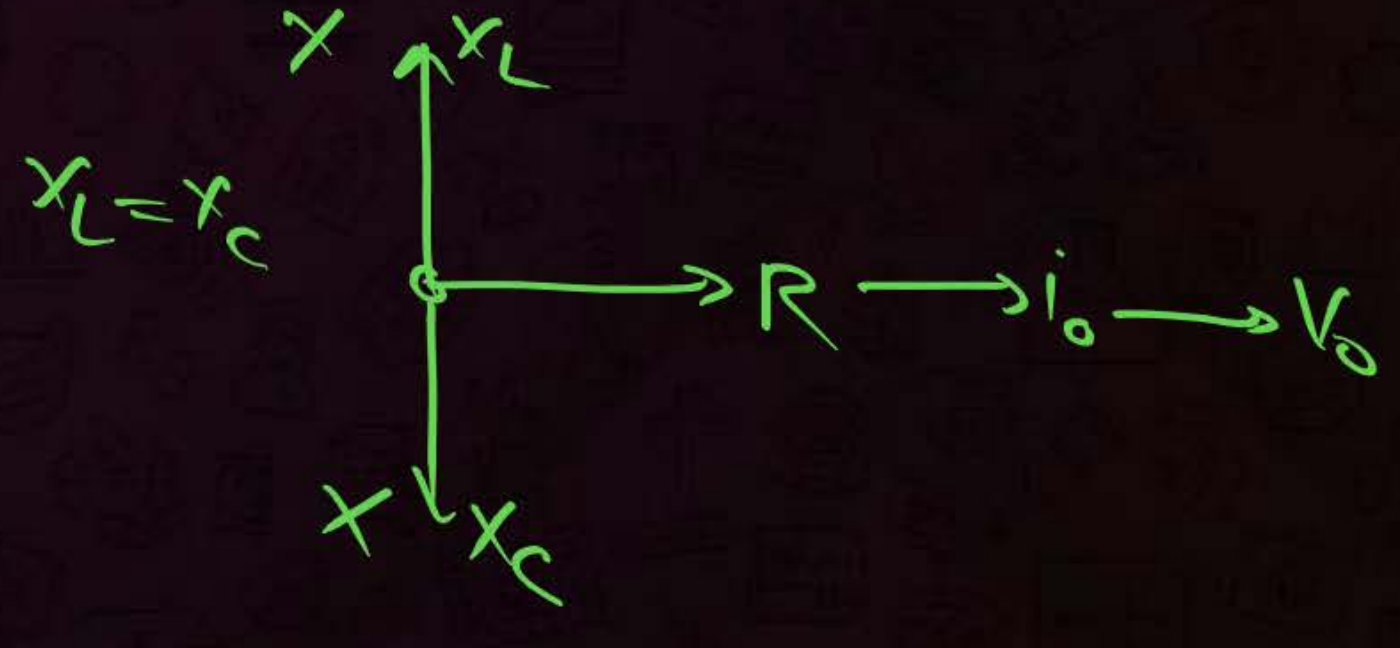
QUESTION



Assertion: At resonance, LCR series circuit have a minimum current.

Reason: At resonance, in LCR series circuit, the current and e.m.f are not in phase with each other. (AIIMS 2016)

- 1 Assertion (A) is True, Reason (R) is True; Reason (R) is a correct explanation for Assertion (A)
- 2 Assertion (A) is True, Reason (R) is True; Reason (R) is not a correct explanation for Assertion (A)
- 3 Assertion (A) is True, Reason (R) is False.
- 4 Assertion (A) is False, Reason (R) is ~~True~~.



QUESTION



The value of quality factor is

(2000)

1 $\omega L/C$ ✗

2 $1/\omega RC$ ✓

3 \sqrt{LC} ✗ $\Rightarrow \frac{1}{\sqrt{LC}}$ ✓

4 L/R ✗

QUESTION



A coil of inductance $8 \mu\text{H}$ is connected to a capacitor of capacitance $0.02 \mu\text{F}$. To what wavelength is this circuit tuned? (AIIMS 2015)

- 1 $9.54 \times 10^3 \text{ m}$
- 2 $4.12 \times 10^2 \text{ m}$
- 3 $15.90 \times 10^3 \text{ m}$
- 4 $7.54 \times 10^2 \text{ m}$

$$\omega_r = \frac{1}{\sqrt{LC}}$$
$$f_r = \frac{1}{2\pi\sqrt{LC}}$$

Light Wave

$$c = f\lambda$$
$$\lambda = \frac{c}{f}$$

QUESTION



$L\omega$

If L , C and R are the self inductance, capacitance and resistance respectively, which of the following does not have the dimension of time?

[27 June, 2022 (S-II)]

1 RC

2 L/R

3 \sqrt{LC}

4 L/C

QUESTION



In an ac circuit, an inductor, a capacitor and a resistor are connected in series with $X_L = R = X_C$. Impedance of this circuit is:

[31 Aug, 2021 (Shift-I)]

(JEE Mains)

1 $2R^2$

2 Zero

3 $R\sqrt{2}$

4 R

$$Z = \sqrt{(X_L - X_C)^2 + R^2}$$

$$= \sqrt{0^2 + R^2}$$

$$Z = R$$

QUESTION



HW

A series resonant LCR circuit has a quality factor (Q-factor) 0.4. If $R = 2 \text{ k}\Omega$, $C = 0.1 \text{ }\mu\text{F}$, then the value of inductance is **(AIIMS 2016)**

- 1 0.1 H
- 2 0.064 H
- 3 2 H
- 4 5 H

QUESTION



In the circuit shown below, the ac source has voltage $V = 20 \cos(\omega t)$ volts with $\omega = 2000$ rad/sec. the amplitude of the current will be

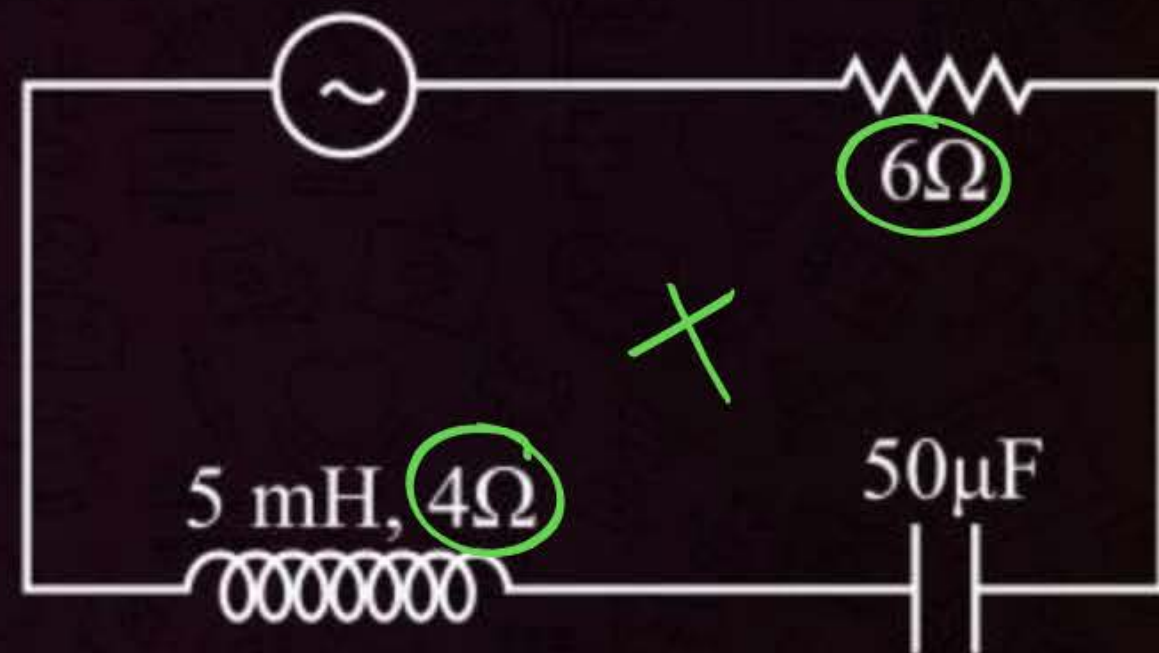
$$R = 4 + 6 = 10$$

- 1 2 A
- 2 3.3 A
- 3 $2/\sqrt{5}$ A
- 4 $\sqrt{5}$ A

$$\hat{i}_0 = \frac{V_0}{Z}$$

\searrow
 R

$$i_0 = \frac{V_0}{R} = \frac{20}{10} = 2$$



Resonance

$$X_L = \omega L = 5 \times 10^{-3} \times 2000 = 10\Omega$$

$$X_C = \frac{1}{\omega C} = \frac{1}{2000 \times 50 \times 10^{-6}} = 10\Omega$$

QUESTION

HW



In a series LCR circuit the voltage across resistance, capacitance and inductance is 10 V each. If the capacitance is short circuited, the voltage across the inductance will be

(AIIMS 2000)

