



LIVE ((•))

# **JEE MAIN 2024**

**ATTEMPT – 01 , 29<sup>TH</sup> JAN 2024 , SHIFT – 02**

# **PAPER DISCUSSION**

# Mathematics





Given set  $\{1, 2, 3, \dots, 50\}$ , one number is selected randomly from set. Find probability that number is multiple of 4 or 6 or 7.

**A**  $\frac{21}{50}$

$\boxed{4 \& 6} \& 7$   
 $(12) \leftarrow$

**B**  $\frac{18}{50}$

$12 + 8 + 7 - 4 - 1 - 1 + 0$

$= 20 + 7 - 6$

$= (21) \Rightarrow P = 21/50$

**C**  $\frac{8}{25}$

**D**  $\frac{21}{25}$

$n(4 \cup 6 \cup 7) =$

$n(4) = \left[ \frac{50}{4} \right] = 12$

$n(6) = \left[ \frac{50}{6} \right] = 8$

$n(7) = \left[ \frac{50}{7} \right] = 7$

$n(4 \cap 6) = \left[ \frac{50}{12} \right] = 4$

$n(6 \cap 7) = \left[ \frac{50}{42} \right] = 1$

$n(4 \cap 7) = \left[ \frac{50}{28} \right] = 1$

$n(4 \cap 7 \cap 6) = 0$



Area bounded by  $0 \leq x \leq 3$ ,  $0 \leq y \leq \text{minimum}(2x + 2, x^2 + 2)$  is  $A$ , then  $12A$  is

**A** 164 ✓

**B** 134

**C** 155

**D** 162

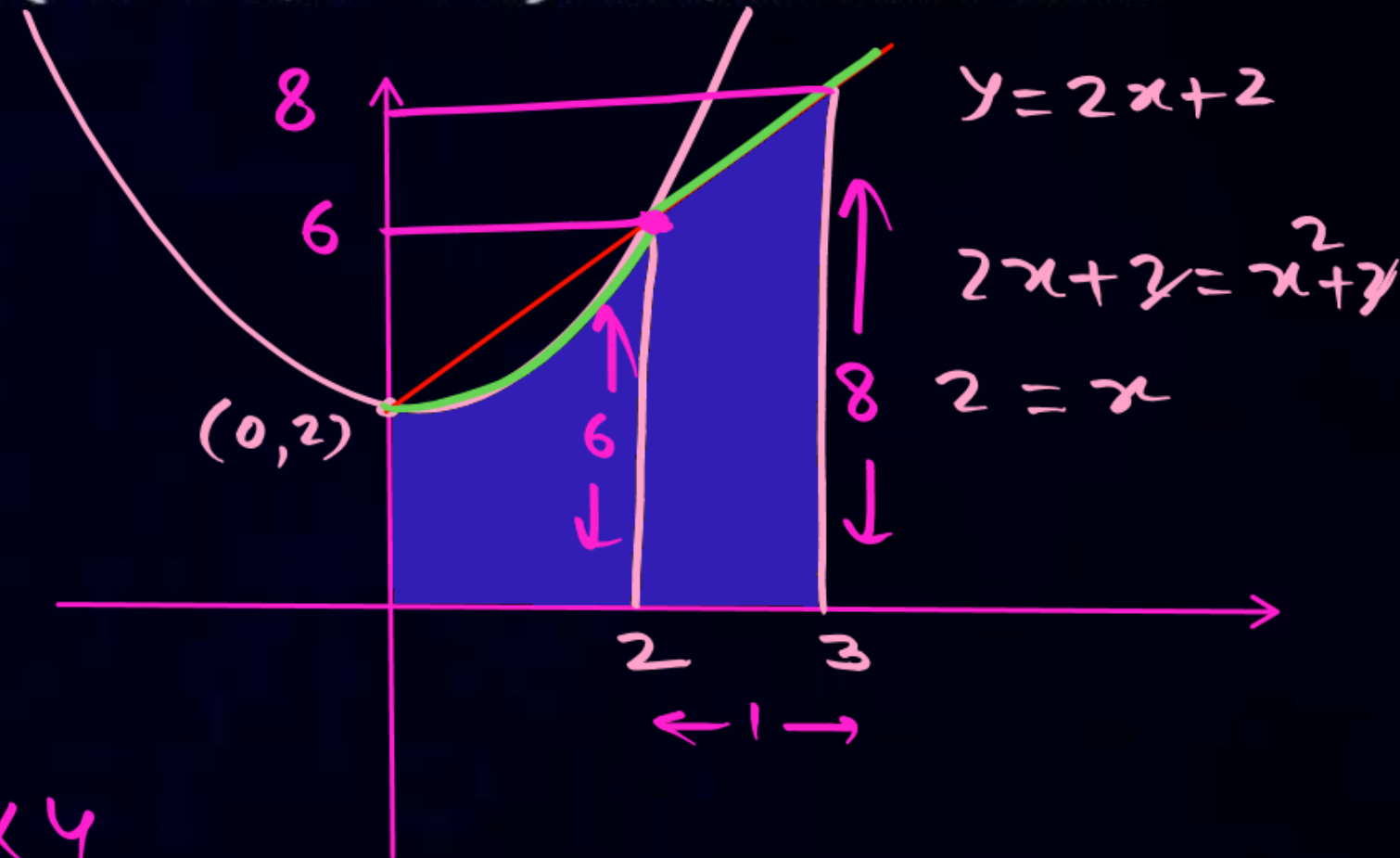
$$\int_0^2 (x^2 + 2) dx + \frac{1}{2}(8+6) \cdot 1$$

$$\left. \frac{x^3}{3} + 2x \right|_0^2 + 7$$

$$\frac{8}{3} + 4 + 7$$

$$A = \frac{8}{3} + 11$$

$$A = \frac{41}{3} \Rightarrow 12A = 41 \times 4 = 164$$







The value of  $\int_{\pi/6}^{\pi/3} \sqrt{1 - \sin 2x} dx$  is \_\_\_\_\_.

