

3. If $\begin{bmatrix} 1 & 2 & 1 \\ 2 & 3 & 1 \\ 3 & a & 1 \end{bmatrix}$ is non-singular matrix and $a \in A$, then the set A is:

(a) $\mathbb{R}$ (b) $\{0\}$ (c) $\{4\}$ (d) $\mathbb{R} - \{4\}$

Sol. (d) $\mathbb{R} - \{4\}$

4. If $|A| = |kA|$, where A is a square matrix of order 2, then sum of all possible values of k is:

(a) 1 (b) -1 (c) 2 (d) 0

Sol. (d) 0

5. If $\frac{d}{dx} [f(x)] = ax + b$ and $f(0) = 0$, then $f(x)$ is equal to;

(a) $a + b$ (b) $\frac{ax^2}{2} + bx$ (c) $\frac{ax^2}{2} + bx + c$ (d) b

Sol. (b) $\frac{ax^2}{2} + bx$

6. Degree of the differential equation $\sin x + \cos \left(\frac{dy}{dx} \right) = y^2$ is:

(a) 2 (b) 1 (c) not defined (d) 0

Sol. (b) 1

7. The integrating factor of the differential equation $(1-y^2) \frac{dx}{dy} + yx = ay, (-1 < y < 1)$ is:

(a) $\frac{1}{y^2 - 1}$ (b) $\frac{1}{\sqrt{y^2 - 1}}$ (c) $\frac{1}{1 - y^2}$ (d) $\frac{1}{\sqrt{1 - y^2}}$

Sol. (d) $\frac{1}{\sqrt{1 - y^2}}$

8. Unit vector along $\overline{PQ}$, where coordinates of P and Q respectively are $(2, 1, -1)$ and $(4, 4, -7)$ is:

(a) $2\hat{i} + 3\hat{j} - 6\hat{k}$ (b) $-2\hat{i} - 3\hat{j} + 6\hat{k}$ (c) $\frac{-2}{7}\hat{i} - \frac{3}{7}\hat{j} + \frac{6}{7}\hat{k}$ (d) $\frac{2}{7}\hat{i} + \frac{3}{7}\hat{j} - \frac{6}{7}\hat{k}$

Sol. (d) $\frac{2}{7}\hat{i} + \frac{3}{7}\hat{j} - \frac{6}{7}\hat{k}$

9. Position vector of the mid-point of line segment AB is $3\hat{i} + 2\hat{j} - 3\hat{k}$. If position vector of the point A is $2\hat{i} + 3\hat{j} - 4\hat{k}$, then position vector of the point B is:

(a) $\frac{5}{2}\hat{i} + \frac{5}{2}\hat{j} - \frac{7}{2}\hat{k}$ (b) $4\hat{i} + \hat{j} - 2\hat{k}$ (c) $5\hat{i} + 5\hat{j} - 7\hat{k}$ (d) $\frac{\hat{i}}{2} - \frac{\hat{j}}{2} + \frac{\hat{k}}{2}$