

NCERT Solutions for Class 9 Maths Chapter 8: Here we provide NCERT Solutions for Class 9 Maths Chapter 8 Quadrilaterals to help students prepare for their exams. These solutions provide clear explanations and step-by-step guidance on problems related to quadrilaterals making it easier for students to grasp the concepts.

By using these solutions students can practice effectively clarify their doubts and strengthen their understanding of quadrilaterals which will be beneficial for achieving better results in their exams.

NCERT Solutions for Class 9 Maths Chapter 8 Quadrilaterals Overview

These solutions for NCERT Class 9 Maths Chapter 8 Quadrilaterals are prepared by subject experts of Physics Wallah. They provide a detailed overview of quadrilaterals including their properties, types and various theorems related to them.

By following these solutions, students can gain a clear understanding of the chapter's concepts and learn to solve problems efficiently. The step-by-step guidance helps in building a strong foundation which is important for their exams.

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Below we have provided NCERT Solutions for Class 9 Maths Chapter 8 Quadrilaterals-

Question 1. The angles of the quadrilateral are in the ratio 3 : 5 : 9 : 13. Find all the angles of the quadrilateral.

Solution:

Let the angles of the quadrilateral be $3x$, $5x$, $9x$ and $13x$.

$$\therefore 3x + 5x + 9x + 13x = 360^\circ$$

[Angle sum property of a quadrilateral]

$$\Rightarrow 30x = 360^\circ$$

$$\Rightarrow x = 12^\circ$$

$$\therefore 3x = 3 \times 12^\circ = 36^\circ$$

$$5x = 5 \times 12^\circ = 60^\circ$$

$$9x = 9 \times 12^\circ = 108^\circ$$

$$13x = 13 \times 12^\circ = 156^\circ$$

\Rightarrow The required angles of the quadrilateral are 36° , 60° , 108° and 156° .

Question 2. If the diagonals of a parallelogram are equal, then show that it is a rectangle.

Solution:

Let ABCD is a parallelogram such that $AC = BD$.

In $\triangle ABC$ and $\triangle DCB$,

$AC = DB$ [Given]

$AB = DC$ [Opposite sides of a parallelogram]

$BC = CB$ [Common]

$\therefore \triangle ABC \cong \triangle DCB$ [By SSS congruency]

$\Rightarrow \angle ABC = \angle DCB$ [By C.P.C.T.] ... (1)

Now, $AB \parallel DC$ and BC is a transversal. [\because ABCD is a parallelogram]

$\therefore \angle ABC + \angle DCB = 180^\circ$... (2) [Co-interior angles]

From (1) and (2), we have

$$\angle ABC = \angle DCB = 90^\circ$$

i.e., ABCD is a parallelogram having an angle equal to 90° .

\therefore ABCD is a rectangle.

Question 3. Show that if the diagonals of a quadrilateral bisect each other at right angles, then it is a rhombus.

Solution:

Let ABCD be a quadrilateral such that the diagonals AC and BD bisect each other at right angles at O.

\therefore In $\triangle AOB$ and $\triangle AOD$, we have

$AO = AO$ [Common]

$OB = OD$ [O is the mid-point of BD]

$\angle AOB = \angle AOD$ [Each 90°]

$\therefore \triangle AOB \cong \triangle AOD$ [By SAS congruency]

$\therefore AB = AD$ [By C.P.C.T.](1)

Similarly, $AB = BC \dots (2)$

$BC = CD \dots (3)$

$CD = DA \dots (4)$

\therefore From (1), (2), (3) and (4), we have

$AB = BC = CD = DA$

Thus, the quadrilateral ABCD is a rhombus.

Alternatively : ABCD can be proved first a parallelogram then proving one pair of adjacent sides equal will result in rhombus.

Question 4. Show that the diagonals of a square are equal and bisect each other at right angles.

Solution:

Let ABCD be a square such that its diagonals AC and BD intersect at O.

(i) To prove that the diagonals are equal, we need to prove $AC = BD$.

