

NCERT Solutions for Class 10 Maths Chapter 12 Exercise 12.1: NCERT Solutions for Class 10 Maths Chapter 12, Exercise 12.1, focus on Surface Areas and Volumes of solid shapes like cones, cylinders, spheres, hemispheres, and combinations of these. This exercise helps students understand the application of formulas to calculate curved, lateral, and total surface areas and volumes of these shapes.

It emphasizes problem-solving skills by combining geometry with real-life applications. Step-by-step solutions are provided to simplify concepts and enhance clarity. This exercise is crucial for building a strong foundation for geometry-related problems, boosting confidence in solving CBSE board exam questions effectively.

NCERT Solutions for Class 10 Maths Chapter 12 Exercise 12.1 Overview

NCERT Solutions for Class 10 Maths Chapter 12, Exercise 12.1, provide a comprehensive understanding of Surface Areas and Volumes, focusing on geometric shapes like cylinders, cones, spheres, and their combinations. This exercise is crucial for developing problem-solving skills, as it bridges theoretical geometry with practical applications, such as designing objects or calculating capacities.

Mastering these concepts is important for CBSE exams and forms the foundation for advanced studies in science, engineering, and architecture. The solutions emphasize accuracy, logical reasoning, and formula application, ensuring students gain confidence and clarity in tackling real-world mathematical problems involving 3D shapes.

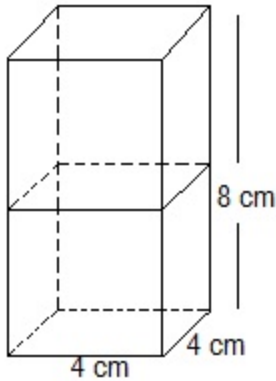
NCERT Solutions for Class 10 Maths Chapter 12 Exercise 12.1 Surface Areas and Volumes

Below is the NCERT Solutions for Class 10 Maths Chapter 12 Exercise 12.1 Surface Areas and Volumes -

1. 2 cubes each of volume 64 cm^3 are joined end to end. Find the surface area of the resulting cuboid.

Answer:

The diagram is given as:



Given,

The Volume (V) of each cube is = 64 cm^3

This implies that $a^3 = 64 \text{ cm}^3$

$\therefore a = 4 \text{ cm}$

Now, the side of the cube = $a = 4 \text{ cm}$

Also, the length and breadth of the resulting cuboid will be 4 cm each, while its height will be 8 cm.

So, the surface area of the cuboid = $2(lb+bh+lh)$

$$= 2(8 \times 4 + 4 \times 4 + 4 \times 8) \text{ cm}^2$$

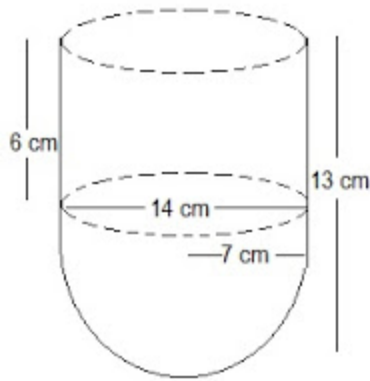
$$= 2(32 + 16 + 32) \text{ cm}^2$$

$$= (2 \times 80) \text{ cm}^2 = 160 \text{ cm}^2$$

2. A vessel is in the form of a hollow hemisphere mounted by a hollow cylinder. The diameter of the hemisphere is 14 cm, and the total height of the vessel is 13 cm. Find the inner surface area of the vessel.

Answer:

The diagram is as follows:



Now, the given parameters are:

The diameter of the hemisphere = $D = 14$ cm

The radius of the hemisphere = $r = 7$ cm

Also, the height of the cylinder = $h = (13-7) = 6$ cm

And the radius of the hollow hemisphere = 7 cm

Now, the inner surface area of the vessel = CSA of the cylindrical part + CSA of the hemispherical part

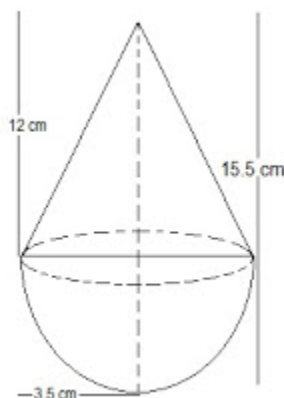
$$(2\pi rh + 2\pi r^2) \text{ cm}^2 = 2\pi r(h+r) \text{ cm}^2$$

$$2 \times \left(\frac{22}{7}\right) \times 7(6+7) \text{ cm}^2 = 572 \text{ cm}^2$$

3. A toy is in the form of a cone of radius 3.5 cm mounted on a hemisphere of the same radius. The total height of the toy is 15.5 cm. Find the total surface area of the toy.