- 1** $10/\sqrt{2}$ V
- 2** 10 V
- 3** $10\sqrt{2}$ V
- 4** 20 V

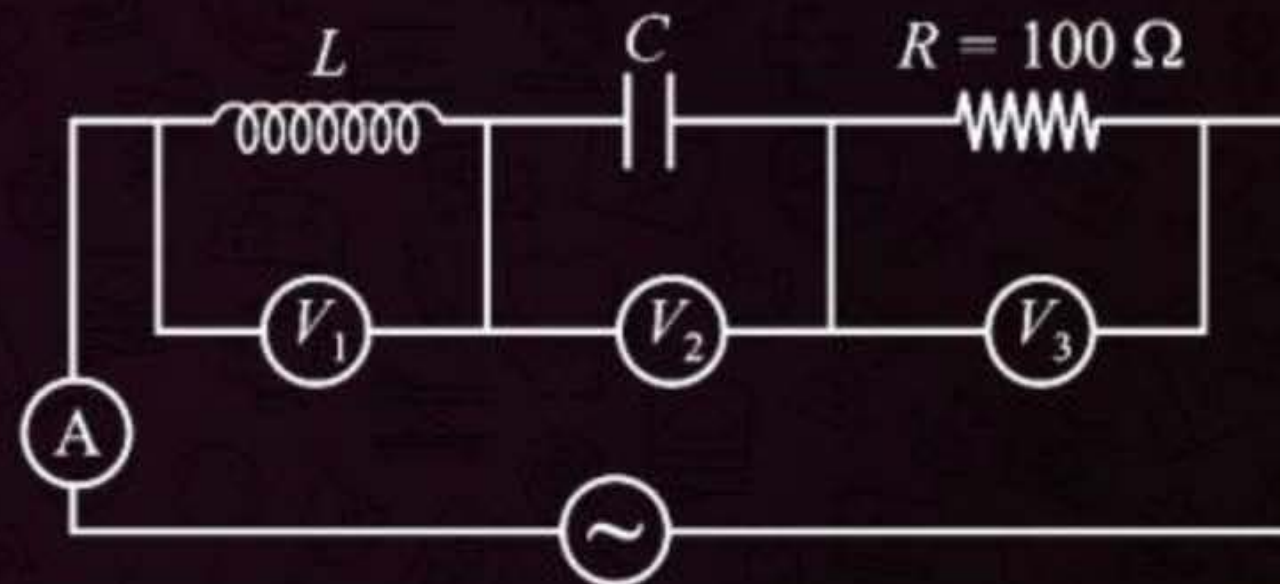
QUESTION

Hw



In the given circuit the reading of voltmeter V_1 and V_2 are 300 volts each. The reading of the voltmeter V_3 and ammeter A are respectively. The source voltage is 220 V, 50 Hz
(2010)

- 1 150 V, 2.2 A
- 2 200 V, 2.2 A
- 3 220 V, 2.2 A
- 4 100 V, 2.0 A



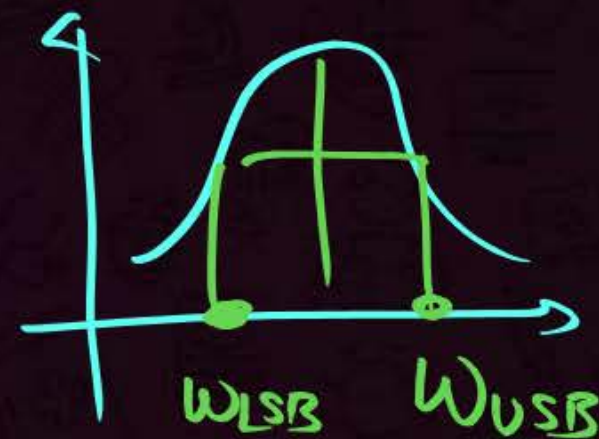
QUESTION



A series L-C-R circuit containing 5.0 H inductor, 80 μ F capacitor and 40 Ω resistor is connected to 230 V variable frequency AC source. The angular frequencies of the source at which power transferred to the circuit is half the power at the resonant angular frequency are likely to be

[NEET 2021]

- 1 25 rad/s and 75 rad/s
50
- 2 50 rad/s and 25 rad/s
25
- 3 46 rad/s and 54 rad/s
8
- 4 42 rad/s and 58 rad/s
16



$$\begin{aligned} BW &= \omega_{USB} - \omega_{LSB} = \frac{R}{L} \\ &= \frac{40}{5} = 8 \end{aligned}$$

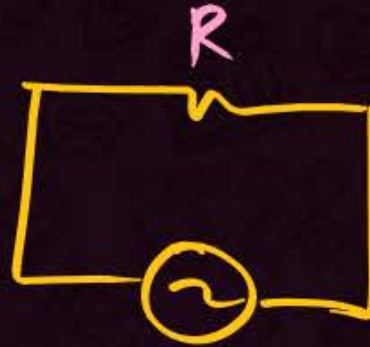


Choke Coil

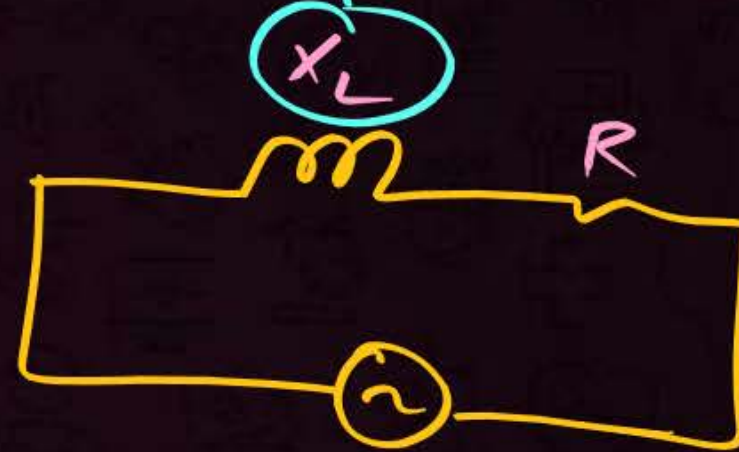
It is used to control the current in a circuit without dissipating any power or energy.

Inductor

Can be capacitor
also

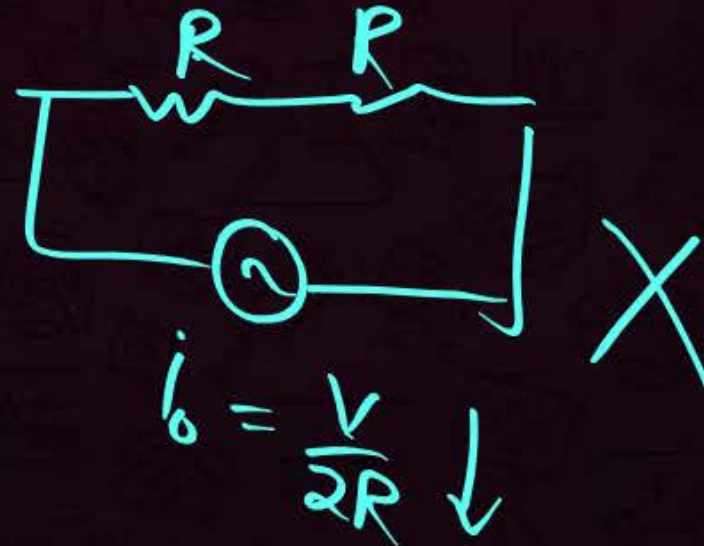


$$i_0 = \frac{V_0}{R}$$



$$i_0 = \frac{V_0}{\sqrt{X_L^2 + R^2}}$$

dec



$$i_0 = \frac{V}{2R}$$

QUESTION



Assertion: A capacitor of suitable capacitance can be used in an AC circuit in place of the choke coil.

Reason: A capacitor blocks DC and allows AC only.

(AIIMS 2019)

- 1 Assertion (A) is True, Reason (R) is True; Reason (R) is a correct explanation for Assertion (A)
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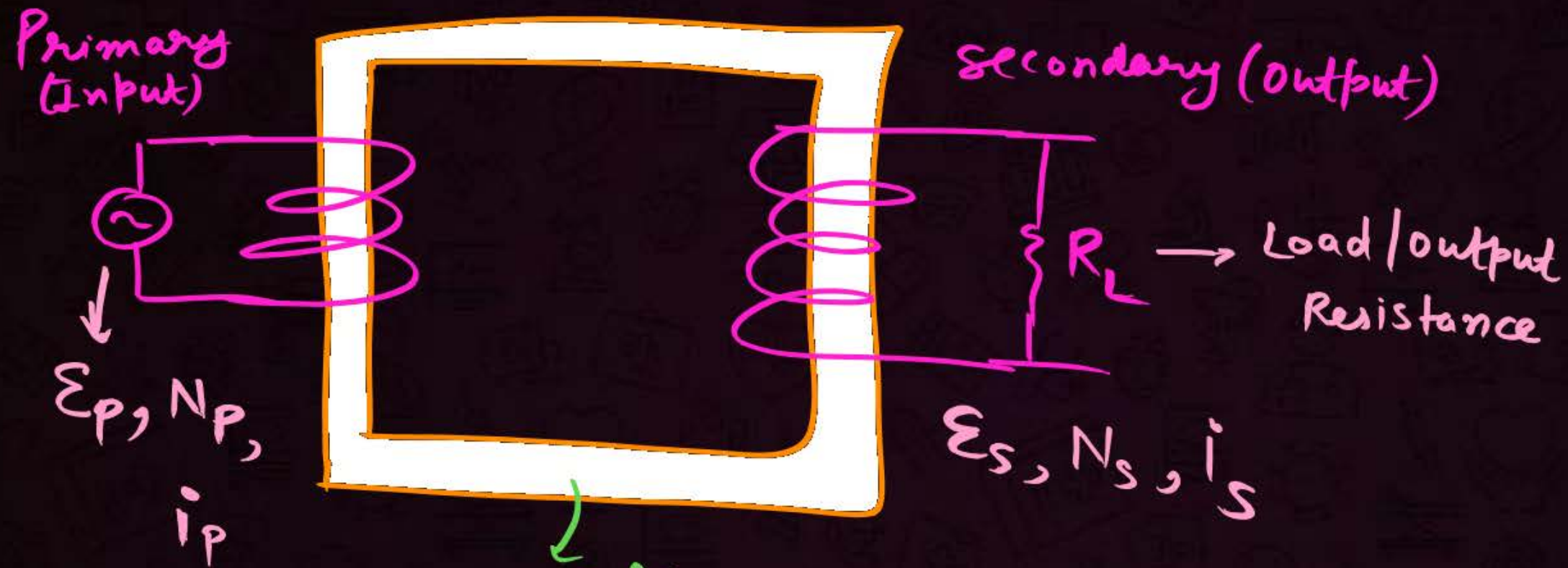
Transformer



To step up or step down the voltage.

Based on mutual inductance ^(EMI) between two coils. Whenever there is change in current in primary coil, there is emf induced in the secondary coil.

