

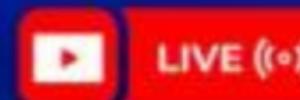


JEE MAIN 2024

ATTEMPT - 01, 27TH JAN 2024, SHIFT - 02

PAPER DISCUSSION

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PAPER DISCUSSION



Mathematics

Coefficient of x^{2012} in $(1-x)^{2008} (1+x+x^2)^{2007}$

A 0 ✓

B 1

C 2

D 3

$$(1-x) \left[\underbrace{(1-x)(1+x+x^2)}_{(1-x^3)^2} \right]^{2007}$$

$$(1-x^3)^{2007} - x (1-x^3)^{2007}$$

$$\cancel{x^{2012}} \quad \cancel{x^{2011}}$$

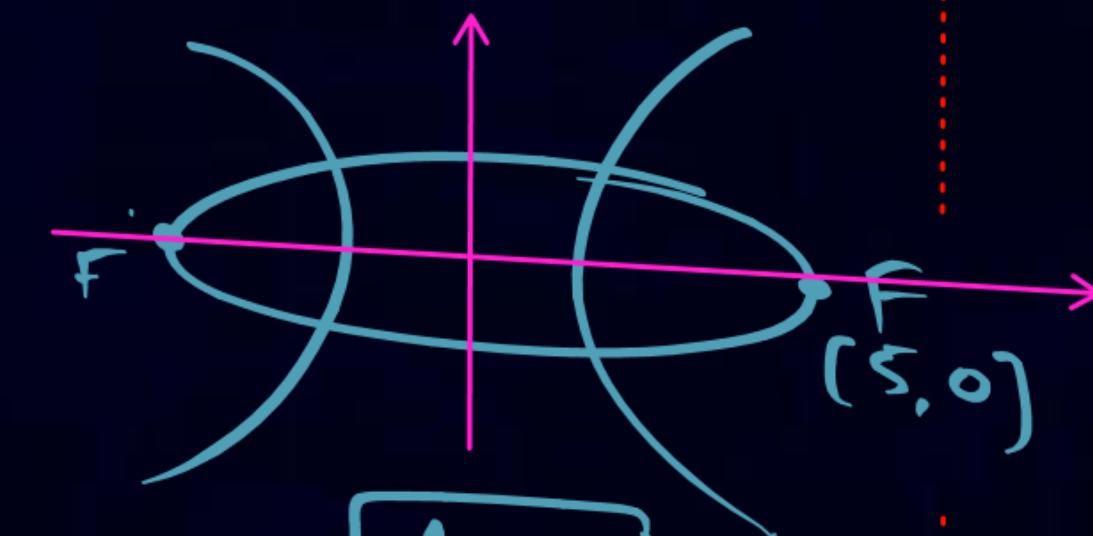
$x^3 \rightarrow \text{multiples}$

① x^{3k}

③

An ellipse is passing through foci of hyperbola $\frac{x^2}{16} - \frac{y^2}{9} = 1$ and product of their eccentricities is 1 then the length of chord of ellipse passing through $(0, 2)$ and parallel to x-axis is

- A $\frac{5\sqrt{5}}{3}$
- B $\frac{3}{5\sqrt{5}}$
- C $\frac{10\sqrt{5}}{3}$
- D $\frac{20\sqrt{5}}{3}$



$$A = 5$$

$$\frac{x^2}{16} - \frac{y^2}{9} = 1$$

$$f (ae, 0)$$

$$a = 4$$

$$b = 3$$

$$a^2 e^2 = a^2 + b^2$$

$$16e^2 = 4^2 + 3^2$$

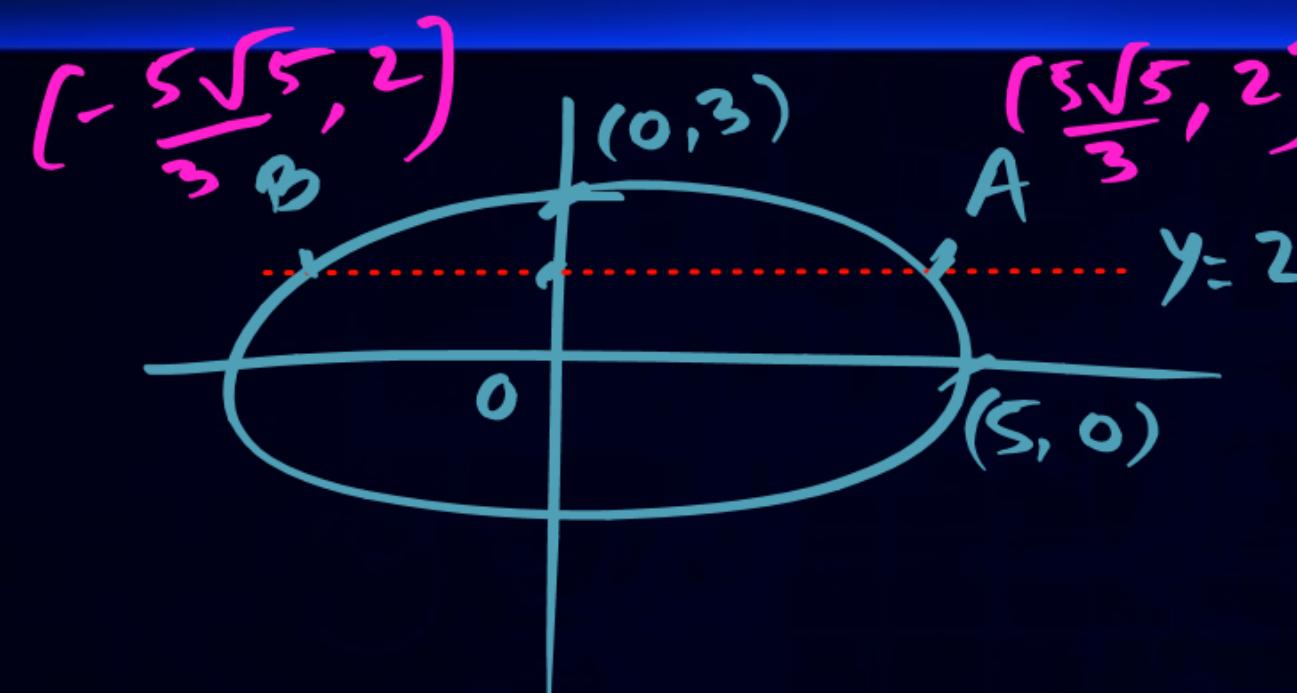
$$e = \frac{5}{4}$$

$$B^2 = A^2(1 - E^2)$$

$$B^2 = 25 \left(1 - \frac{25}{16}\right) = \frac{25 \times 5}{16}$$

$$F \left[4 \times \frac{5}{4}, 0 \right]$$

$$F (5, 0)$$



$$AB = 2 \times \frac{5\sqrt{5}}{3}$$

$$= \frac{10\sqrt{5}}{3}$$

$$\frac{x^2}{25} + \frac{y^2}{9} = 1$$

$$\frac{x^2}{25} + \frac{4}{9} = 1$$

$$\frac{x^2}{25} = \frac{5}{9}$$

$$x = \pm \frac{5\sqrt{5}}{3}$$

$\lim_{x \rightarrow 0} \frac{3 - a \sin x - b \cos x - \ln(1+x)}{3 \tan^2 x}$ is non zero finite find $2b - a$

- A 2
- B 5
- C 7 ✓
- D 9

$$2 \times 3^{-(-1)} = 7$$

$$\lim_{x \rightarrow 0} \frac{3 - a \sin x - b \cos x - \ln(1+x)}{3x^2}$$

$$b = 3 \quad \checkmark$$

$$\lim_{x \rightarrow 0} \frac{3 - a \sin x - 3 \cos x - \ln(1+x)}{3x^2}$$

$$\frac{-a \cos x + 3 \sin x - \frac{1}{1+x}}{6x} \rightarrow -a - \frac{1}{1} = 0$$

$$a = -1 \quad \checkmark$$

If $\tan^{-1} x + \tan^{-1} 2x = \frac{\pi}{4}$, then find number of solutions.