**A**  $\sqrt{2} - \sqrt{3} + 1$

**B**  $2\sqrt{2} - \sqrt{3} - 1$

**C**  $2\sqrt{2} + \sqrt{3} - 1$

**D**  $\sqrt{2} + \sqrt{3} - 1$

$$\int_{\pi/6}^{\pi/3} \sqrt{(\cos x - \sin x)^2} dx$$

$$\int_{\pi/6}^{\pi/3} |\cos x - \sin x| dx$$

$$\int_{\pi/6}^{\pi/4} (\cos x - \sin x) dx + \int_{\pi/4}^{\pi/3} (\sin x - \cos x) dx$$

$$\left. \sin x + \cos x \right|_{\pi/6}^{\pi/4} + \left. -(\cos x + \sin x) \right|_{\pi/4}^{\pi/3}$$

$$\sqrt{2} - \left[ \frac{1}{2} + \frac{\sqrt{3}}{2} \right] + \sqrt{2} - \left[ \frac{1}{2} + \frac{\sqrt{3}}{2} \right]$$

$$2\sqrt{2} - (1 + \sqrt{3})$$

$$2\sqrt{2} - 1 - \sqrt{3}$$

Remainder when  $\left((64)^{32}\right)^{32}$  divided by 9 is \_\_\_\_\_.

**A** 1 ✓  $\left[ (1 + \underline{63})^{32} \right]^{32}$

**B** 2  $(1 + 63I)^{32}$

**C** 3  $\textcircled{1} + 63I'$

**D** 4

9





Let  $\cos(2\sin^{-1}x) = \frac{1}{9}$ ,  $x > 0$  holds true for  $x = \frac{m}{n}$ , where  $m$  &  $n$  are coprime further  $\alpha$  &  $\beta$  are roots of quadratic equation  $mx^2 - nx - m + n = 0$  ( $\alpha > \beta$ ) then point  $(\alpha, \beta)$  lies on the line

$$\text{Let } \sin^{-1}x = \theta \Rightarrow \sin\theta = x$$

$$\cos 2\theta = \frac{1}{9}$$

$$1 - 2\sin^2\theta = \frac{1}{9}$$

$$1 - 2x^2 = \frac{1}{9}$$

$$2x^2 = \frac{8}{9}$$

$$x^2 = \frac{4}{9}$$

$$x = \frac{2}{3}$$

$$m = 2$$

$$n = 3$$

$$2x^2 - 3x + 1 = 0$$

$$2x^2 - 2x - x + 1 = 0$$

$$(2x - 1)(x - 1) = 0$$

$$x = \frac{1}{2} \text{ or } 1$$

$$\alpha = 1$$

$$\beta = \frac{1}{2}$$

$$P(1, \frac{1}{2})$$

**A**  $5x - 8y = 9$

**B**  $5x + 8y = 9$

**C**  $8x + 5y = 9$

**D**  $8x - 5y = 3$



If  $\alpha$  &  $\beta$  are roots of the equation  $x^2 - \sqrt{6}x + 3 = 0$  and where  $\text{Im}(\beta) < 0$ . If  $\frac{\alpha^{99}}{\beta} + \beta^{98} = 3^n(a + ib)$ , then  $a, b, n$ .

$$\begin{aligned}
 x &= \frac{\sqrt{6} \pm \sqrt{6-12}}{2} \\
 &= \frac{\sqrt{6} \pm \sqrt{6}i}{2} = \frac{\sqrt{6}}{2} (1 \pm i) = \sqrt{\frac{3}{2}} (1 \pm i) \\
 \frac{\alpha^{99}}{\beta} + \beta^{98} &= \frac{\alpha^{99} + \beta^{99}}{\beta} = \frac{2(\sqrt{3})^{99} \left(-\frac{1}{\sqrt{2}}\right)}{\frac{\sqrt{3}}{\sqrt{2}} (1-i)} = \frac{2(\sqrt{3})^{98} (-1)}{1-i}
 \end{aligned}$$





$$\alpha = \sqrt{3/2} (1 + i)$$

$$= \sqrt{3} \left( \frac{1}{\sqrt{2}} + \frac{i}{\sqrt{2}} \right)$$

$$\alpha = \sqrt{3} (\cos \pi/4 + i \sin \pi/4)$$

$$\alpha^{99} = (\sqrt{3})^{99} \operatorname{cis} \left( \frac{99\pi}{4} \right)$$

$$\alpha^{99} = (\sqrt{3})^{99} \left[ -\frac{1}{\sqrt{2}} + \frac{1}{\sqrt{2}} i \right]$$

$$\alpha^{99} + \beta^{99} = 2(\sqrt{3})^{99} \left( -\frac{1}{\sqrt{2}} \right)$$

$$\beta = \sqrt{3/2} (1 - i)$$

$$\beta = \sqrt{3} (\cos \pi/4 - i \sin \pi/4)$$

$$\beta^{99} = (\sqrt{3})^{99} \left( \cos \frac{99\pi}{4} - i \sin \frac{99\pi}{4} \right)$$

$$\beta^{99} = (\sqrt{3})^{99} \left[ -\frac{1}{\sqrt{2}} - \frac{i}{\sqrt{2}} \right]$$