Construction and Working



Ideal Transformer

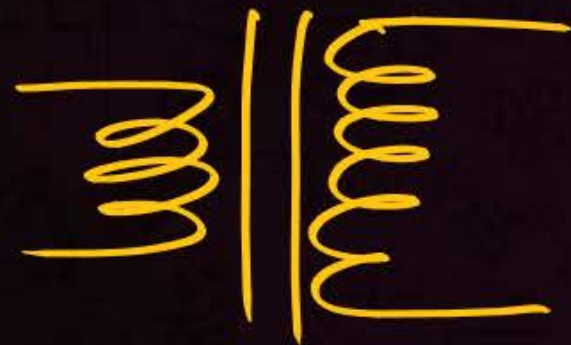
↓
No flux Loss

No Power Loss

★

$$\frac{E_P}{E_S} = \frac{N_P}{N_S} = \frac{i_S}{i_P}$$

a) Step-up Transformer

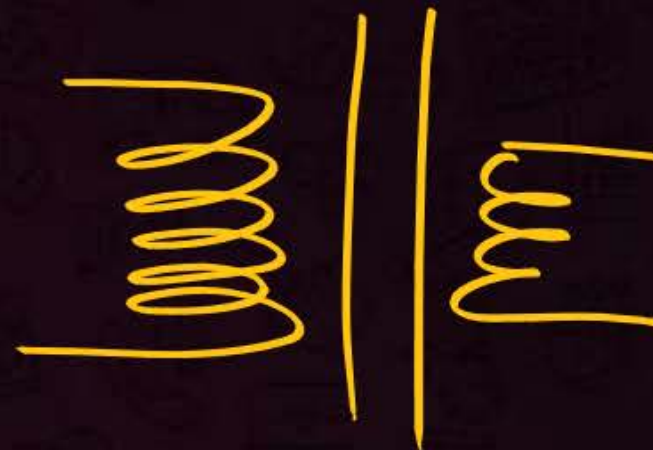


$$N_p < N_s$$

$$\varepsilon_p < \varepsilon_s \text{ (Up } \uparrow \text{)}$$

$$i_p > i_s$$

b) Step-down Transformer



$$N_p > N_s$$

$$\varepsilon_p > \varepsilon_s \text{ (Down } \downarrow \text{)}$$

$$i_p < i_s$$

Whatever we gain
in voltage, we lose in
current.

Non - Ideal Transformer



$$\hookrightarrow P_s \neq P_p$$

$$\hookrightarrow P_s < P_p$$

$$\eta = \frac{P_s}{P_p} \times 100 = \frac{\sum_s i_s}{\sum_p i_p} \times 100 \Rightarrow \text{efficiency}$$

QUESTION



A transformer works on the principle of

(AIIMS 1998)

1 mutual induction

2 inverter

3 convertor

4 self-induction.

QUESTION



Match the List-I with List-II. Choose the correct answer from the options given below:

[1 Feb, 2023 (S-I)]

- 1 A → IV, B → II, C → I, D → III
- 2 A → II, B → I, C → III, D → IV
- 3 A → II, B → IV, C → I, D → III
- 4 A → IV, B → III, C → I, D → II

List - I		List - II	
A	AC generator	i	Presence of both L and C $\frac{1}{\sqrt{LC}}$
B	Transformer	ii	Electromagnetic Induction
C	Resonance phenomenon to occur	iii	Quality factor
D	Sharpness of resonance	iv	Mutual Inductance

QUESTION



Which of the following quantity is increased in a step-down transformer? **(AIIMS 1999)**

- 1 Voltage
- 2 Current
- 3 Power
- 4 Frequency.

$V \downarrow$
 $i \uparrow$

QUESTION



The primary winding of a transformer has 500 turns whereas its secondary has 5000 turns. The primary is connected to an A.C. supply 20 V, 50 Hz. The secondary will have an output of

- 1 2 V, 50 Hz
- 2 2 V, 5 Hz
- ☒ 3 200 V, 50 Hz
- 4 200 V, 500 Hz

$$\frac{E_p}{E_s} = \frac{N_p}{N_s}$$

→ No change.

TBS

$$\frac{20}{E_s} = \frac{\cancel{500}}{\cancel{5000} / 10}$$

$$500 \xrightarrow{\times 10} 5000$$

$$20 \xrightarrow{\times 10} 200$$

$$E_s = 20 \times 10 = 200$$

QUESTION

HW



A step-up transformer operates on a 230 V line and supplies a load of 2 A. The ratio of primary and secondary windings is 1 : 25. Then the current in the primary is

- 1 25 A
- 2 50 A
- 3 15 A
- 4 12.5 A

QUESTION



Turn ratio in a step-up transformer is 1 : 2. If a Lechlanche cell of 1.5 V is connected across the input, what is the voltage across the output? ↑ DC
(AIIMS 2000)

- 1 1.5 V
- 2 0.0 V
- 3 3 V
- 4 0.75 V

Transformer → AC

→ DC X

$$e = 0$$

QUESTION

HW



An ideal transformer has 100 turns in the primary and 250 turns in the secondary. The peak value of the ac is 28 V. The r.m.s. secondary voltage is nearest to

- 1 50 V
- 2 70 V
- 3 100 V
- 4 40 V

HW

A transformer consisting of 300 turns in the primary and 150 turns in the secondary gives output power of 2.2 kW. If the current in the secondary coils is 10 A, then the input voltage and current in the primary coil are

[10 April, 2019 (Shift-I)]

1 220 V and 10 A

2 440 V and 5 A

3 440 V and 20 A

4 220 V and 20 A

QUESTION



The primary and secondary coils of a transformer have 50 and 1500 turns respectively. If the magnetic flux ϕ linked with the primary coil is given by $\phi = \phi_0 + 4t$, where ϕ is in webers t is time in seconds and ϕ_0 is a constant, the output voltage across the secondary coil is

$$N_p = 50$$

$$N_s = 1500$$

$$\mathcal{E}_p = -\frac{d\phi}{dt} = -(0 + 4) = -4\text{V}$$

$$\mathcal{E}_s = ?$$

$$\frac{\mathcal{E}_s}{\mathcal{E}_p} = \frac{N_s}{N_p}$$

$$\begin{array}{ccc} & \xrightarrow{\times 30} & \\ 50 & \longrightarrow & 1500 \\ 4\text{V} & \longrightarrow & 120 \\ & \xleftarrow{\times 30} & \end{array}$$

1 90 volt

2 120 volt

3 220 volt

4 30 volt

QUESTION



A transformer is employed to reduce 220 V to 11 V. The primary draws a current of 5 A and the secondary 90 A. The efficiency of the transformer is

- 1 20%
- 2 40%
- 3 70%
- ☒ 4 90%

$$\begin{aligned}
 \eta &= \frac{\epsilon_s i_s}{\epsilon_p i_p} \times 100 \\
 &= \frac{11 \times 90}{220 \times 5} \times 100 \\
 &= \frac{99}{110} \times 100 = \frac{990}{11} \\
 &= 90\%
 \end{aligned}$$

Non-ideal

$$\frac{\epsilon_p}{\epsilon_s} = \frac{N_p}{N_s} \neq \frac{i_s}{i_p}$$

$$\frac{V_p}{V_s} \neq \frac{i_s}{i_p}$$

QUESTION

HW



A transformer is used to light 100 W – 110 V lamp from 220 V mains. If the main current is 0.5 A, the efficiency of the transformer is approximately

1 50%

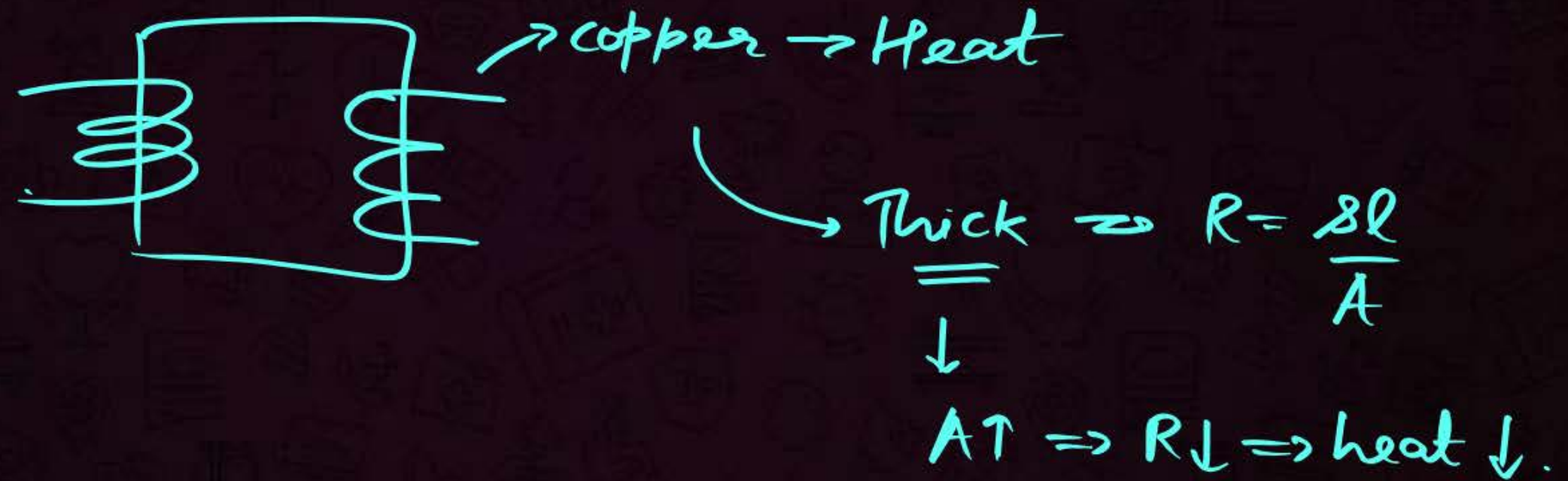
2 90%

3 10%

4 30%

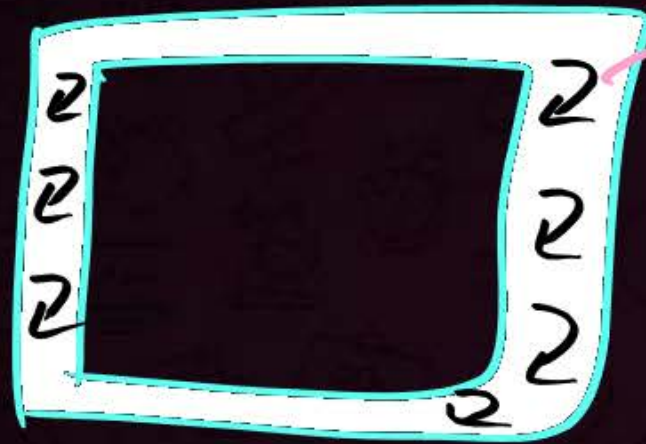
Losses in Transformer:

1. Copper Loss: Due to resistance of the windings, the heat is produced. To reduce it, we use thick wires.

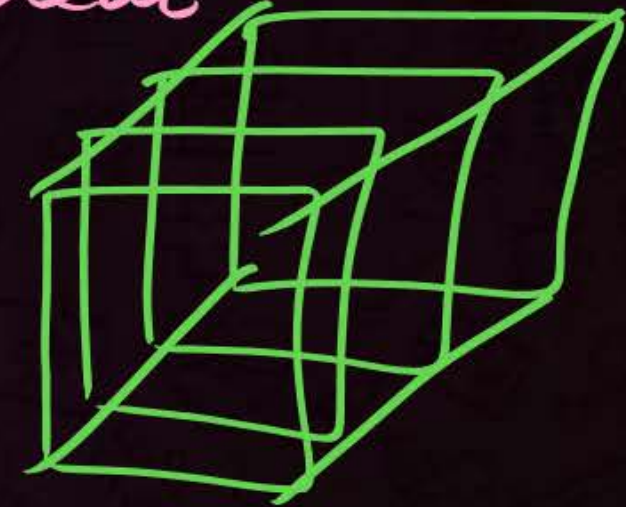
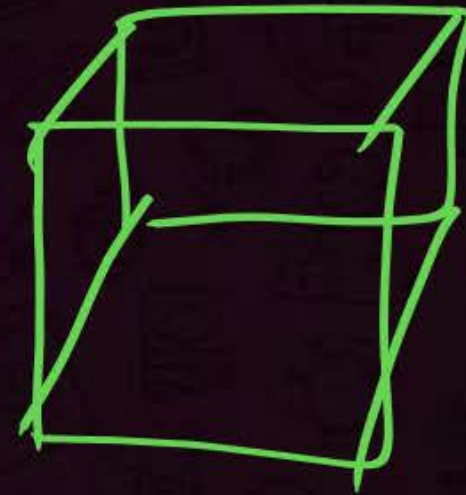


2. **Iron Losses:** Due to eddy currents being produced in the soft iron core, heat is produced. To reduce it we, use laminated core.

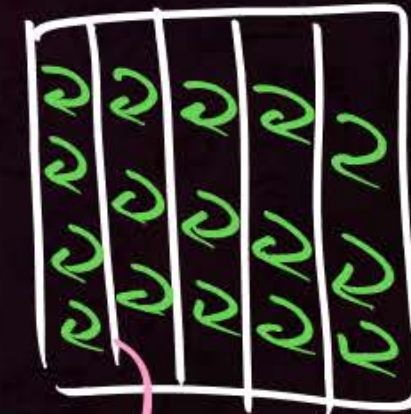
(sheet/slice)



Eddy current \rightarrow heat

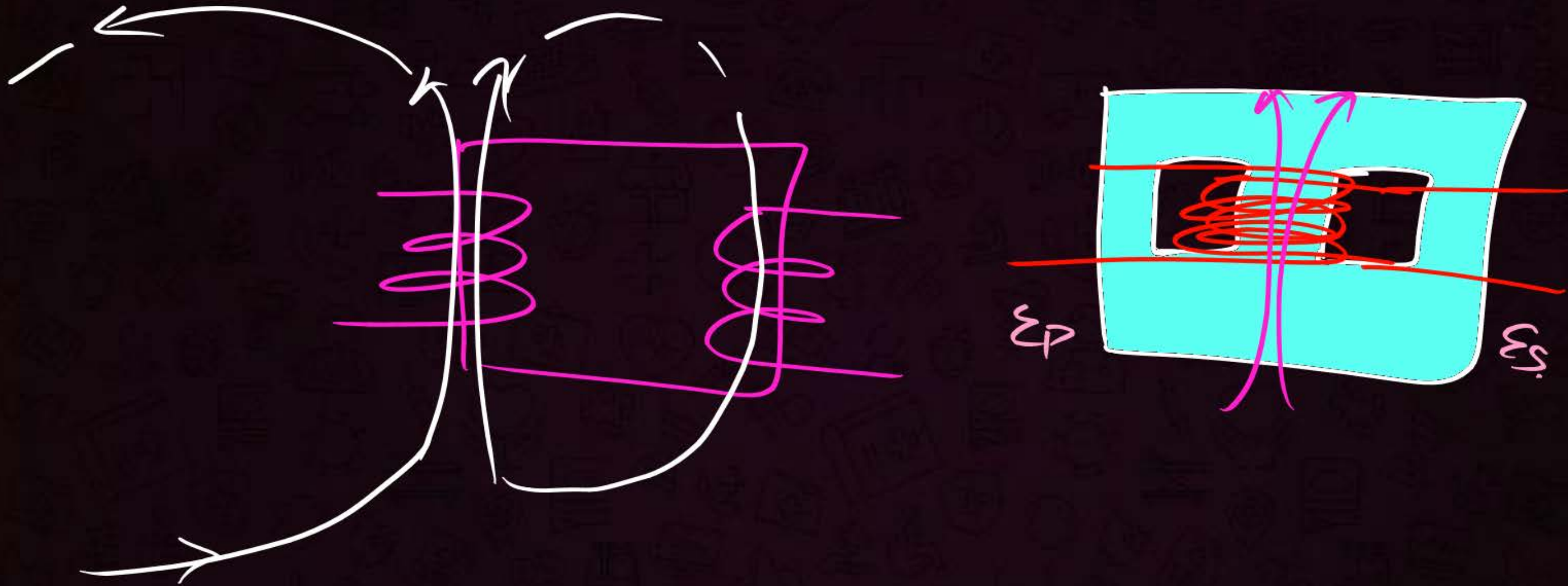


Side-View

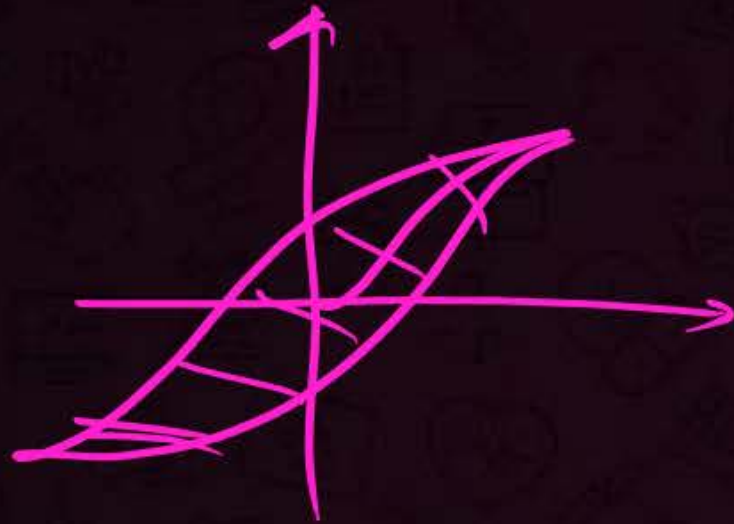


Lacquer (insulating power)

3. **Flux Loss:** To reduce it, we mount both coils on a single vertical pole.



4. **Hysteresis Loss**: Due to repeated magnetization and de - magnetization, there will be magnetic fatigue. There will be more energy losses.



5. **Magneto - striction**: Due to humming noise of the transformer.

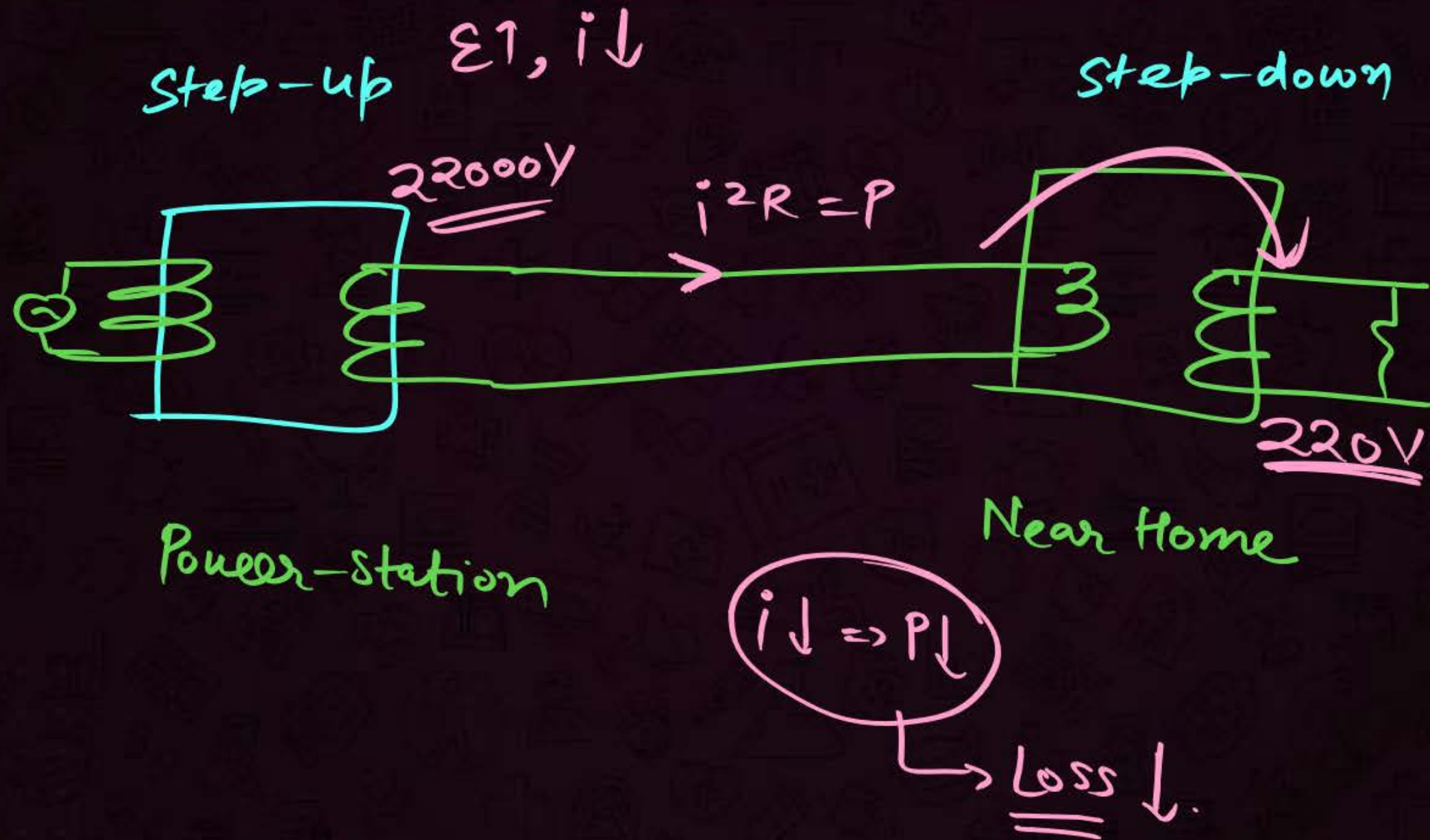
Assertion: We use a thick wire in the secondary coil of a step-down transformer to reduce the production of heat.