$$\tan^{-1} \left(\frac{x+2x}{1-x \cdot 2x} \right) = \pi/4$$

$$\tan^{-1} \left(\frac{3x}{1-2x^2} \right) = \pi/4$$

$$\frac{3x}{1-2x^2} = 1$$

$$3x = 1 - 2x^2$$

$$2x^2 + 3x - 1 = 0$$

①

$$x = \frac{-3 \pm \sqrt{9+4x^2}}{2x^2}$$

$$= \frac{-3 \pm \sqrt{17}}{4}$$

$$\frac{-3 + \sqrt{17}}{4}$$

+ve

$$(-\infty, \infty)$$

$$\frac{-3 - \sqrt{17}}{4}$$

-ve

Reject

If $\lim_{x \rightarrow \frac{1}{\sqrt{2}}} \frac{\sin(\cos^{-1}x) - x}{1 - \tan(\cos^{-1}x)} = \frac{-k}{\sqrt{2}}$, then the value of k is

A

2

$$\cos^{-1}x = \theta \Rightarrow x = \cos\theta$$

B

1

$$\lim_{\theta \rightarrow \pi/4} \frac{\sin\theta - \cos\theta}{1 - \tan\theta} = \frac{\sin\theta - \cos\theta}{1 - \frac{\sin\theta}{\cos\theta}} \\ = \frac{(\sin\theta - \cos\theta) \cos\theta}{(\cos\theta - \sin\theta)}$$

C

1/2

D

1/4

$$\frac{-k}{\sqrt{2}} = -\frac{1}{\sqrt{2}}$$

$K = 1$ ✓

$$\lim_{\theta \rightarrow \pi/4} -\frac{\cos\theta}{\sin\theta} = -\frac{1}{\sqrt{2}}$$

If 20th term from the end of the progression

- $20, 19\frac{1}{4}, 18\frac{1}{2}, 17\frac{3}{4}, \dots, -129\frac{1}{4}$ is
- A -120

- B -115

- C -125

- D -110

$$d = -\frac{3}{4}$$

$$a = -129\left(\frac{1}{4}\right)$$

-115

$$\begin{aligned}
 T_{20} &= a + 19d \\
 &= -129\left(\frac{1}{4}\right) + 19\left(-\frac{3}{4}\right) \\
 &= -\left[129 + \frac{1}{4}\right] + \frac{57}{4} \\
 &= -129 - \frac{1}{4} + \frac{57}{4} \\
 &= -129 + \frac{56}{4}
 \end{aligned}$$

Difference of subsets of 2 finite sets with m & n elements, is 56 then find distance between (m, n) & $(-2, -3)$.

A

10 ✓

B

16

C

14

D

None of these

$$d^2 = 8^2 + 6^2$$

$$d = \sqrt{64 + 36}$$

$$= 10$$

$$(6, 3) \& (-2, -3)$$

$$2^m - 2^n = 56$$

$$2^6 - 2^3 = 56$$

$$m = 6$$

$$n = 3$$

$$2^3 = 8$$

$$2^4 = 16$$

$$2^5 = 32$$

$$2^6 = 64$$

If α and $\frac{1}{\bar{\alpha}}$ are two complex numbers which satisfy the equations $|z - z_0|^2 = 4$ and $|z - z_0|^2 = 16$ respectively, where $z_0 = 1 + i$, then the value of $5|\alpha|^2$ is

$$\alpha \bar{\alpha} = |\alpha|^2$$

$$\frac{1}{\bar{\alpha}} = \frac{\alpha}{|\alpha|^2}$$

In $\triangle OPC$

$$\cos \theta = \frac{k^2 + 2 - 4}{2k\sqrt{2}} = \frac{k^2 - 2}{2\sqrt{2}k}$$

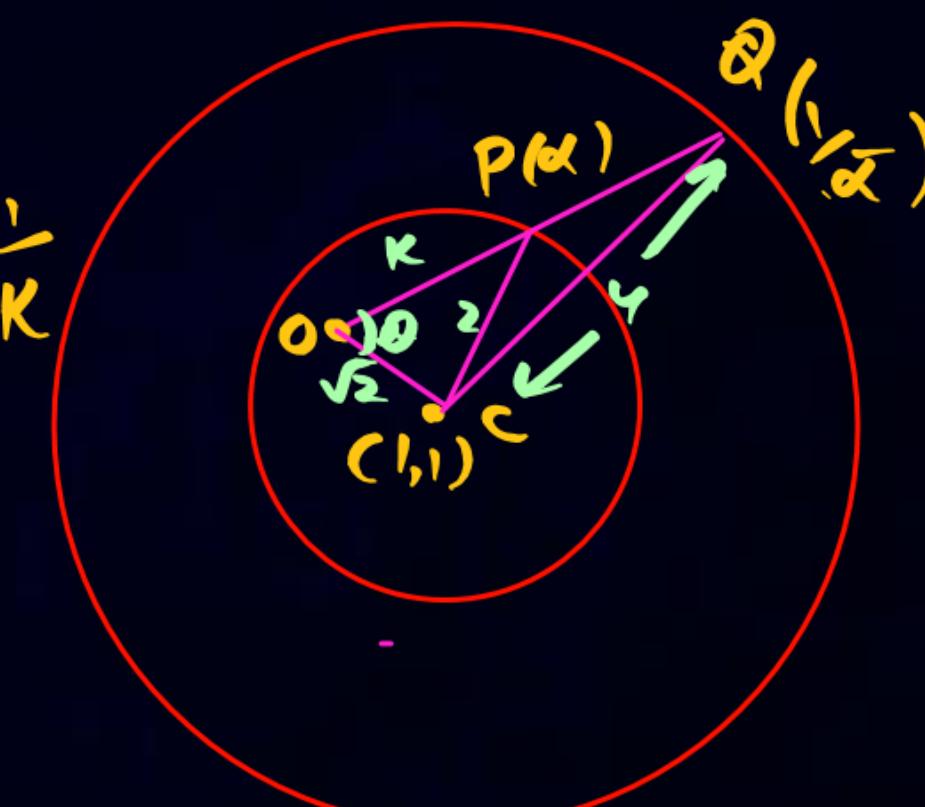
In $\triangle OQC$

$$\cos \theta = \frac{\frac{1}{k^2} + 2 - 16}{2 \cdot \frac{1}{k} \cdot \sqrt{2}} = \frac{\frac{1}{k^2} - 14}{2\sqrt{2} \cdot \frac{1}{k}}$$

$$OP = |\alpha| = k$$

$$OQ = \left| \frac{1}{\bar{\alpha}} \right|$$

$$OQ = \frac{1}{|\bar{\alpha}|} = \frac{1}{k}$$



$$(x-1)^2 + (y-1)^2 = 4$$

$$(x-1)^2 + (y-1)^2 = 16$$

$$\frac{k^2 - 2}{2\sqrt{2}k} = \frac{k^2 - 14}{2\sqrt{2} \cdot \cancel{k}}$$

$$\frac{k^2 - 2}{k} = \frac{1 - 14k^2}{\cancel{k}}$$

$$k^2 - 2 = 1 - 14k^2$$

$$15k^2 = 3$$

$$15|\alpha|^2 = 3$$

$$|\alpha|^2 = \frac{1}{5}$$

$$5|\alpha^2| = 1$$

The integral $\int \frac{(x^8 - x^2)}{(x^{12} + 3x^6 + 1) \tan^{-1}(x^3 + \frac{1}{x^3})} dx$ is equal to:

A $\frac{1}{3} \ln \left| \left(\tan^{-1} \left(x^3 + \frac{1}{x^3} \right) \right) \right| + C$