Answer:

The diagram is as follows:



Given that the radius of the cone and the hemisphere (r) = 3.5 cm or $7/2$ cm

The total height of the toy is given as 15.5 cm.

So, the height of the cone (h) = $15.5 - 3.5 = 12$ cm

$$\text{Slant height of the cone (l)} = \sqrt{h^2 + r^2}$$

$$\Rightarrow l = \sqrt{12^2 + (3.5)^2}$$

$$\Rightarrow l = \sqrt{12^2 + (7/2)^2}$$

$$\Rightarrow l = \sqrt{144 + 49/4} = \sqrt{(576 + 49)/4} = \sqrt{625/4}$$

$$\Rightarrow l = 25/2$$

\therefore The curved surface area of the cone = $\pi r l$

$$(22/7) \times (7/2) \times (25/2) = 275/2 \text{ cm}^2$$

Also, the curved surface area of the hemisphere = $2\pi r^2$

$$2 \times (22/7) \times (7/2)^2$$

$$= 77 \text{ cm}^2$$

Now, the Total surface area of the toy = CSA of the cone + CSA of the hemisphere

$$= (275/2) + 77 \text{ cm}^2$$

$$= (275 + 154)/2 \text{ cm}^2$$

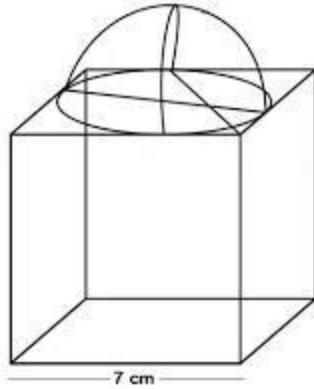
$$= 429/2 \text{ cm}^2 = 214.5 \text{ cm}^2$$

So, the total surface area (TSA) of the toy is 214.5 cm^2

4. A cubical block of side 7 cm is surmounted by a hemisphere. What is the greatest diameter the hemisphere can have? Find the surface area of the solid.

Answer:

It is given that each side of the cube is 7 cm. So, the radius will be $7/2$ cm.



We know,

The total surface area of solid (TSA) = surface area of the cubical block + CSA of the hemisphere – Area of the base of the hemisphere

$$\therefore \text{TSA of solid} = 6 \times (\text{side})^2 + 2\pi r^2 - \pi r^2$$

$$= 6 \times (\text{side})^2 + \pi r^2$$

$$= 6 \times (7)^2 + (22/7) \times (7/2) \times (7/2)$$

$$= (6 \times 49) + (77/2)$$

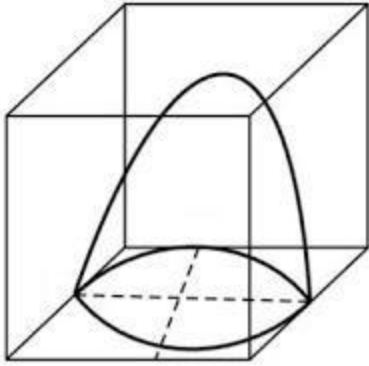
$$= 294 + 38.5 = 332.5 \text{ cm}^2$$

So, the surface area of the solid is 332.5 cm^2

5. A hemispherical depression is cut out from one face of a cubical wooden block such that the diameter l of the hemisphere is equal to the edge of the cube. Determine the surface area of the remaining solid.

Answer:

The diagram is as follows:



Now, the diameter of the hemisphere = Edge of the cube = l

So, the radius of the hemisphere = $l/2$

\therefore The total surface area of solid = surface area of cube + CSA of the hemisphere – Area of the base of the hemisphere

The surface area of the remaining solid = $6(\text{edge})^2 + 2\pi r^2 - \pi r^2$

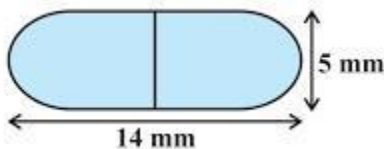
$$= 6l^2 + \pi r^2$$

$$= 6l^2 + \pi(l/2)^2$$

$$= 6l^2 + \pi l^2/4$$

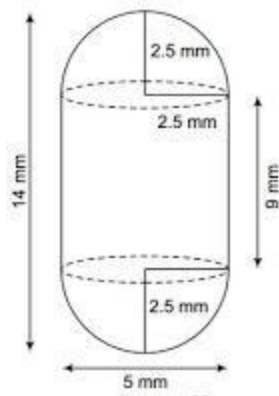
$$= l^2/4(24 + \pi) \text{ sq. units}$$

6. A medicine capsule is in the shape of a cylinder with two hemispheres stuck to each of its ends. The length of the entire capsule is 14 mm, and the diameter of the capsule is 5 mm. Find its surface area.



Answer:

Two hemispheres and one cylinder are shown in the figure given below.