Reason: Eddy currents can be reduced by using laminated cores.

- 1 Assertion (A) is True, Reason (R) is True; Reason (R) is a correct explanation for Assertion (A)
- 2 ☒ Assertion (A) is True, Reason (R) is True; Reason (R) is not a correct explanation for Assertion (A)
- 3 Assertion (A) is True, Reason (R) is False.
- 4 Assertion (A) is False, Reason (R) is True.



Long Distance Power Transmission





LC Oscillations

Syllabus ✗

Risk cover ✓

$$W = \frac{1}{\sqrt{LC}}$$



$(10J)$
C ✓

$(6C + 4J)$

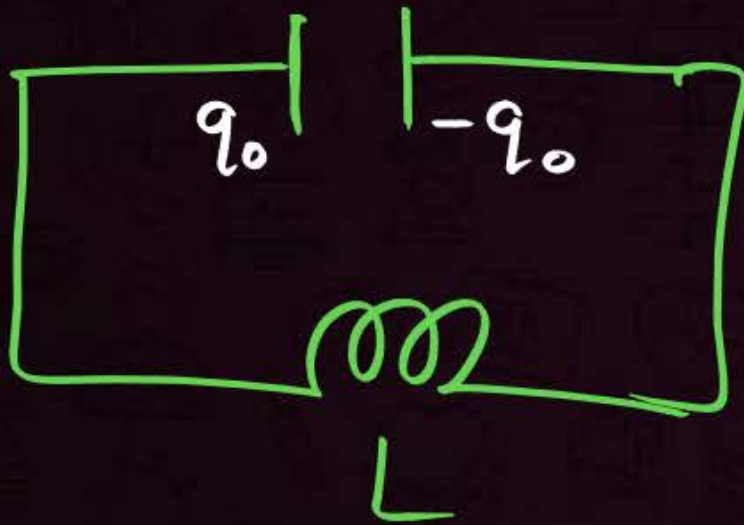
$(10J)$

JEE Mains

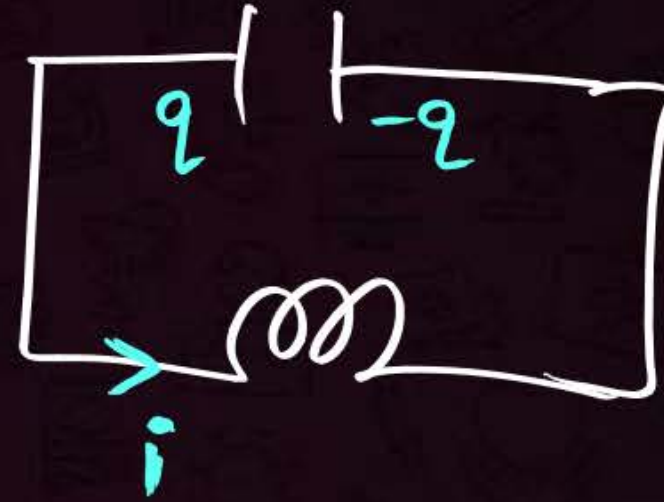
$k \rightarrow \frac{1}{C}$
$m \rightarrow L$

inertia

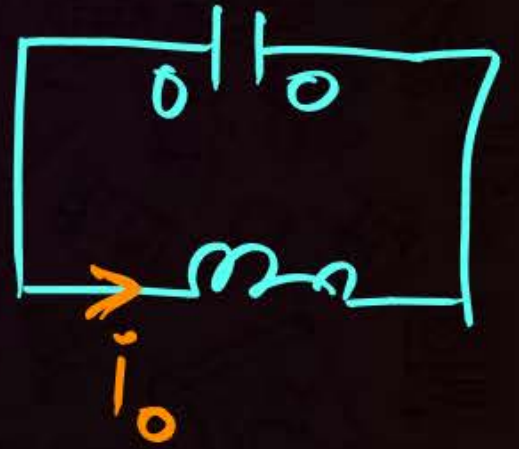
electrical inertia



\Rightarrow



\Rightarrow



$q_0 \rightarrow \text{max}^m \text{ charge}$

Still $\rightarrow \frac{1}{2} kx^2 + \frac{1}{2} mv^2$

$$\frac{q^2}{2C} + \frac{1}{2} Li^2$$

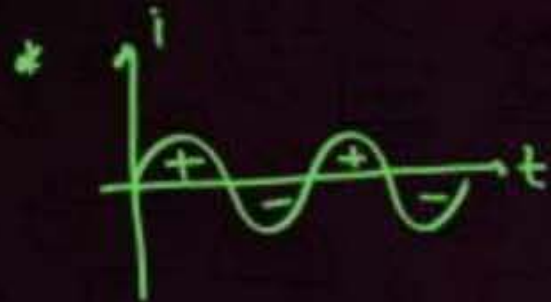
$$E = \frac{q^2}{2C} + \frac{1}{2} Li^2 = \frac{q_0^2}{2C} = \frac{1}{2} Li_0^2$$

$i_0 \rightarrow \text{max}^m$

conserved

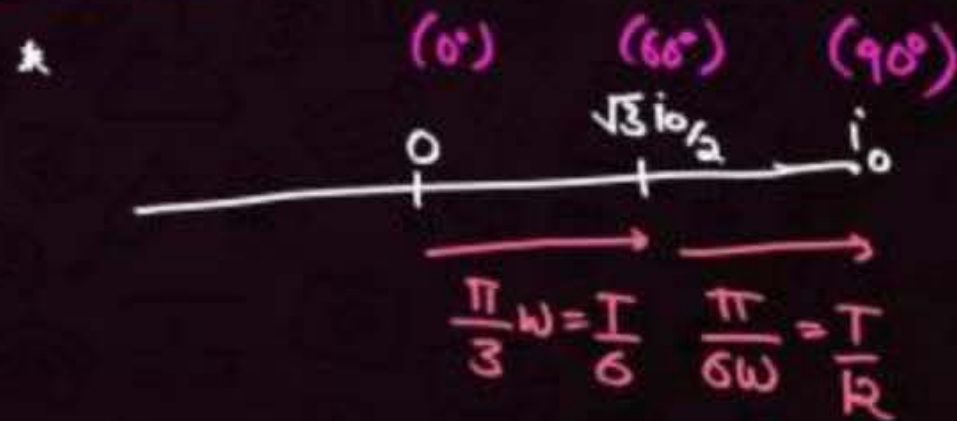
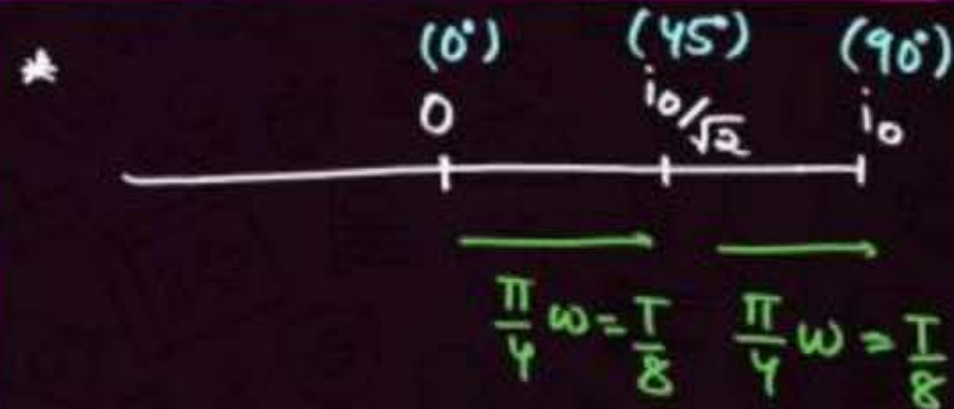
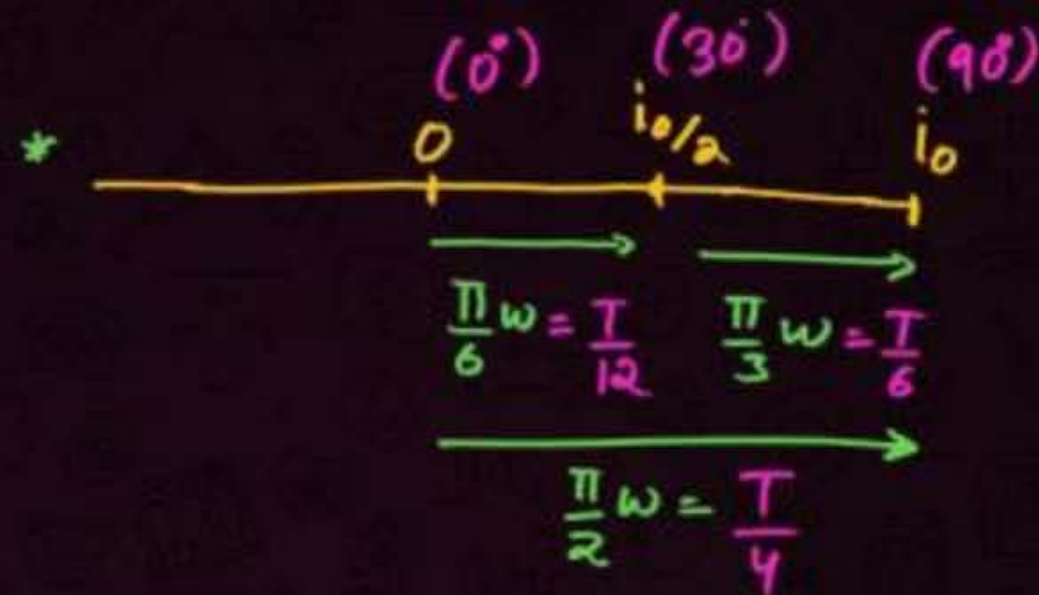
TBS capsule ①

- * AC → changes its value after regular interval.