B $\ln \left| \left(\tan^{-1} \left(x^3 + \frac{1}{x^3} \right) \right) \right| + C$

C $\frac{1}{6} \ln \left| \left(\tan^{-1} \left(x^3 + \frac{1}{x^3} \right) \right) \right| + C$

D $\frac{1}{9} \ln \left| \left(\tan^{-1} \left(x^3 + \frac{1}{x^3} \right) \right) \right| + C$

$$\begin{aligned} & \text{Handwritten notes:} \\ & \text{The integral is: } \int \frac{x^8 - x^2}{x^6 \left[x^6 + 3 + \frac{1}{x^6} \right] \tan^{-1} \left(x^3 + \frac{1}{x^3} \right)} dx \\ & \quad \text{where } \left(x^3 + \frac{1}{x^3} \right)^2 + 1 = t^2 \\ & \quad \text{and } \left(3x^2 - \frac{3}{x^4} \right) dx = dt \\ & \quad \text{Also, } \tan^{-1} t = z \quad \frac{1}{t^2} dt = dz \\ & \quad \text{So, } \int \frac{dt}{t^2(t^2 + 1) \tan^{-1} t} = \frac{1}{3} \int \frac{dz}{z^2} = \frac{1}{3} \ln(\tan^{-1} t) + C \end{aligned}$$

If $2\tan^2 \theta - 5 \sec \theta = 1$ has exactly 7 solutions in $\left[0, \frac{n\pi}{2}\right]$ for least value

of $n \in \mathbb{N}$, then $\sum_{k=1}^n \frac{k}{2^n}$ is equal to $n=1 [0, \pi/2]$

A

$$\frac{9}{2^9}$$

$$\frac{1}{2^n} \sum_{K=1}^n K$$

B

$$\frac{91}{2^{13}}$$

$$\frac{1}{2^{13}} (1+2+\dots+13)$$

C

$$\frac{7}{2^7}$$

$$\frac{1}{2^{13}} \frac{13 \times 14}{2}$$

D

$$\frac{11}{2^{12}}$$

$$\frac{1}{2^{13}} (13 \times 7)$$

$$\cos \theta = \frac{1}{3}$$

$$2(\sec^2 \theta - 1) - 5 \sec \theta = 1$$

$$\sec \theta = t$$

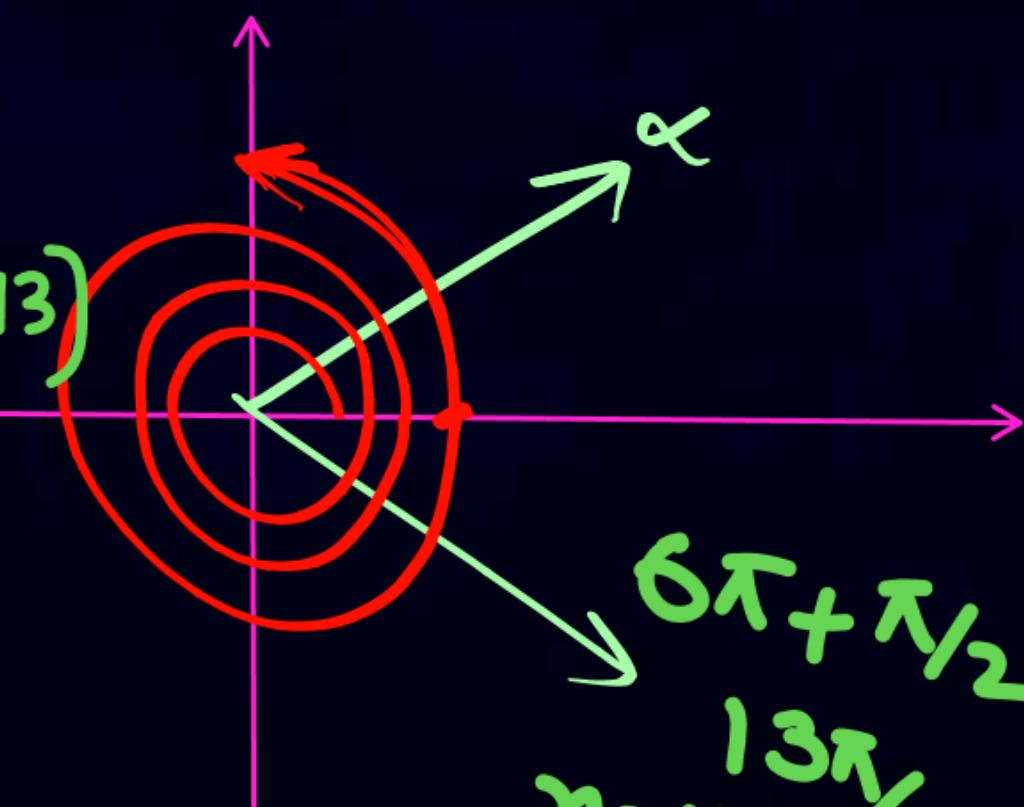
$$2t^2 - 2 - 5t = 1$$

$$2t^2 - 5t - 3 = 0$$

$$2t^2 - 6t + t - 3 = 0$$

$$(2t+1)(t-3) = 0$$

$$t = -\frac{1}{2}, t = 3$$



$$n = 13\pi/2$$

$$\sum_{k=1}^{13} \frac{k}{2^k}$$

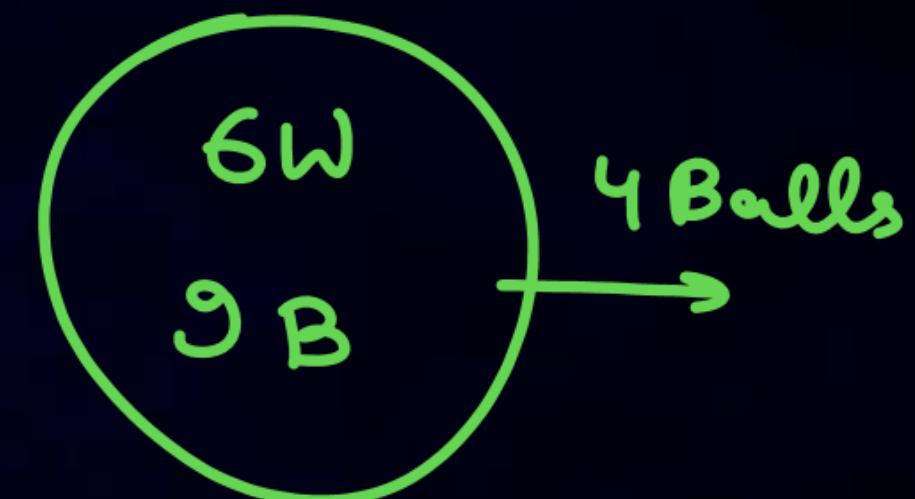
$$S = \frac{1}{2^1} + \frac{2}{2^2} + \frac{3}{2^3} + \dots + \frac{13}{2^{13}}$$

$$S_2 = -\frac{1}{2^2} + \frac{2}{2^3} - \frac{3}{2^4} + \dots + \frac{13}{2^{14}}$$

An urn contains 6 white and 9 black balls. Two successive draws of 4 balls are made without replacement. The probability that the first draw gives all white balls and second draw gives all black balls is:

- A $\frac{2}{335}$
- B $\frac{1}{495}$
- C $\frac{5}{812}$
- D $\frac{3}{715}$ ✓

$$\begin{aligned}
 &= \frac{\overset{6C_4}{\cancel{15C_4}} \times \overset{9C_4}{\cancel{11C_4}}}{\cancel{15} \times \cancel{14} \times \cancel{13} \times \cancel{12}} \times \frac{\cancel{9 \times 8 \times 7 \times 6}}{\cancel{4!}} \\
 &\quad \times \frac{1}{\cancel{13} \times \cancel{12}} \times \frac{\cancel{7 \times 6}}{\cancel{11} \times \cancel{10} \times \cancel{9} \times \cancel{8}} = \frac{3}{55 \times 13} = \frac{3}{715}
 \end{aligned}$$



The vertices of a triangle are $A(1, 2, 2)$, $B(2, 1, 2)$ & $C(2, 2, 1)$.