Here, the diameter of the capsule = 5 mm

\therefore Radius = $5/2 = 2.5$ mm

Now, the length of the capsule = 14 mm

So, the length of the cylinder = $14 - (2.5 + 2.5) = 9$ mm

\therefore The surface area of a hemisphere = $2\pi r^2 = 2 \times (22/7) \times 2.5 \times 2.5$
 $= 275/7 \text{ mm}^2$

Now, the surface area of the cylinder = $2\pi rh$

$= 2 \times (22/7) \times 2.5 \times 9$

$(22/7) \times 45 = 990/7 \text{ mm}^2$

Thus, the required surface area of the medicine capsule will be

$= 2 \times \text{surface area of hemisphere} + \text{surface area of the cylinder}$

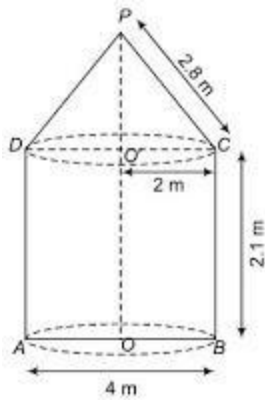
$= (2 \times 275/7) \times 990/7$

$= (550/7) + (990/7) = 1540/7 = 220 \text{ mm}^2$

7. A tent is in the shape of a cylinder surmounted by a conical top. If the height and diameter of the cylindrical part are 2.1 m and 4 m, respectively, and the slant height of the top is 2.8 m, find the area of the canvas used for making the tent. Also, find the cost of the canvas of the tent at the rate of Rs 500 per m^2 . (Note that the base of the tent will not be covered with canvas.)

Answer:

It is known that a tent is a combination of a cylinder and a cone.



From the question, we know that

Diameter = 4 m

The slant height of the cone (l) = 2.8 m

Radius of the cone (r) = Radius of cylinder = $4/2 = 2$ m

Height of the cylinder (h) = 2.1 m

So, the required surface area of the tent = surface area of the cone + surface area of the cylinder

$$= \pi r l + 2\pi r h$$

$$= \pi r (l + 2h)$$

$$= (22/7) \times 2 (2.8 + 2 \times 2.1)$$

$$= (44/7) (2.8 + 4.2)$$

$$= (44/7) \times 7 = 44 \text{ m}^2$$

\therefore The cost of the canvas of the tent at the rate of ₹500 per m^2 will be

$$= \text{Surface area} \times \text{cost per m}^2$$

$$44 \times 500 = ₹22000$$

So, Rs. 22000 will be the total cost of the canvas.

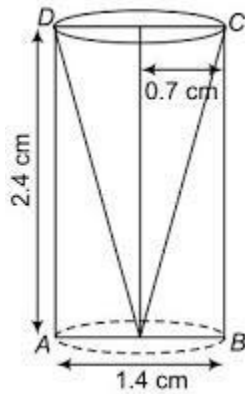
8. From a solid cylinder whose height is 2.4 cm and diameter is 1.4 cm, a conical cavity of the

same height and same diameter is hollowed out. Find the total surface area of the

remaining solid to the nearest cm^2 .

Answer:

The diagram for the question is as follows:



From the question, we know the following:

The diameter of the cylinder = diameter of conical cavity = 1.4 cm

So, the radius of the cylinder = radius of the conical cavity = $1.4/2 = 0.7$

Also, the height of the cylinder = height of the conical cavity = 2.4 cm

$$\begin{aligned}\therefore \text{Slant height of the conical cavity } (l) &= \sqrt{h^2 + r^2} \\ &= \sqrt{(2.4)^2 + (0.7)^2} \\ &= \sqrt{5.76 + 0.49} = \sqrt{6.25} \\ &= 2.5 \text{ cm}\end{aligned}$$

Now, the TSA of the remaining solid = surface area of conical cavity + TSA of the cylinder

$$= \pi r l + (2\pi r h + \pi r^2)$$

$$= \pi r (l + 2h + r)$$

$$= (22/7) \times 0.7 (2.5 + 4.8 + 0.7)$$

$$= 2.2 \times 8 = 17.6 \text{ cm}^2$$

So, the total surface area of the remaining solid is 17.6 cm^2

Benefits of Using NCERT Solutions for Class 10 Maths

Chapter 12 Exercise 12.1

Comprehensive Understanding: Provides detailed explanations of concepts like surface areas and volumes of geometric shapes, ensuring conceptual clarity.

Step-by-Step Solutions: Simplifies problem-solving with clear, structured approaches to complex questions.

Exam Preparedness: Helps students tackle CBSE exam questions confidently, adhering to the latest syllabus.

Real-Life Applications: Links geometry with practical uses, such as calculating capacities and designing objects.

Time Management: Enhances speed and accuracy in solving 3D geometry problems.

Accessible Format: Available in PDF format for convenient offline learning and revision.