Distance of  $(2, 4)$  from the line  $2x + y + 2 = 0$  measured parallel to the line  $\sqrt{3}x + y + 2 = 0$ :

**A**  $\frac{10}{2 - \sqrt{3}}$

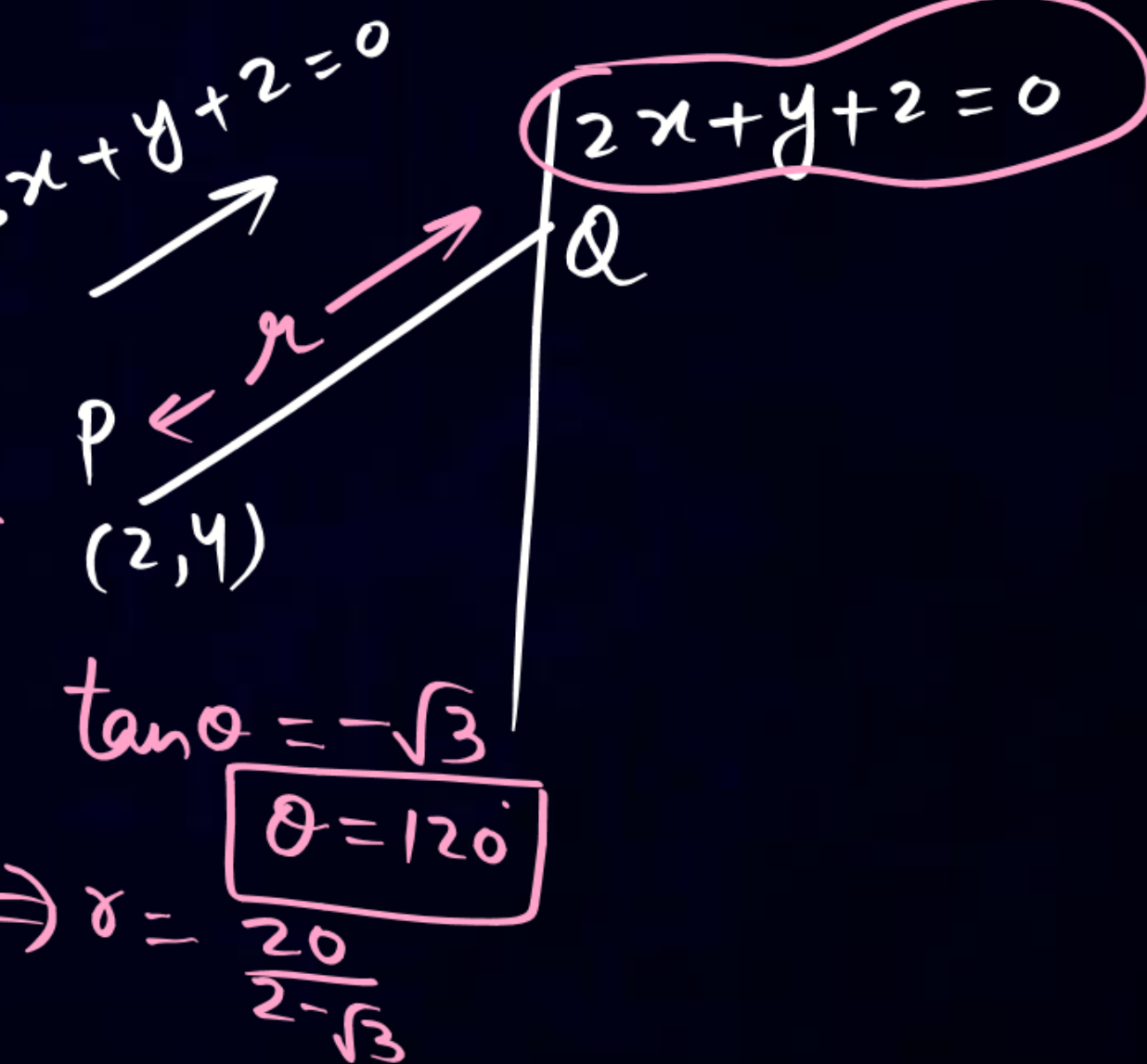
**B**  $\frac{10}{2 + \sqrt{3}}$

**C**  $\frac{10}{2 + \sqrt{5}}$

**D** None of these

$Q[2 + r \cos 120^\circ, 4 + r \sin 120^\circ]$   
 $Q[2 - \frac{r}{2}, 4 + \frac{\sqrt{3}r}{2}]$   
 $2(2 - \frac{r}{2}) + (4 + \frac{\sqrt{3}r}{2}) + 2 = 0$   
 $10 - r + \frac{\sqrt{3}r}{2} = 0$   
 $10 = r(1 - \frac{\sqrt{3}}{2})$   
 $\Rightarrow r = \frac{20}{2 - \sqrt{3}}$

$\sqrt{3}x + y + 2 = 0$   
 $2x + y + 2 = 0$   
 $\tan \theta = -\sqrt{3}$   
 $\theta = 120^\circ$







$a_1, a_2, \dots$  are in G.P. such that  $a_1 = \frac{1}{8}$ ,  $a_1 \neq a_2$  and every term is equal to arithmetic mean of its two successive terms. Find  $S_{20} - S_{18}$ .