The perpendicular distance of its orthocentre from the given sides are ℓ_1 , ℓ_2 & ℓ_3 . Find the value of $\ell_1^2 + \ell_2^2 + \ell_3^2$. $= 3/6 = 1/2$

A 1

$$x = \frac{1}{2} \frac{\sqrt{2}}{\sqrt{3}}$$

B $\frac{1}{2}$

$$x = \frac{1}{\sqrt{6}}$$

C $\frac{1}{3}$

$$G\left(\frac{5}{3}, \frac{5}{3}, \frac{5}{3}\right)$$

D $\frac{1}{4}$

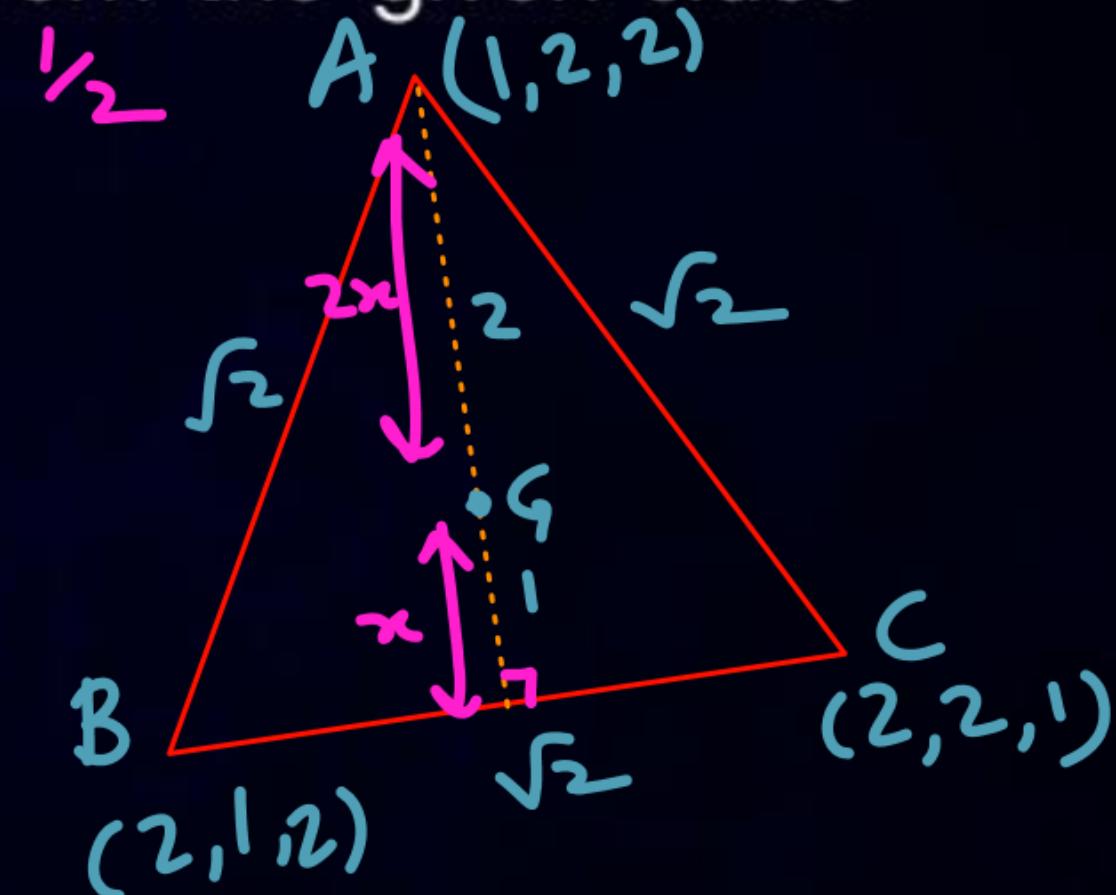
$$2x = AG$$

$$2x = \sqrt{\left(\frac{2}{3}\right)^2 + \left(\frac{1}{3}\right)^2 + \left(\frac{1}{3}\right)^2} = \sqrt{\frac{6}{9}} = \sqrt{\frac{2}{3}}$$

$$AB = \sqrt{1^2 + 1^2} = \sqrt{2}$$

$$BC = \sqrt{2}$$

$$AC = \sqrt{2}$$



If the mean of 15 observations are 12 and S.D is 3, But upon Rechecking we found that observation 12 was wrongly written as 10 if the new mean is μ and new variance is σ^2 then find the value of $15(\mu + \mu^2 + \sigma^2)$.

$$\frac{\sum x_i}{15} = 12$$

$$\sum x_i = 15 \times 12$$

$$\sum x_i = 180$$

$$\sum x_i = 180 - 10 + 12$$

$$\text{Correct sum} = 182$$

$$\mu = \frac{182}{15}$$

$$\frac{\sum x_i^2 - (12)^2}{15} = 9.$$

$$\frac{\sum x_i^2}{15} = 144 + 9$$

$$\begin{aligned}\sum x_i^2 &= 153 \times 15 \\ \text{Correct} &= 153 \times 15 - 10^2 + 12^2 \\ &= 153 \times 15 + 44\end{aligned}$$

$$\sigma^2 = \frac{\sum x_i^2}{15} - (\mu)^2$$

$$\mu^2 + \sigma^2 = \frac{\sum x_i^2}{15}$$

$$\mu + \mu^2 + \sigma^2 = \frac{153 \times 15 + 44}{15} + \frac{182}{15}$$

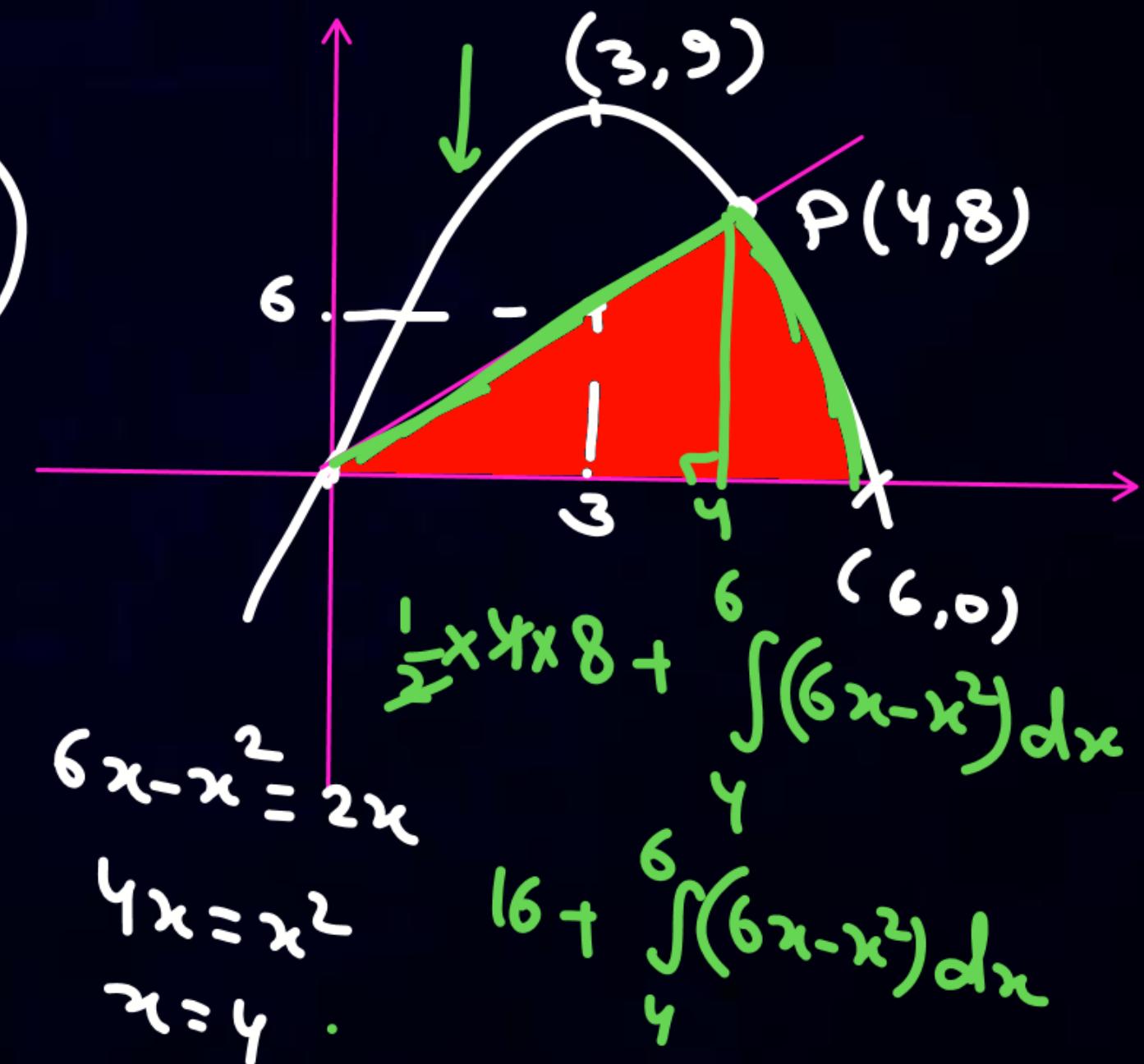
$$\text{Ans} = 153 \times 15 + 44 + 182$$