Home supply → sinusoidal AC

- * $i = i_0 \sin \omega t$, $V = V_0 \sin \omega t$
- India → $f = 50 \text{ Hz}$
- Current changes direction 2 times every cycle.



TBS Capsule (2)

* $i_{av} = \frac{\text{Total Charge Flow}}{\text{Total time}}$
(Mean)

* Total charge

• $i \times t \rightarrow$ if $i = \text{const.}$

• $\int i dt \Rightarrow$ if $i = \text{variable}$

• Area under $i-t$ graph

• $i_{av} = \langle i \rangle = \frac{\int i dt}{\int dt}$

* $i_{rms} = \sqrt{\frac{\int i^2 dt}{\int dt}} = \sqrt{\langle i^2 \rangle}$

* virtual or effective current

* Meaning

$$i_{rms} = \sqrt{\frac{i_1^2 + i_2^2 + \dots + i_n^2}{n}}$$

* $i_{av} \rightarrow$ Based on charge flow.

* $i_{rms} \rightarrow$ Based on heat generated

* Home Supply $\rightarrow i = i_0 \sin \omega t$

Full Cycle $\Rightarrow i_{av} = 0, i_{rms} = \frac{i_0}{\sqrt{2}}$
(0 to T)

• Half cycle
(0 to $T/2$)

$$i_{av} = \frac{2i_0}{\pi} = 0.637 i_0$$

$$i_{rms} = \frac{i_0}{\sqrt{2}} = 0.707 i_0$$

* Form Factor

$$\hookrightarrow \frac{i_{rms}}{i_{av}} = 1.11$$

* Rms & average values valid for voltages as well.

* Full cycle

$$\begin{aligned} \bullet & \langle \sin \omega t \rangle = \langle \cos \omega t \rangle \\ & = \langle \sin 2\omega t \rangle = \langle \cos 2\omega t \rangle = 0 \end{aligned}$$

* Half cycle

$$\langle \sin \omega t \rangle = \frac{2}{\pi}$$

$$\bullet \langle \sin^2 \omega t \rangle = \langle \cos^2 \omega t \rangle = \frac{1}{2}$$

(TBS)

$$\bullet i = a + b \sin \omega t$$

$$i_{rms} = \sqrt{a^2 + \frac{b^2}{2}}$$

$$\bullet i = a \sin \omega t + b \cos \omega t$$

$$i_{rms} = \sqrt{\frac{a^2 + b^2}{2}}$$

* Normal ammeter \rightarrow DC measure ✓
AC measure ✗

* AC (Hot wire) Ammeter \rightarrow AC & DC both measure.

\rightarrow Based on heat \Rightarrow Non-Linear scale
 $(H \propto i^2)$

* $V_{rms} = 220 \text{ V}$ (Home supply)

* If nothing mentioned, assume rms value.

TBS Capsule ③

* Purely resistive

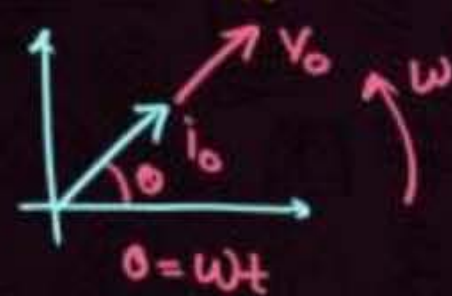
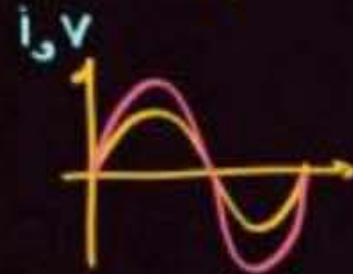


$$V = V_0 \sin \omega t$$

$$i = i_0 \sin \omega t$$

• Same phase

$$i_0 = \frac{V_0}{R} \quad \& \quad i_{rms} = \frac{V_{rms}}{R}$$



$$P = V_0 i_0 \sin^2 \omega t$$

$$P_{av} = \frac{V_0 i_0}{2}$$

$$= V_{rms} i_{rms}$$

$$= i_{rms}^2 R = \frac{V_{rms}^2}{R}$$

* Purely Inductive



$$V = V_0 \sin \omega t$$

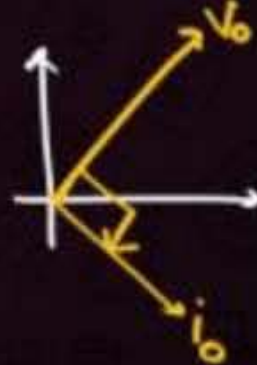
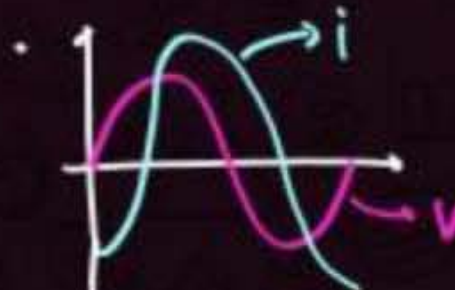
$$i = i_0 \sin \left(\omega t - \frac{\pi}{2} \right)$$

$$= -i_0 \cos \omega t$$

• V leads, i lags by 90°

$$i_0 = \frac{V_0}{X_L}, \quad i_{rms} = \frac{V_{rms}}{X_L}$$

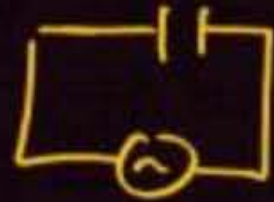
$$X_L = \omega L = 2\pi f L$$



$$P = -\frac{V_0 i_0}{2} \sin 2\omega t$$

• $P_{av} = 0$ \rightarrow Full Cycle
 \rightarrow Half Cycle

* Purely capacitive



$$V = V_0 \sin \omega t$$

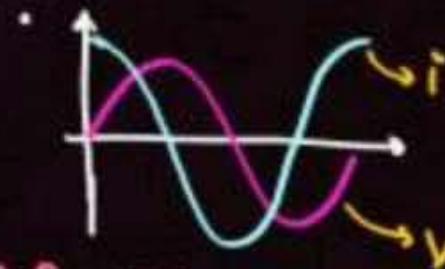
$$i = i_0 \sin \left(\omega t + \frac{\pi}{2} \right)$$

$$i = i_0 \cos \omega t$$

• V lags, i leads by 90°

$$i_0 = \frac{V_0}{X_C}, \quad i_{rms} = \frac{V_{rms}}{X_C}$$

$$X_C = \frac{1}{\omega C} = \frac{1}{2\pi f C}$$



$$P = \frac{V_0 i_0}{2} \sin \omega t$$

$P_{av} = 0$
 Full / Half Cycle

* Purely C & Purely L circuits have wattless currents.

• Units of X_L, X_C & R are ohm (Ω)

• Capacitor

Blocks DC

DC $\rightarrow f = 0$
 $X_C \rightarrow \infty$

High f AC $\rightarrow f \rightarrow \infty$
 $X_C \rightarrow 0$

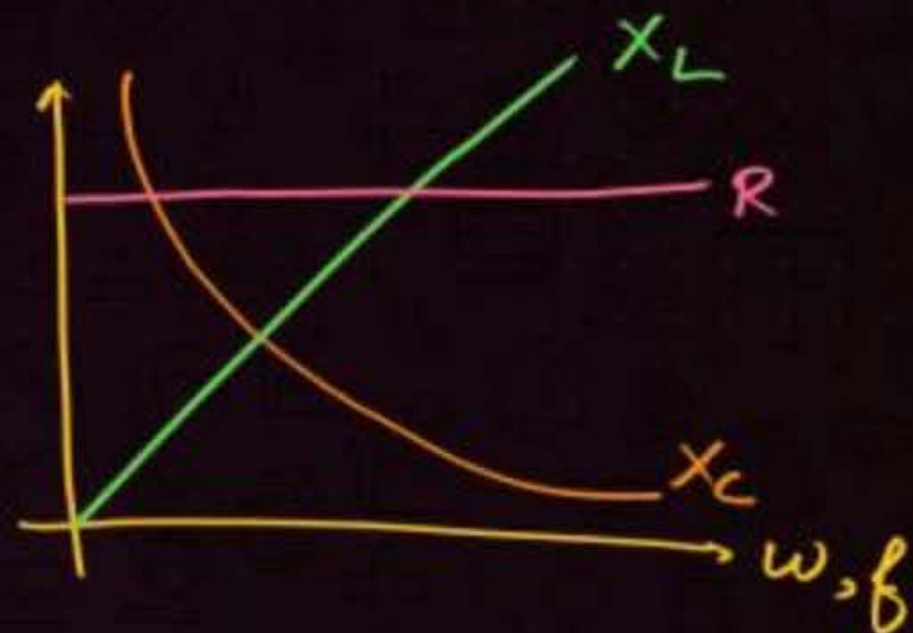
High pass filter

Inductor

DC $\rightarrow X_L \rightarrow 0$

High f AC \rightarrow Blocks AC
 $X_L \rightarrow \infty$

Low pass filter

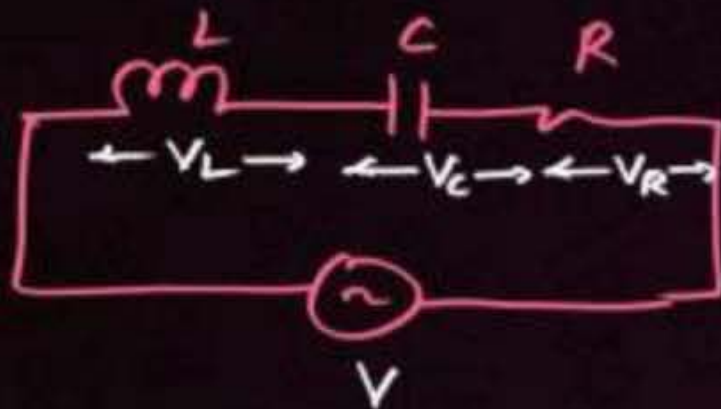


* $X_C \propto \frac{1}{\omega} \propto \frac{1}{f}$

* $X_L \propto \omega \propto f$

* $R \rightarrow$ independent of ω & f

TBS capsule (4)