A  $-2^{15}$  ✓

B  $-2^{10}$

C  $-2^{20}$

D  $-2^5$

$a = \frac{1}{8}, r = -2$

$S_{20} - S_{18} = T_{19} + T_{20}$

$= 2T_{18}$

$= 2a r^{17} = 2 \times \frac{1}{8} \times (-2)^{17}$

$= -2^{15}$

$T_{18} = \frac{T_{19} + T_{20}}{2}$

$a, ar, ar^2, \dots$

$a = \frac{ar + ar^2}{2}$

$r^2 + r = 2$

$r^2 + r - 2 = 0$

$r = -2$

$\begin{matrix} \nearrow 1 \\ \searrow -2 \end{matrix}$



If  $P(3, 2, 3)$   $Q(4, 6, 2)$   $R(7, 3, 2)$  are the vertices of  $\Delta PQR$ , then find  $\angle QPR =$

**A**  $\cos^{-1} \frac{1}{18}$

**B**  $\frac{\pi}{6}$

**C**  $\frac{\pi}{3}$

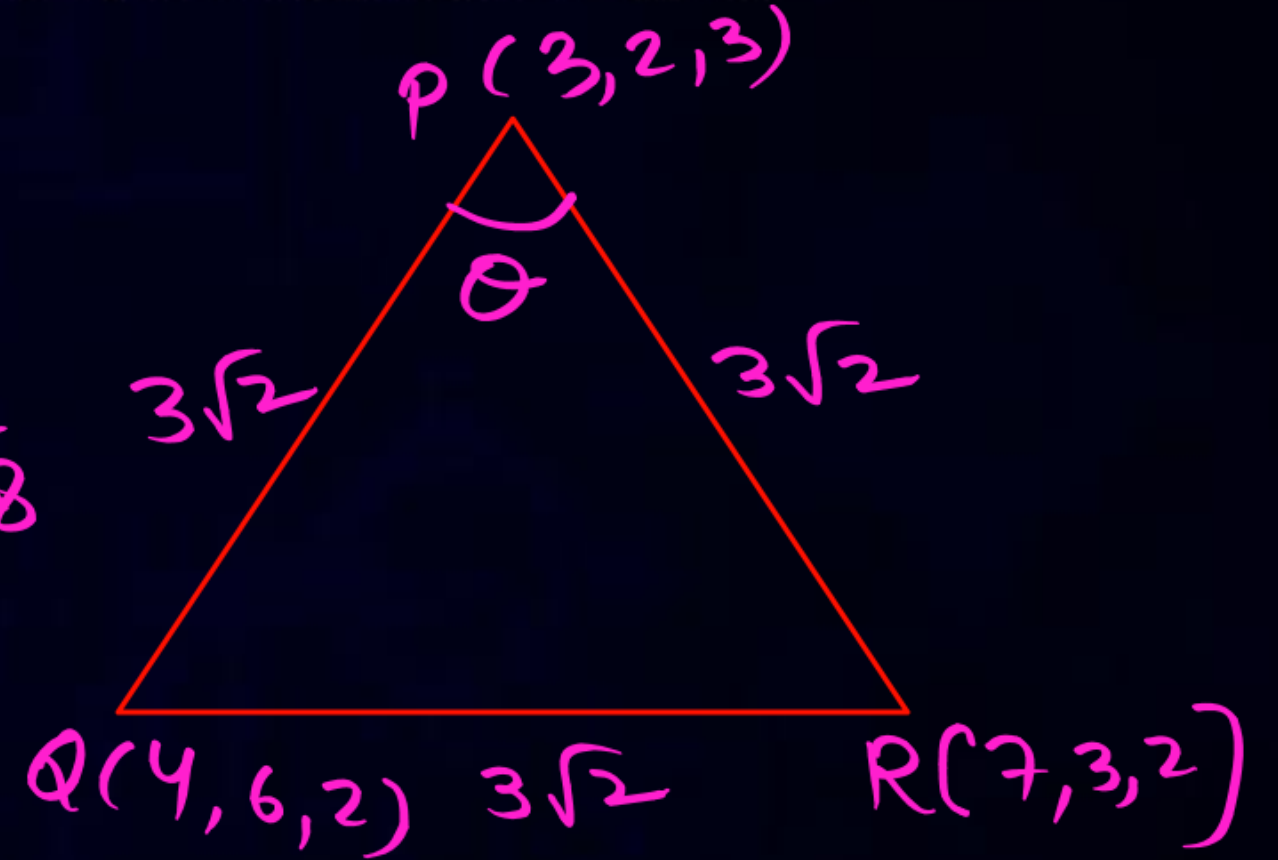
**D**  $\cos^{-1} \frac{7}{18}$

$$(PQ)^2 = 1^2 + 4^2 + 1^2 = 18$$

$$PQ = 3\sqrt{2}$$

$$PR = \sqrt{4^2 + 1^2 + 1^2} = \sqrt{18}$$

$$QR = \sqrt{3^2 + 3^2} = \sqrt{18}$$







8 identical books are to be kept in 4 shelves. Find the number of different ways this can be done.