Ans 

A is the area of region $0 \leq y \leq \min(2x, 6x - x^2)$, then find $12A$.

- A 304
- B 302
- C 288
- D 312

$$\begin{aligned}
 y &= 6x - x^2 \\
 \frac{dy}{dx} &= 6 - 2x = 0 \\
 x &= 3 \\
 y &= 6 \times 3 - 3^2 \\
 &= 9 \\
 (3, 9) & \\
 y &= 2x
 \end{aligned}$$



$$16 + \int_4^6 (6x - x^2) dx$$

$$16 + \left[3x^2 - \frac{x^3}{3} \right]_4^6$$

$$16 + 3(6^2 - 4^2) - \left(\frac{6^3 - 4^3}{3} \right)$$

$$16 + 3 \times 20 - \left[\frac{216 - 64}{3} \right]$$

$$76 - \left[\frac{152}{3} \right]$$

$$A = \frac{76}{3}$$

$$\therefore A = 76 \times 4 \\ = 304$$

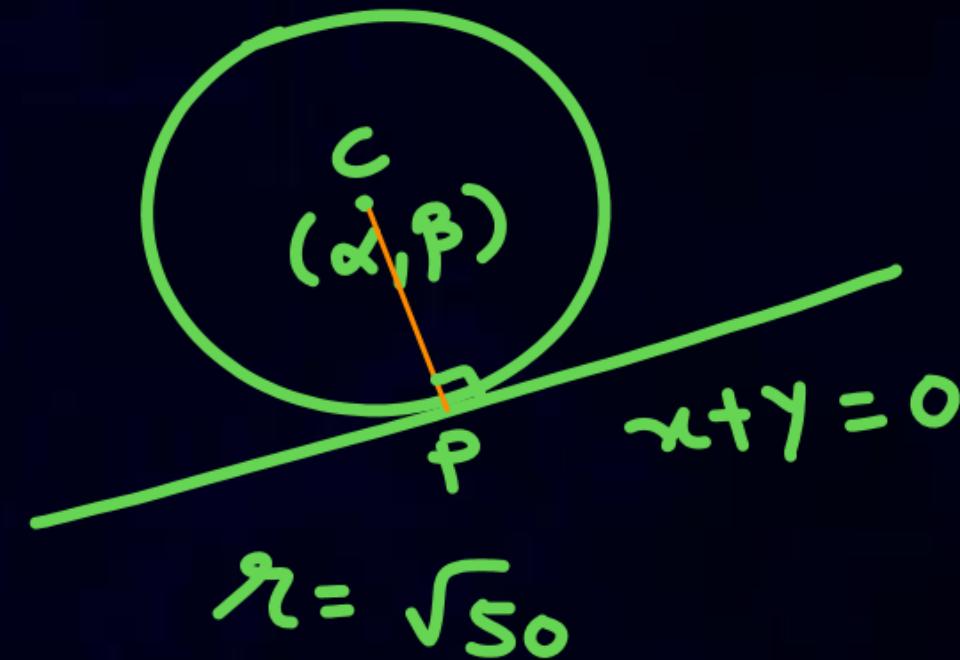
Equation of tangent to circle $(x - \alpha)^2 + (y - \beta)^2 = 50$ is $x + y = 0$.
find $(\alpha + \beta)^2$.

$$CP = r$$

$$\left| \frac{\alpha + \beta}{\sqrt{2}} \right| = \sqrt{50}$$

$$|\alpha + \beta| = \sqrt{100}$$

$$|\alpha + \beta| = 10$$



There are four boxes A_1, A_2, A_3 and A_4 . Box A_i has i cards and on each card a number is printed, the numbers are from 1 to i . A box is selected randomly, the probability of selection of box A_i is $\frac{i}{10}$ and then a card is drawn. Let E_i represents the event that a card with number ' i ' is drawn. $P(A_3/E_2)$ is equal to:

A $\frac{1}{4}$

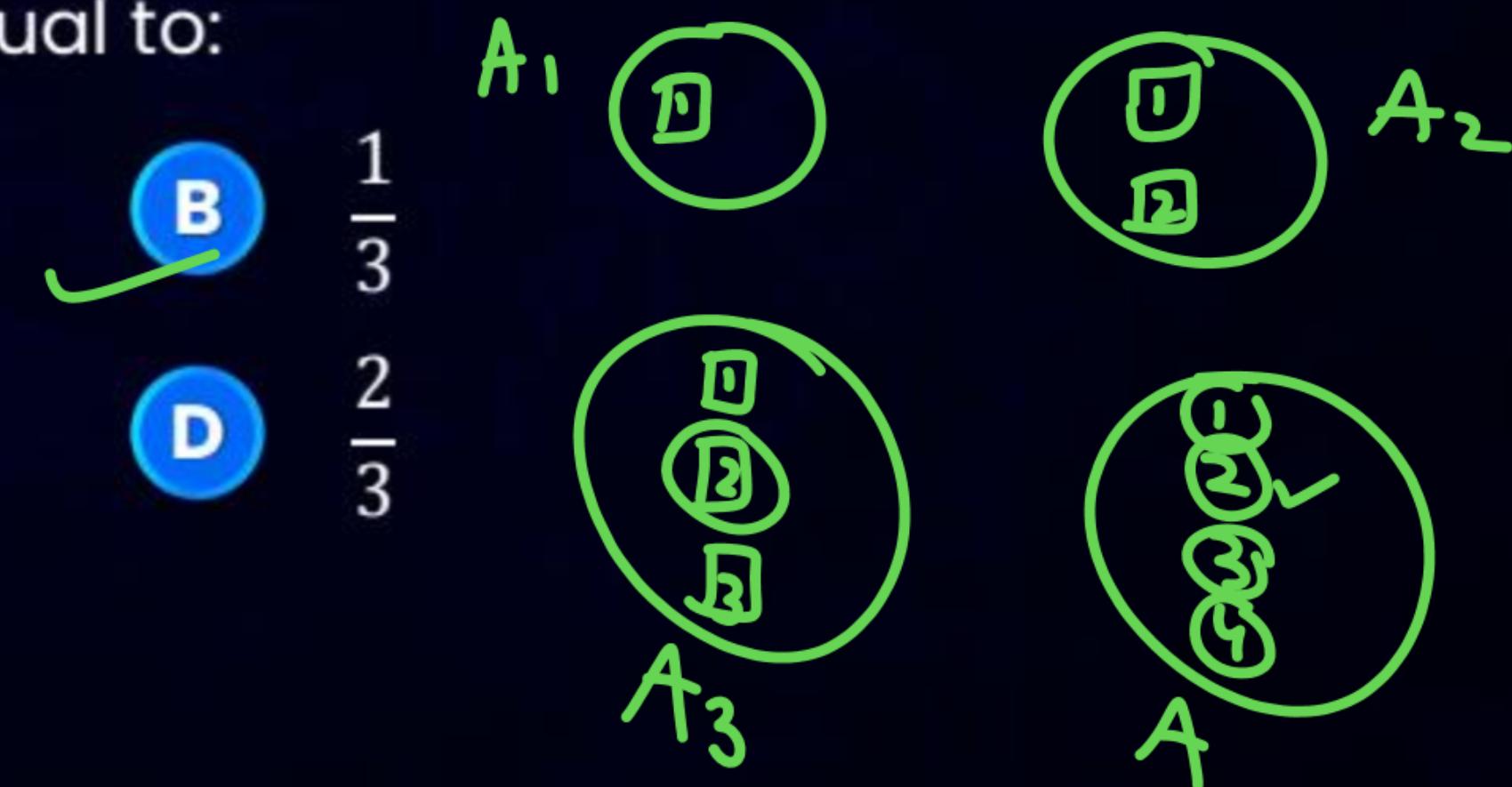
C $\frac{1}{2}$

$P(A_1) = \frac{1}{10}$

$P(A_2) = \frac{2}{10}$

$P(A_3) = \frac{3}{10}$

$P(A_4) = \frac{4}{10}$



$$P(A_3/E_2) = \frac{P(A_3 \cap E_2)}{P(E_2)}$$

$$P(E_2)$$

$$\begin{aligned} P(E_2) &= \frac{2}{10} \times \frac{1}{2} + \left(\frac{3}{10} \times \frac{1}{3} \right) + \frac{4}{10} \times \frac{1}{4} \\ &= \frac{1}{10} + \frac{1}{10} + \frac{1}{10} = \frac{3}{10} \end{aligned}$$

$$\frac{\frac{3}{10} \times \frac{1}{3}}{\frac{3}{10}} = \frac{1}{3}$$

If $\frac{dy}{dx} + xy = x^3y^3$, $y(0) = 1$, then $y(7)$ equals

- A $1/50$
- B 50
- C $1/\sqrt{50}$
- D $\sqrt{50}$

$$\frac{dy}{dx} + xy = x^3y^3$$

$$\frac{1}{y^3} \frac{dy}{dx} + xy = x^3$$

$$\frac{1}{y^2} = t$$

$$-\frac{2}{y^3} \frac{dy}{dx} = \frac{dt}{dx}$$

$$\frac{1}{y^3} \frac{dy}{dx} = -\frac{1}{2} \frac{dt}{dx}$$

$$te^{-x^2} = \int -2x^3 e^{-x^2} dx$$

$$-x^2 = z$$

$$-2x dx = dz$$

$$= \int dz (-z) e^z$$

$$= - \int z e^z dz$$

$$= -[ze^z - e^z] + C$$

$$= -e^z(z-1) + C$$

$$IF = e^{\int -2x dx} = e^{-x^2}$$

$$te^{-x^2} = -e^z(z-1) + C$$

$$\frac{1}{y^2} e^{-x^2} = -e^{-x^2}(-x^2-1) + C$$

$$\frac{e^{-x^2}}{y^2} = e^{-x^2}(x^2+1) + C$$

$$\frac{1}{y^2} = x^2 + 1$$

$$x = 7$$

$$\frac{1}{y^2} = 49 + 1$$

$$\boxed{\frac{1}{y^2} = x^2 + 1 + Ce^{x^2}}$$

$$x=0, y=1$$

$$y = 0 + 1 + Ce^0$$

$$\boxed{C=0}$$

$$y^2 = \frac{1}{50}$$

$$y = \frac{1}{\sqrt{50}}$$

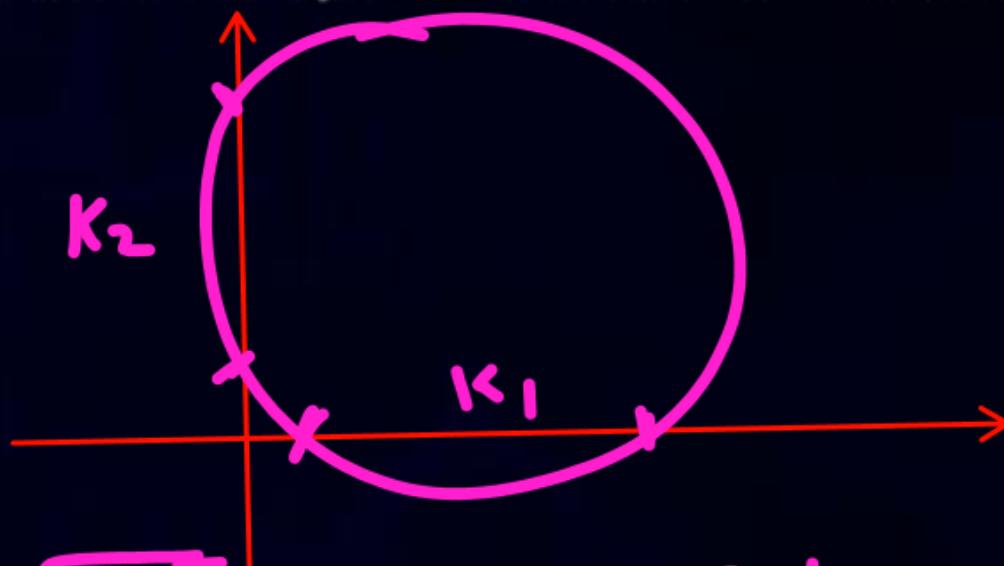
A circle cuts two perpendicular lines so that intercept on each of the line is of given length.

The locus of the centre of circle

$$\begin{aligned} -g &= h \\ -f &= k \end{aligned}$$

- A a hyperbola of eccentricity $5/4$
- B a hyperbola of eccentricity $\sqrt{2}$
- C an ellipse of eccentricity $4/5$
- D a parabola

$$x^2 - y^2 = c$$



$$2\sqrt{g^2 - c} = K_1 \Rightarrow g^2 - c = \left(\frac{K_1}{2}\right)^2$$

$$2\sqrt{f^2 - c} = K_2 \Rightarrow f^2 - c = \left(\frac{K_2}{2}\right)^2$$

$$g^2 - f^2 = \frac{K_1^2 - K_2^2}{4}$$

If $\int \frac{\sin 2x}{\sin 3x \sin 5x} dx = \frac{1}{p} \log_e |\sin 3x| - \frac{1}{q} \log_e |\sin 5x| + C$, then $|p - q|$ is equal to
 (where C is constant of integration)

A

$$1 \quad \int \frac{\sin(5x - 3x)}{\sin 3x \sin 5x} dx$$

B

$$2 \quad \frac{\sin 5x \cos 3x - \cos 5x \sin 3x}{\sin 3x \sin 5x}$$

C

$$5 \quad \int \cot 3x - \int \cot 5x$$

D

$$7 \quad \underbrace{\ln(\sin 3x)}_{3} - \underbrace{\ln(\sin 5x)}_{5}$$

$$p=3 \\ q=5$$

If $a_n = \int_0^{\pi/2} \frac{\sin^2 nx}{\sin x} dx$, then $a_2 - a_1, a_3 - a_2, a_4 - a_3$ are in