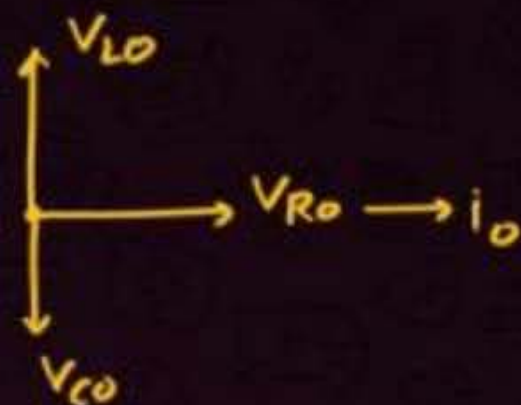
* series \rightarrow i same.

$$i = i_0 \sin \omega t$$

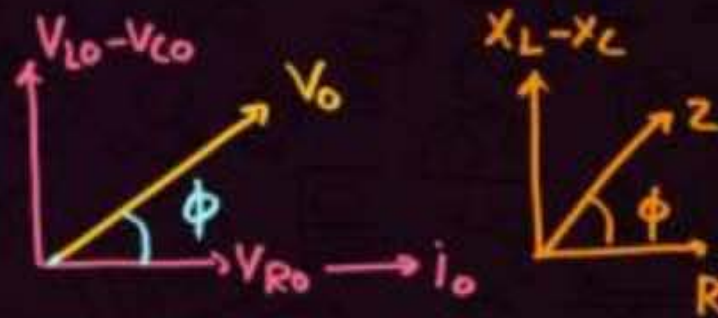
* $V_L + V_C + V_R = V$ ✓

* $V_{L0} + V_{C0} + V_{R0} = V_0$ ✗

* $\vec{V}_{L0} + \vec{V}_{C0} + \vec{V}_{R0} = \vec{V}_0$ ✓



a) L dominated ($X_L > X_C$)

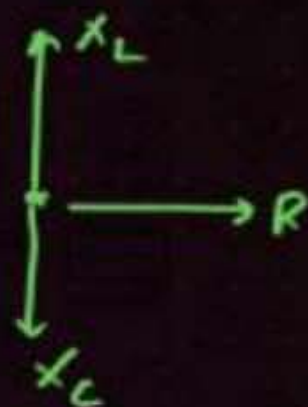


$$V_0 = \sqrt{(V_{L0} - V_{C0})^2 + V_{R0}^2}$$

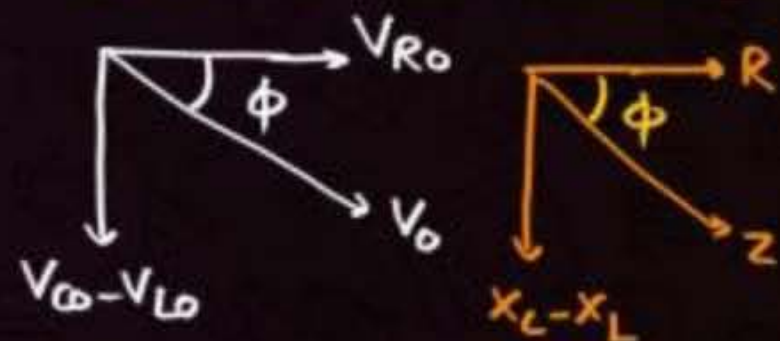
$$V = V_0 \sin(\omega t + \phi)$$

• $\tan \phi = \frac{V_{L0} - V_{C0}}{V_{R0}} = \frac{X_L - X_C}{R}$

• V leads



b) C dominated ($X_L < X_C$)



$$V_0 = \sqrt{(V_{C0} - V_{L0})^2 + V_{R0}^2}$$

$$V = V_0 \sin(\omega t - \phi)$$

• $\tan \phi = \frac{V_{C0} - V_{L0}}{V_{R0}} = \frac{X_C - X_L}{R}$

• V lags

$$* Z = \sqrt{(X_L - X_C)^2 + R^2}$$

$$* i_o = \frac{V_o}{Z}, \quad i_{rms} = \frac{V_{rms}}{Z}$$

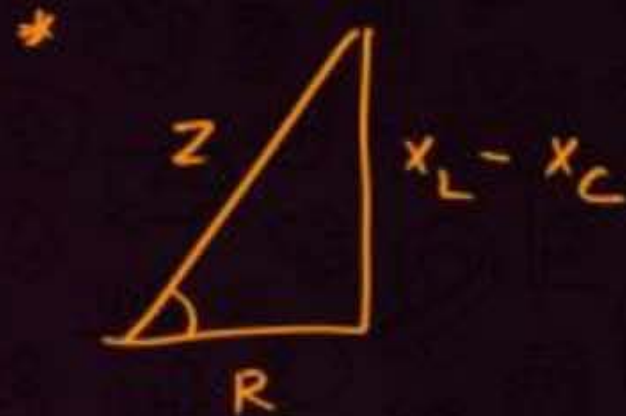
$$* \begin{aligned} P_{av} &= \frac{V_o i_o}{2} \cos \phi \\ P_{av} &= \frac{V_{rms} i_{rms}}{2} \cos \phi \end{aligned}$$

True
power

app. power

power
factor

$$* \cos \phi = \frac{R}{Z} \rightarrow \frac{V_{R0}}{V_o}$$



Impedance Δ .

$$\cdot i_{wattless} = i_{rms} \sin \phi$$

• Phasor diagram \rightarrow also valid
for rms values.

TBS Capsule ⑤

* Resonance $\rightarrow i_o \rightarrow \max$
 $Z \rightarrow \min$

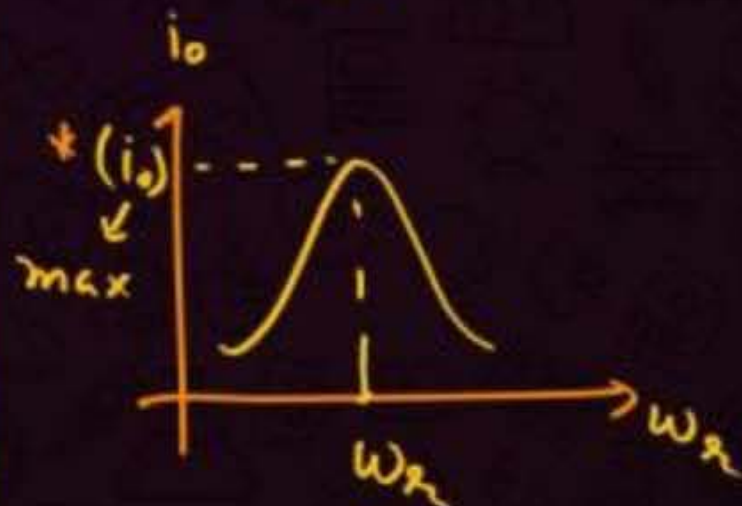
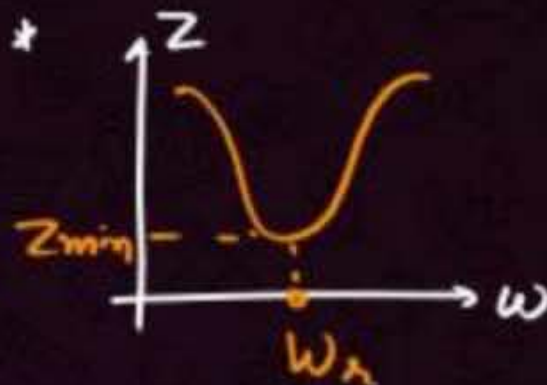
\downarrow
 $X_L = X_C \Rightarrow \omega_r = \frac{1}{\sqrt{LC}}$

$$f_r = \frac{1}{2\pi\sqrt{LC}}$$

* $Z_{\min} = R$

* $(i_o)_{\max} = \frac{V_o}{R}$

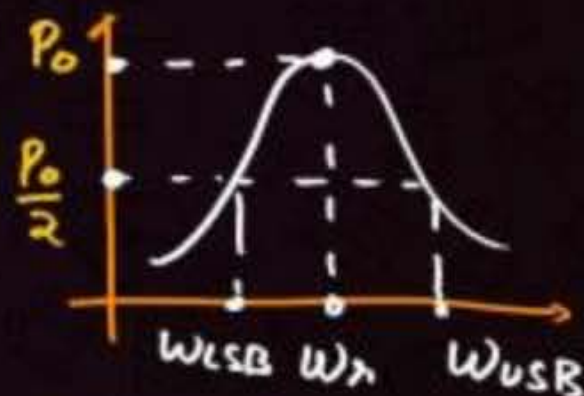
* $f \rightarrow$ matching at resonance.