A

B

C

D

distinct shelves →

$$x_1 + x_2 + x_3 + x_4 = 8$$

Identical shelf

${}^{11}C_3$

|   |   |   |   |
|---|---|---|---|
| 0 | 0 | 0 | 8 |
| 0 | 0 | 1 | 7 |
| 0 | 0 | 2 | 6 |
| 0 | 0 | 3 | 5 |
| 0 | 0 | 4 | 4 |
| 0 | 1 | 2 | 5 |

15



If  $\ln a, \ln b, \ln c$  are in A.P. and  $\ln a - \ln 2b, \ln 2b - \ln 3c, \ln 3c - \ln a$  are in A.P. then  $a : b : c$  is \_\_\_\_\_.

A  $1:2:3$

B  $7:7:4$

C  $9:6:4$

D  $4:6:9$

$$2 \ln b = \ln a + \ln c$$

$$\ln\left(\frac{a}{2b}\right), \ln\left(\frac{2b}{3c}\right), \ln\left(\frac{3c}{a}\right) \quad b^2 = ac \Rightarrow b/a = c/b$$

$$2 \ln\left(\frac{2b}{3c}\right) = \ln \frac{a}{2b} + \ln\left(\frac{3c}{a}\right)$$

$$\left(\frac{2b}{3c}\right)^2 = \frac{a}{2b} \cdot \frac{3c}{a} \Rightarrow \frac{4b^2}{9c^2} = \frac{3c}{2b} \Rightarrow \frac{8b^3}{27} = c^3$$

$$\boxed{\frac{2b}{3} = c} \checkmark$$





$$\frac{2b}{3} = c$$

$$\boxed{b/c = 3/2}$$

$$c/b = 2/3 = b/a$$

$$c/b = b/a$$

$$a/b = 3/2 \times 3/3 = 9/6$$

$$b/c = 3/2 \times 2/2 = 6/4$$

$$9:6:4$$



If  $r = |z|$ ,  $\theta = \arg(z)$  and  $z = 2 - 2i \tan\left(\frac{5\pi}{8}\right)$ , then find  $(r, \theta)$ .

**A**  $\left(2\sec\frac{5\pi}{8}, \frac{3\pi}{8}\right)$

**B**  $\left(2\sec\frac{3\pi}{8}, \frac{3\pi}{8}\right)$

**C**  $\left(2\tan\frac{3\pi}{8}, \frac{5\pi}{8}\right)$

**D**  $\left(2\tan\frac{3\pi}{8}, \frac{3\pi}{8}\right)$

$$|z| = \sqrt{2^2 + 4\tan^2\frac{5\pi}{8}}$$

$$= 2\sqrt{1 + \tan^2\frac{5\pi}{8}}$$

$$= 2\sqrt{\sec^2\frac{5\pi}{8}}$$

$$r = 2|\sec\frac{5\pi}{8}| = 2\sec\frac{3\pi}{8}$$

$$\frac{4\pi}{8} = 90^\circ$$
$$\frac{5\pi}{8} > 90^\circ$$

$$z = 2 + 2i \tan\frac{3\pi}{8}$$
$$\arg z = \tan^{-1}\left(\tan\frac{3\pi}{8}\right)$$
$$\theta = \frac{3\pi}{8}$$





In which interval the function  $f(x) = \frac{x}{x^2-6x-16}$  is increasing:

$$f'(x) > 0$$

**A**  $\phi$  ✓

**B**  $\left[1, \frac{3}{7}\right) \cup \left(\frac{5}{4}, \infty\right)$

**C**  $\left(\frac{5}{4}, \infty\right)$

**D**  $\left[\frac{3}{4}, \frac{5}{4}\right]$

$$f'(x) = \frac{1 \cdot (x^2 - 6x - 16) - x(2x - 6)}{(x^2 - 6x - 16)^2}$$

$$\frac{x^2 - 6x - 16 - 2x^2 + 6x}{( )^2}$$

$$\frac{-x^2 - 16}{( )^2} = \frac{-(x^2 + 16)}{( )^2} \rightarrow -ve$$



$(\alpha, \beta)$  lies on the  $y^2 = 4x$  and  $(\alpha, \beta)$  also lie on chord with mid-point  $(1, \frac{5}{4})$  of another parabola  $x^2 = 8y$ , then value  $|(8 - \beta)(\alpha - 28)|$  is \_\_\_\_\_.

A 192 ✓

B 92

C 64

D 128

$$\alpha = t^2, \beta = 2t$$

$$x + 4 = 4y$$

$$t^2 + 4 = 8t$$

$$t^2 - 8t + 4 = 0$$

$$(t - 4)^2 = -4 + 16$$

$$x^2 = 8y$$

$$T = S_1$$

$$xx_1 - 4(y + y_1) = x_1^2 - 8y_1$$

$$xx_1 - 4(y + 5/4) = 1 - 8 \cdot 5/4$$

$$x - 4y - 5 = 1 - 10$$

$$x - 4y + 4 = 0$$

$$x + 4 = 4y$$





$$|(8-2t)(t^2-28)|$$

$$|(8-2t)(8t-4-28)|$$

$$|(8-2t)(8t-32)|$$

$$16 |(4-t)(t-4)|$$

$$16 |(t-4)^2|$$

$$16 \times 12 = \boxed{192}$$

$$\begin{array}{r} 160 \\ 32 \\ \hline 192 \end{array}$$



Unit vector  $\hat{u} = x\hat{i} + y\hat{j} + z\hat{k}$  makes angles  $\frac{\pi}{2}, \frac{\pi}{3}, \frac{2\pi}{3}$  with