A A.P

B G.P

C H.P

D A.G.P

$$a_n = \int_0^{\pi/2} \frac{\sin^2 nx}{\sin x} dx \sim \textcircled{1}$$

$$a_{n-1} = \int_0^{\pi/2} \frac{\sin^2 (n-1)x}{\sin x} dx \sim \textcircled{2}$$

$$\begin{aligned} a_n - a_{n-1} &= \int_0^{\pi/2} \left(\frac{\sin^2 nx - \sin^2 (n-1)x}{\sin x} \right) dx \\ &\stackrel{\pi/2}{=} \int_0^{\pi/2} \frac{\sin (2n-1)x \sin x}{\sin x} dx \end{aligned}$$

$$= -\frac{\cos (2n-1)x}{(2n-1)} \Big|_0^{\pi/2}$$

$$= \frac{1 - \cos (2n-1)\pi/2}{(2n-1)} \Big|_0^{\pi/2}$$

⇒

$$a_n - a_{n-1} = \frac{1}{2n-1}$$

$$\left. \begin{aligned} a_2 - a_1 &= \frac{1}{3} \\ a_3 - a_2 &= \frac{1}{5} \\ a_4 - a_3 &= \frac{1}{7} \end{aligned} \right\}$$

A is a 2×2 matrix, I is 2×2 identity matrix. $|A - xI| = 0$ has the roots $-1, 3$. Then the sum of diagonal elements of A^2 .

$$x^2 - (\underbrace{a+d}_\text{tr A})x + \underbrace{ad-bc}_\text{|A|} = 0$$

$$x^2 - (\text{sum})x + \text{product} = 0$$

$$\text{Sum} = (a+d) = 2$$

$$\text{Product} = |A| = -3$$

$$A^2 - 2A - 3I = 0$$

$$A^2 = 2A + 3I$$

$$\begin{aligned} \text{tr}(A^2) &= 2\text{tr}A + 3\text{tr}I \\ &= 4+6 \end{aligned}$$

$$A = \begin{bmatrix} a & b \\ c & d \end{bmatrix}$$

$$xI = \begin{bmatrix} x & 0 \\ 0 & x \end{bmatrix}$$

$$A - xI = \begin{bmatrix} a-x & b \\ c & d-x \end{bmatrix}$$

$$|A - xI| = (a-x)(d-x) - bc$$

$$0 = ad + x^2 - (a+d)x - bc$$

$0 < a < 1, \int_0^\pi \frac{dx}{1-2a\cos x+a^2} = \text{value of the integral}$

A $\frac{\pi^2}{\pi+a^2}$

B $\frac{\pi}{1+a^2}$

C $\frac{\pi^2}{\pi-a^2}$

D $\frac{\pi}{1-a^2}$

$$I = \int_0^\pi \frac{dx}{1-2a\cos x+a^2} \rightarrow 0$$

$x \rightarrow \pi - x$

$$I = \int_0^\pi \frac{dx}{1+2a\cos x+a^2} \rightarrow ②$$

$$2I = \int_0^\pi \frac{1+2a\cancel{\cos x+a^2} + 1-2a\cancel{\cos x+a^2}}{(1+a^2)^2 - 4a^2 \cos^2 x} dx$$

$$\begin{aligned} I &= \int_0^\pi \frac{dx}{(1+a^2)^2 - 4a^2 \cos^2 x} \\ I &= 2 \int_0^{\pi/2} \frac{(1+a^2) dx}{(1+a^2)^2 - 4a^2 \cos^2 x} \\ &= 2 \int_0^{\pi/2} \frac{(1+a^2) \sec^2 x dx}{(1+a^2)^2 (1+\tan^2 x) - 4a^2} \\ &= 2(1+a^2) \int_{\substack{\tan x \\ 1}}^{\pi/2} \frac{\sec^2 x dx}{(1+a^2)^2 + (1+a^2)^2 \tan^2 x - 4a^2} \end{aligned}$$

$$2(1+a^2) \int \frac{\sec^2 x \, dx}{(1-a^2)^2 + (1+a^2)^2 \tan^2 x} = \left. \frac{2}{1+a^2} \cdot \frac{(1+a^2)}{1-a^2} \tan^{-1} \frac{t}{\frac{1-a^2}{1+a^2}} \right|_0^\infty$$

$$\frac{2(1+a^2)}{(1+a^2)^2} \int \frac{\sec^2 x \, dx}{\frac{(1-a^2)^2}{(1+a^2)^2} + \tan^2 x} = \left. \left(\frac{2}{1-a^2} \right) \cdot \frac{\pi}{2} \right.$$

$$\tan x = t$$

$$\frac{2}{1+a^2} \int_0^\infty \frac{dt}{\left(\frac{1-a^2}{1+a^2} \right)^2 + t^2}$$

For $x \in (0, 3)$

$$g(x) = 3f\left(\frac{x}{3}\right) + f(3-x) \text{ and } f''(x) > 0 \quad \forall x \in (0, 3),$$

If $g(x)$ is increasing in $(\alpha, 3)$ and decreasing in $(0, \alpha)$ then find α .

$$g'(x) = 3f'\left(\frac{x}{3}\right) \cdot \frac{1}{3} + f'(3-x)(-1) > 0$$

$$\text{for } \uparrow \quad f'\left(\frac{x}{3}\right) - f'(3-x) > 0 \quad \alpha = 9/4$$

$$(x/3) > (3-x)$$

$$x/3 > 3-x$$

$$4x > 9 > 9 - 3x$$

$$x > 9/4$$

Let $f: R - \left\{-\frac{1}{2}\right\} \rightarrow R$ and $g: R - \left\{-\frac{5}{2}\right\} \rightarrow R$ be defined as $f(x) = \frac{2x+3}{2x+1}$ and $g(x) = \frac{|x|+1}{2x+5}$ then the domain of the function $f(g(x))$ is: $x \rightarrow g(x)$

A

 R

B

 $R - \left\{-\frac{5}{2}\right\}$

C

 $R - \left\{-\frac{1}{2}, -\frac{5}{2}\right\}$

D

 $R - \left\{-\frac{1}{2}\right\}$

$$x \neq -\frac{5}{2}$$

$$\frac{|x|+1}{2x+5} = -\frac{1}{2}$$

$$2|x|+2 = -2x-5$$

$$x < 0 \quad 2 = -5x$$

$$x > 0$$

$$2x+2 = -2x-5$$

$$4x = -7$$

$$f(g(x)) = \frac{2g(x)+3}{2g(x)+1}$$

$$2g(x)+1 \neq 0$$

$$g(x) \neq -\frac{1}{2}$$

Values of α for which $\left| \begin{array}{ccc} 1 & \frac{3}{2} & \alpha + \frac{3}{2} \\ 1 & \frac{1}{3} & \alpha + \frac{1}{3} \\ 2\alpha + 3 & 3\alpha + 1 & 0 \end{array} \right| = 0$ lies in the interval

$$2\alpha^2 + 6\alpha + 1 = 0$$

$$\alpha = \frac{-6 \pm \sqrt{36 - 8}}{2 \times 2}$$

$$= \frac{-6 \pm \sqrt{28}}{2 \times 2}$$

$$= \frac{-6 \pm 2\sqrt{7}}{2 \times 2}$$

$$= \frac{-3 \pm \sqrt{7}}{2}$$

A (0, 3)

B (-3, 0)

C (-2, 1)

D (-2, 0)

$$C_3 \rightarrow C_3 - C_2 - \alpha C_1$$

$$\left| \begin{array}{ccc} 1 & \cancel{\frac{3}{2}} & 0 \\ 1 & \cancel{\frac{1}{3}} & 0 \\ 2\alpha + 3 & 3\alpha + 1 & -(3\alpha + 1) - \alpha(2\alpha + 3) \end{array} \right| = 0$$

$$-(3\alpha + 1) - \alpha(2\alpha + 3) - 2\alpha^2 - 6\alpha - 1 = 0$$

#

If $\frac{dy}{dx} = \frac{x+y-2}{x-y}$, and $y(0) = 2$, find $\underline{y(2)}$.