* Bandwidth (B.W.)

$$= \omega_{USB} - \omega_{LSB}$$

$$= 2\Delta\omega = \frac{R}{L}$$



$$P_o \rightarrow \frac{P_o}{2}$$

$$(i_o)_{\max} \rightarrow \frac{(i_o)_{\max}}{\sqrt{2}}$$

$$* Q = \frac{\omega_r}{2\Delta\omega} = \frac{\omega_r L}{R} = \frac{1}{R\omega_r C} = \frac{1}{R} \sqrt{\frac{L}{C}}$$

TBS capsule ⑥

* Transformer \rightarrow mutual inductance

$$\boxed{\frac{\mathcal{E}_p}{\mathcal{E}_s} = \frac{N_p}{N_s} = \frac{I_s}{I_p}} \rightarrow \text{ideal}$$

• step-up

$$\mathcal{E}_s > \mathcal{E}_p$$



$$I_s < I_p$$

step-down

$$\mathcal{E}_s < \mathcal{E}_p$$



$$I_s > I_p$$

* Non-ideal $\rightarrow P_s < P_p$

$$\eta = \frac{P_s}{P_p} \times 100 = \frac{\mathcal{E}_s I_s}{\mathcal{E}_p I_p} \times 100 \quad \frac{\mathcal{E}_p}{\mathcal{E}_s} = \frac{N_p}{N_s} \neq \frac{I_s}{I_p}$$

* Losses : ① Copper loss \rightarrow due to R of wires.
Use thick wires

② Iron loss \rightarrow Eddy currents
Use laminated core, lacquer.

③ Flux loss \rightarrow single pole mounting

④ Hysteresis \rightarrow Repeated use

⑤ Magnetostriction \rightarrow Humming Noise

* Long Distance $\Rightarrow V \uparrow \Rightarrow I \downarrow \Rightarrow$ so that power loss ($i^2 R$) is less.

TBS capsule ⑦

* choke-coil $\Rightarrow X_L$ (inductor)

reduces i without
power loss.

• Capacitor can also be
used.

* LC Oscillations (Extra)



$$E = \frac{q^2}{2C} + \frac{1}{2} Li^2$$

$$E = \frac{1}{2} kx^2 + \frac{1}{2} mv^2$$

$$k \rightarrow \frac{1}{C} \quad \cdot \quad m \rightarrow L$$

• Total energy constant.

$$E = \frac{q_0^2}{2C} = \frac{1}{2} Li_0^2$$

$$\omega = \frac{1}{\sqrt{LC}}$$

TBS Army – Tanuj Sir

TANUJ SIR

JOIN MY OFFICIAL TELEGRAM CHANNEL

Physics Wallah





Homework

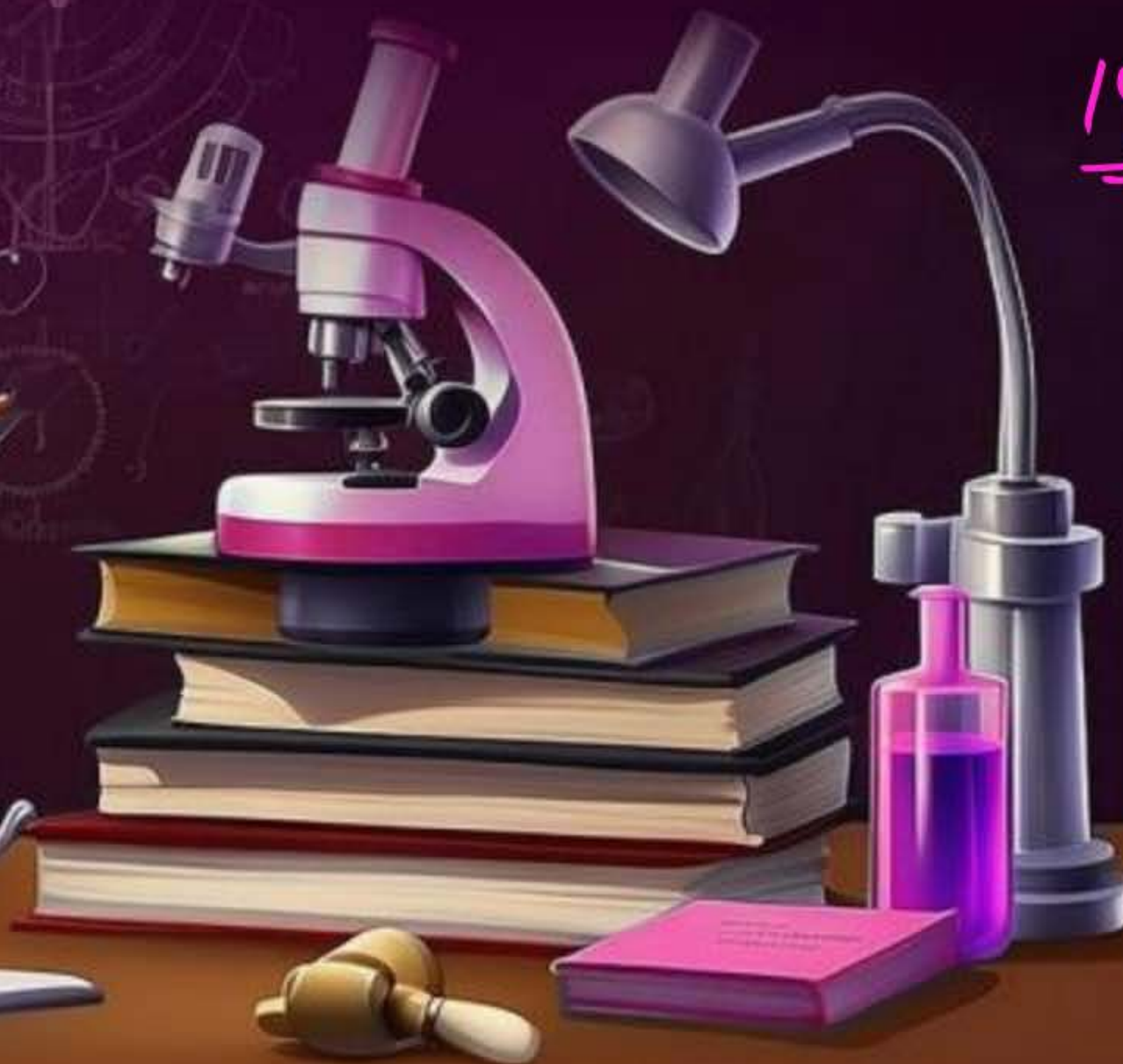
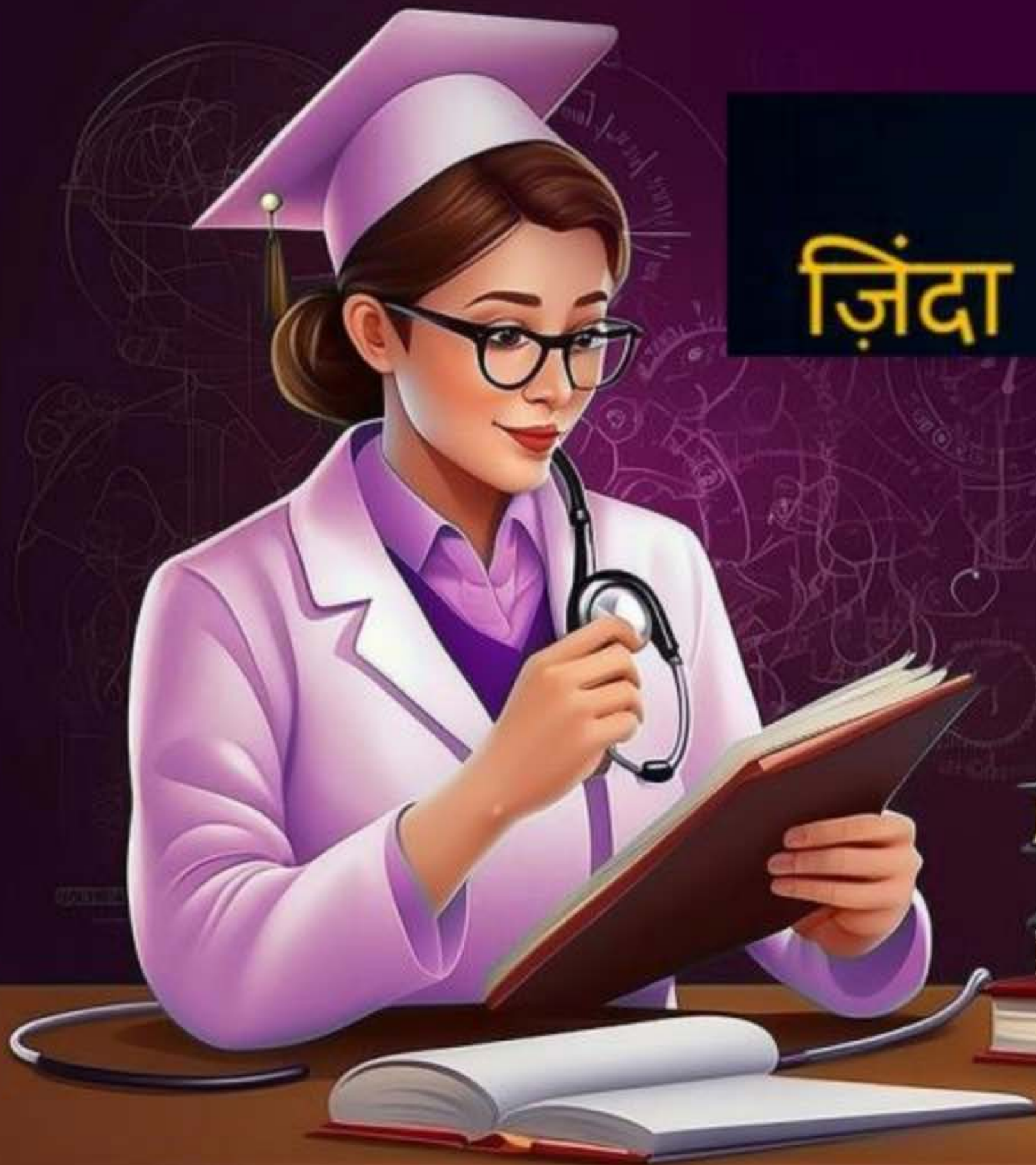


10 am Subah DPP Battle - Ground

Slide No.	option
56	2
75	1
87	1
97	4
100	4
101	4
103	2
105	1
106	3
118	2
120	1
121	2
124	2

FOR NOTES & DPP CHECK DESCRIPTION

शुक्रिया !
जिंदा रहे तो फिर मिलेंगे



14 Jan

↓
EM waves

↓
3:30 hrs