$\vec{a} = \left(\frac{1}{\sqrt{2}}\hat{i} + \frac{1}{\sqrt{2}}\hat{k}\right), \left(\frac{1}{\sqrt{2}}\hat{j} + \frac{1}{\sqrt{2}}\hat{k}\right), \left(\frac{1}{\sqrt{2}}\hat{i} + \frac{1}{\sqrt{2}}\hat{j}\right)$  respectively and

$\vec{v} = \frac{1}{\sqrt{2}}\hat{i} + \frac{1}{\sqrt{2}}\hat{j} + \frac{1}{\sqrt{2}}\hat{k}$ . Find  $|\vec{u} - \vec{v}|$ .

$$\vec{u} \cdot \vec{a} = \cos \theta$$

$$\vec{u} \cdot \vec{a} = 0, \vec{u} \cdot \vec{b} = \frac{1}{2}$$

$$\vec{u} \cdot \vec{c} = -\frac{1}{2}$$

$$\frac{x}{\sqrt{2}} + \frac{z}{\sqrt{2}} = 0 \Rightarrow \boxed{x + z = 0} \rightarrow \textcircled{1}$$

$$\frac{y}{\sqrt{2}} + \frac{z}{\sqrt{2}} = \frac{1}{2} \Rightarrow \boxed{y + z = \frac{1}{\sqrt{2}}} \rightarrow \textcircled{2}$$

$$\frac{x}{\sqrt{2}} + \frac{y}{\sqrt{2}} = -\frac{1}{2} \Rightarrow \boxed{x + y = -\frac{1}{\sqrt{2}}} \rightarrow \textcircled{3}$$

$$\textcircled{2} + \textcircled{3} \Rightarrow 2y = 0 \Rightarrow \boxed{y = 0}$$

**A**  $\sqrt{\frac{5}{2}}$

$$y = 0$$

$$x = -\frac{1}{\sqrt{2}}$$

$$z = \frac{1}{\sqrt{2}}$$

$$\vec{u} = -\frac{1}{\sqrt{2}}\hat{i} + \frac{1}{\sqrt{2}}\hat{k}$$

$$\vec{v} = \frac{1}{\sqrt{2}}\hat{i} + \frac{1}{\sqrt{2}}\hat{j} + \frac{1}{\sqrt{2}}\hat{k}$$

**B**  $\sqrt{\frac{7}{2}}$

**D**  $\sqrt{\frac{2}{7}}$

**C**  $\sqrt{\frac{2}{5}}$





$$\vec{u} - \vec{v} = -\sqrt{2}\hat{i} - \frac{1}{\sqrt{2}}\hat{j}$$

$$|\vec{u} - \vec{v}| = \sqrt{2 + \frac{1}{2}} = \sqrt{5/2}$$



The mean of 5 observations is  $\frac{24}{5}$  and variance is  $\frac{194}{25}$ . If the mean of first four observations is  $\frac{7}{2}$ , then the variance of first four observations is \_\_\_\_\_.

A  $\frac{3}{2}$

B  $\frac{5}{2}$

C  $\frac{5}{4}$  ✓

D  $\frac{2}{3}$

$$\frac{x_1 + x_2 + \dots + x_5}{5} = \frac{24}{5}$$

$$14 + x_5 = 24$$

$$\Rightarrow x_5 = 10$$

$$\frac{x_1 + x_2 + \dots + x_4}{4} = \frac{7}{2}$$

$$x_1 + \dots + x_4 = 14$$

$$\frac{194}{25} = \frac{\sum x_i^2}{5} - \left(\frac{24}{5}\right)^2 \Rightarrow \frac{194}{25} + \frac{576}{25} = \frac{\sum x_i^2}{5}$$

$$\frac{770}{5} = \sum x_i^2 \Rightarrow \sum x_i^2 = 154$$





$$\sum_{i=1}^4 x_i^2 + 10^2 = 154$$

$$\begin{aligned}\sum_{i=1}^4 x_i^2 &= 154 - 100 \\ &= 54\end{aligned}$$

$$\begin{aligned}\text{Var} &= \frac{54}{4} - \left(\frac{7}{2}\right)^2 \\ &= \frac{54 - 49}{4} = 5/4.\end{aligned}$$



If  $f(x) = \ln \left( \frac{1-x^2}{1+x^2} \right)$ , then value of  $225(f'(x) - f''(x))$  at  $x = \frac{1}{2}$  is \_\_\_\_\_.