A

0

$$\frac{dy}{dx} = \frac{x+y}{x-y} \quad Y = \sqrt{x}$$

B

2

$$x \frac{dv}{dx} = \frac{1+v}{1-v} - v$$

C

e

$$x \frac{dv}{dx} = \frac{1+\sqrt{-\sqrt{+v^2}}}{1-v}$$

D

 e^2

$$\int \left(\frac{1-v}{1+v^2} \right) dv = \int \frac{dx}{x}$$

$$\tan^{-1} v - \frac{1}{2} \ln(1+v^2) = \ln x + C$$

$$\frac{dy}{dx} = \frac{a_1 x + b_1 y + c_1}{a_2 x + b_2 y + c_2}$$

$$X = x - 1$$

$$Y = y - 1$$

$$\tan^{-1} \left(\frac{Y-1}{X-1} \right) - \frac{1}{2} \ln \left(1 + \left(\frac{Y-1}{X-1} \right)^2 \right) = \ln(x-1) + C$$

$$x=0, y=2$$

$$\tan^{-1}(-1) - \frac{1}{2} \ln 2 = 0 + C$$

$$C = -\pi/4 - \frac{1}{2} \ln 2$$

$$x=2 \checkmark$$

$$\tan^{-1}\left(\frac{y-1}{2-1}\right) - \frac{1}{2} \ln\left(1 + \left(\frac{y-1}{2-1}\right)^2\right) = -\pi/4 - \frac{1}{2} \ln 2$$

$$\boxed{y=0}$$

Let $(x^2 - 4)dy = y(y - 3)dx$ satisfying $y(4) = \frac{3}{2}$ then $y(10)$ is equal to

A

$$\frac{3}{1 - 8^{\frac{1}{4}}}$$

$$\int \frac{dy}{y(y-3)} = \int \frac{dx}{x^2 - 4}$$

B

$$\frac{3}{1 + 8^{\frac{1}{4}}}$$

$$\frac{1}{3} \int \frac{y \cdot (y-3)}{y(y-3)} dy = \frac{1}{2 \times 2} \ln \left(\frac{y-2}{y+2} \right)$$

C

$$\frac{3}{1 + 2^{\frac{1}{4}}}$$

D

$$\frac{3}{1 - 2^{\frac{1}{4}}}$$

Let the image of the point $(1, a, 7)$ in the line $\frac{x}{1} = \frac{y-1}{2} = \frac{z-2}{3}$ be the point (α, β, γ) then which one of the following points lie on the line passing through (α, β, γ) then which making angles $\frac{\pi}{3}$ & $\frac{3\pi}{4}$ with y-axis and z axis respectively and an acute angle with x –axis?

- A** $(1, 2, 1 - \sqrt{2})$
- B** $(3, 4, 3 - 2\sqrt{2})$
- C** $(3, -4, 3 + 2\sqrt{2})$
- D** $(1, -2, 1 + \sqrt{2})$

If $f(x) = \max\{\sin x, \cos x, \frac{1}{2}\}$, then the area of the region bounded by the curves $y = f(x)$, x -axis, y -axis and $x = 2\pi$ is

A $\left(\frac{5\pi}{12} + 3\right)$ sq. units

B $\left(\frac{5\pi}{12} + \sqrt{2}\right)$ sq. units

C $\left(\frac{5\pi}{12} + \sqrt{3}\right)$ sq. units

D $\left(\frac{5\pi}{12} + \sqrt{2} + \sqrt{3}\right)$ sq. units

$\pi/4$

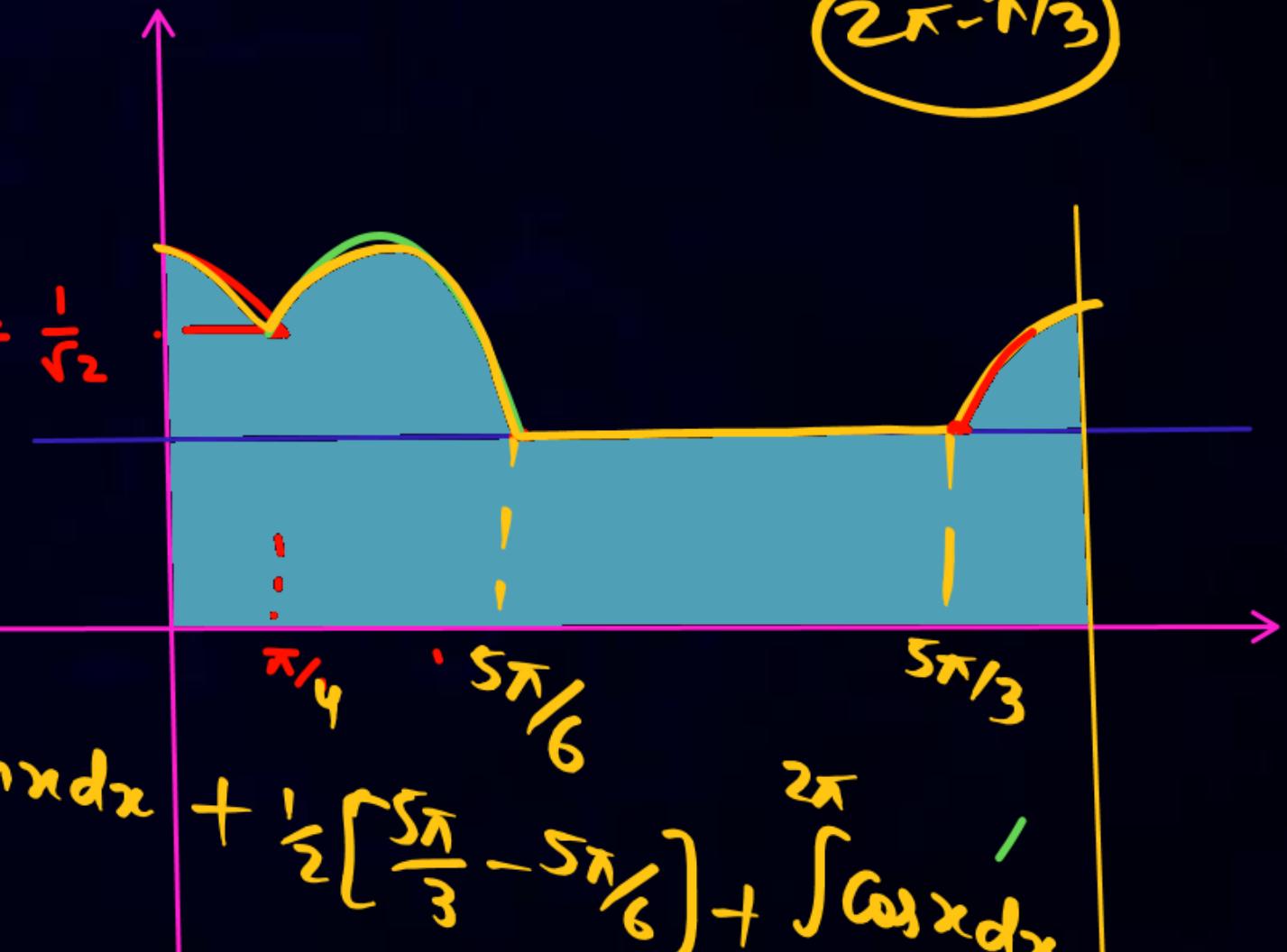
$$\int_0^{\pi/4} \cos x dx + \int_{\pi/4}^{5\pi/6} \sin x dx$$

$$+ \frac{1}{2} \left[\frac{5\pi}{3} - \frac{5\pi}{6} \right]$$

$$+ \int_{5\pi/3}^{2\pi} \cos x dx$$

$\sin x = \frac{1}{2}$

$2\pi - \pi/3$



Imp Points

Notes Revise

Paper discussion

Mock Paper



**THANK
YOU**