$$f(x) = \ln(1-x^2) - \ln(1+x^2)$$

$$f'(x) = \frac{1}{1-x^2}(-2x) - \frac{1}{1+x^2}(2x) = -2x \left( \frac{1}{1-x^2} + \frac{1}{1+x^2} \right)$$

$$f'(x) = -2x \frac{2}{1-x^4} = -\frac{4x}{1-x^4}$$
$$f'\left(\frac{1}{2}\right) = \frac{-4 \times \frac{1}{2}}{1 - \frac{1}{16}} = \frac{-2}{\frac{15}{16}} = -\frac{32}{15}$$

$$225 f'\left(\frac{1}{2}\right) = -32 \times 15$$





$$f'(x) = -\frac{4x}{1-x^4} = \frac{4x}{x^4-1}$$

$$\begin{aligned} \text{Ans} &= 4 \times 19 \times 16 - 32 \times 15 \\ &= 32 [38 - 15] = \boxed{32 \times 23} \end{aligned}$$

$$f''(x) = \frac{(x^4-1)4 - 4x(4x^3)}{(x^4-1)^2} = \frac{4[x^4-1-4x^4]}{(x^4-1)^2}$$

$$f''(x) = \frac{-4[1+3x^4]}{(x^4-1)^2}$$

$$f''\left(\frac{1}{2}\right) = \frac{-4\left[1 + 3\left(\frac{1}{16}\right)\right]}{\left(\frac{15}{16}\right)^2} = -\frac{4 \times 19 \times 16}{225}$$

$$\boxed{225 f''\left(\frac{1}{2}\right) = -4 \times 19 \times 16}$$



A function  $f(x)$  satisfies the differential Equation

$$x \left( \cos \left( \frac{y}{x} \right) \right) \frac{dy}{dx} = \frac{y}{x} \cos \left( \frac{y}{x} \right) + \frac{x}{x} \text{ also given that } f(1) = \frac{\pi}{3},$$

Then find  $f(x)$

$$y = vx \Rightarrow y/x = v$$

$$\cos v \left( v + x \frac{dv}{dx} \right) = v \cos v + 1$$

$$\cancel{v \cos v} + x \cos v \frac{dv}{dx} = \cancel{v \cos v} + 1$$

$$\int \cos v dv = \int \frac{dx}{x}$$

$$\boxed{\sin v = \ln x + C}$$

$$\sin(y/x) = \ln x + C$$

$$\sin(\pi/3) = \ln 1 + C$$

$$\boxed{C = \sqrt{3}/2} \checkmark$$





If  $x^2 = 2^y + 2023$  &  $x, y \in \mathbb{N}$ . Find  $x + y$ .

$$x^2 = \underbrace{2^y}_{\text{even}} + \underbrace{2023}_{\text{odd}}$$

$$y = 1$$

$$x = 45$$

$$\text{odd} = x^2$$

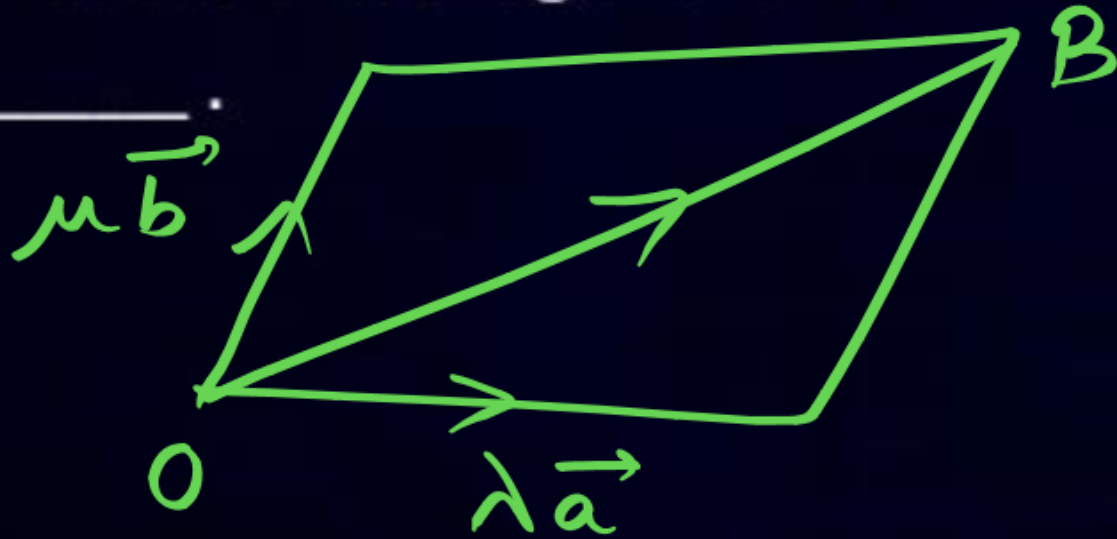
$$(40)^2 = 1600$$

$$(50)^2 = 2500$$

$$\begin{array}{r} 2 \\ 45 \\ 45 \\ \hline 225 \\ 180 \\ \hline 2025 \end{array}$$

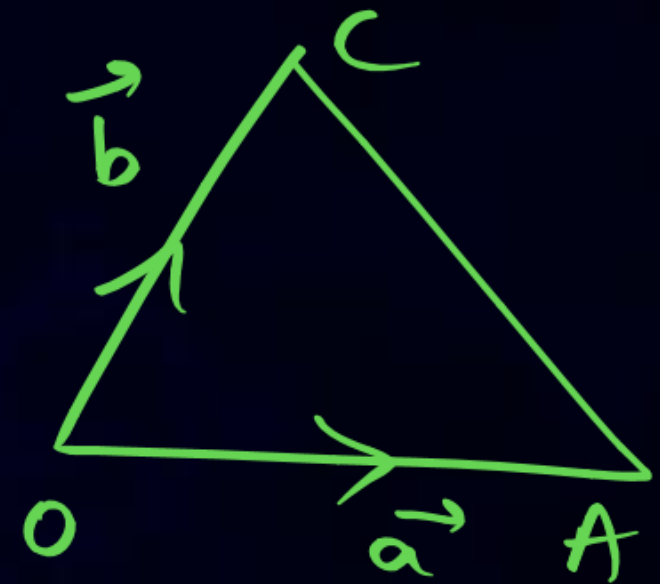


If  $\overrightarrow{OA} = \vec{a}$ ,  $\overrightarrow{OC} = \vec{b}$  and area of  $\triangle OAC$  is  $S$  and a parallelogram with sides parallel to  $\overrightarrow{OA}$  &  $\overrightarrow{OC}$  and diagonal  $\overrightarrow{OB} = 12\vec{a} + 4\vec{b}$ , has area equal to  $B$ , then  $\frac{B}{S}$  is equal to \_\_\_\_\_.



$$\overrightarrow{OB} = \lambda \vec{a} + \mu \vec{b} = 12\vec{a} + 4\vec{b}$$

$$12\vec{a} \text{ \& \; } 4\vec{b} \quad \lambda = 12, \mu = 4.$$



$$S = \frac{1}{2} |\vec{a} \times \vec{b}|$$

$$B = |12\vec{a} \times 4\vec{b}| = 48 |\vec{a} \times \vec{b}|$$

$$\frac{48}{\frac{1}{2}}$$





$\frac{3\cos 2x + \cos^3 2x}{\cos^6 x - \sin^6 x} = x^3 - x^2 + 6$ , then find the sum of roots.

LHS:  $\frac{\cos 2x (3 + \cos^2 2x)}{(\cos^2 x - \sin^2 x) (\cos^4 x + \sin^4 x + \cos^2 x \sin^2 x)}$

$$\frac{3 + \cos^2 2x}{1 - \frac{4\sin^2 x \cos^2 x}{4}} = \frac{3 + \cos^2 2x}{1 - \frac{\sin^2 2x}{4}}$$

$$= 4 \left( \frac{3 + \cos^2 2x}{3 + 1 - \sin^2 2x} \right) = 4$$

$$x^3 - x^2 + 6 = 4$$

$$x^3 - x^2 + 2 = 0$$

$$\text{Sum} = 1 \checkmark$$



Consider function  $f(x) = 2x + 3x^{2/3}$

$$f'(x) = 2 + 3 \cdot \frac{2}{3} x^{-1/3}$$

$$2 \left[ 1 + \frac{1}{x^{1/3}} \right] = 0$$

$$f'(x) = \frac{x^{1/3} + 1}{x^{1/3}} = 0$$

$x > -1$   
 $x^{1/3} > (-1)^{1/3}$   
 $x^{1/3} > -1$

- A** Exactly 1 local minima and no local maxima
- B** Exactly 1 local minima and 1 local maxima
- C** No local minima and 1 local maxima
- D** No local maxima and 1 local minima





Lines  $x + 2y - 10 = 0$  and  $3x - y - 2 = 0$  intersect at A and lines  $2x - 3y + 2 = 0$  and  $4x + 3y - 5 = 0$  intersect at B. Find perpendicular distance of  $(-5, 2)$  from the line AB.

$$x + 2y = 10$$

$$3x - 2 = y$$

$$x + 2(3x - 2) = 10$$

$$7x = 14$$

$$x = 2$$

$$y = 4$$

$$A(2, 4)$$

Eq<sup>n</sup> of AB

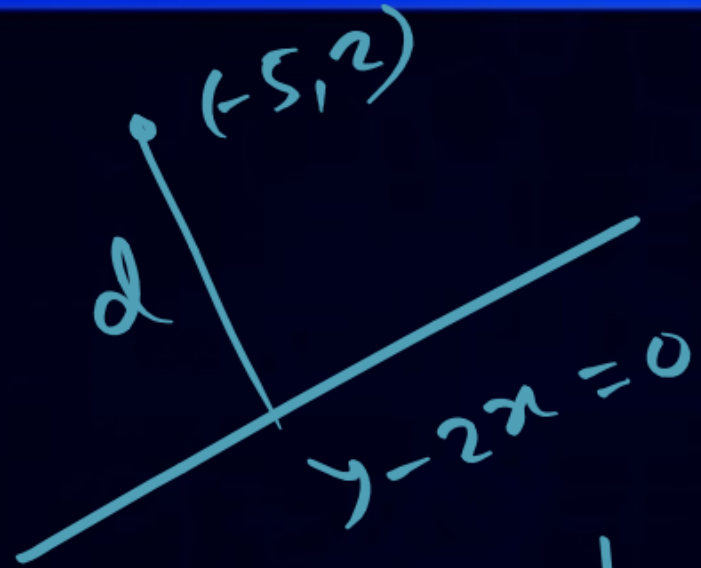
$$y = 2x$$

$$\begin{array}{r} 2x - 3y + 2 = 0 \\ 4x + 3y - 5 = 0 \\ \hline 6x - 3 = 0 \end{array}$$

$$x = \frac{1}{2}$$

$$1 - 3y + 2 = 0 \quad y = 1$$

$$B\left(\frac{1}{2}, 1\right)$$



$$d = \left| \frac{2 + 10}{\sqrt{5}} \right| = \frac{12}{\sqrt{5}}$$





**THANK**  
**YOU**