In $\triangle ABC$ and $\triangle BAD$, we have

$AB = BA$ [Common]

$BC = AD$ [Sides of a square ABCD]

$\angle ABC = \angle BAD$ [Each angle is 90°]

$\therefore \triangle ABC \cong \triangle BAD$ [By SAS congruency]

$AC = BD$ [By C.P.C.T.] ... (1)

(ii) $AD \parallel BC$ and AC is a transversal. [\because A square is a parallelogram]

$\therefore \angle 1 = \angle 3$

[Alternate interior angles are equal]

Similarly, $\angle 2 = \angle 4$

Now, in $\triangle OAD$ and $\triangle OCB$, we have

$AD = CB$ [Sides of a square ABCD]

$\angle 1 = \angle 3$ [Proved]

$\angle 2 = \angle 4$ [Proved]

$\therefore \triangle OAD \cong \triangle OCB$ [By ASA congruency]

$\Rightarrow OA = OC$ and $OD = OB$ [By C.P.C.T.]

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NCERT Solutions for Class 9 Maths Chapter 8

Quadrilaterals Overview

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NCERT Solutions for Class 9 Maths Chapter 8 Exercise 8.1

Below we have provided NCERT Solutions for Class 9 Maths Chapter 8 Quadrilaterals-

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1. The angles of a quadrilateral are in the ratio 3 : 5 : 9 : 13. Find all the angles of the quadrilateral.

Solution:

Let the common ratio between the angles be x .

We know that the sum of the interior angles of the quadrilateral = 360°

Now,

$$3x + 5x + 9x + 13x = 360^\circ$$

$$\Rightarrow 30x = 360^\circ$$

$$\Rightarrow x = 12^\circ$$

, Angles of the quadrilateral are:

$$3x = 3 \times 12^\circ = 36^\circ$$

$$5x = 5 \times 12^\circ = 60^\circ$$

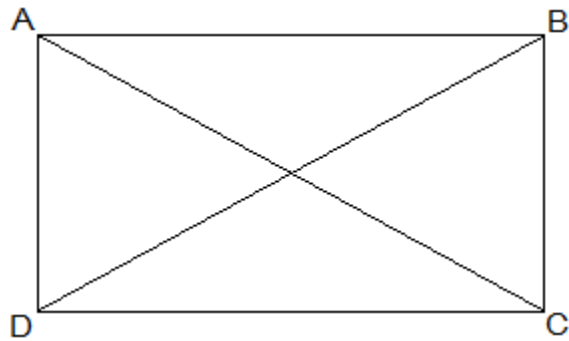
$$9x = 9 \times 12^\circ = 108^\circ$$

$$13x = 13 \times 12^\circ = 156^\circ$$

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2. If the diagonals of a parallelogram are equal, then show that it is a rectangle.

Solution:



Given that,

$$AC = BD$$

To show that ABCD is a rectangle if the diagonals of a parallelogram are equal

To show ABCD is a rectangle, we have to prove that one of its interior angles is right-angled.

Proof,

In $\triangle ABC$ and $\triangle BAD$,

$$AB = BA \text{ (Common)}$$

$$BC = AD \text{ (Opposite sides of a parallelogram are equal)}$$

$$AC = BD \text{ (Given)}$$

Therefore, $\triangle ABC \cong \triangle BAD$ [SSS congruency]

$\angle A = \angle B$ [Corresponding parts of Congruent Triangles]

also,

$\angle A + \angle B = 180^\circ$ (Sum of the angles on the same side of the transversal)

$$\Rightarrow 2\angle A = 180^\circ$$

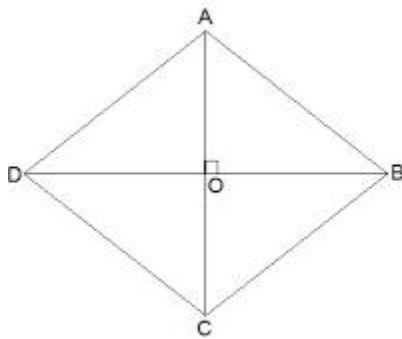
$$\Rightarrow \angle A = 90^\circ = \angle B$$

Therefore, ABCD is a rectangle.

Hence Proved

3. Show that if the diagonals of a quadrilateral bisect each other at right angles, then it is a rhombus.

Solution:



Let ABCD be a quadrilateral whose diagonals bisect each other at right angles.

Given that,

$$OA = OC$$

$$OB = OD$$

$$\text{and } \angle AOB = \angle BOC = \angle OCD = \angle ODA = 90^\circ$$

To show that if the diagonals of a quadrilateral bisect each other at right angles, then it is a rhombus, we have to prove that ABCD is a parallelogram and $AB = BC = CD = AD$

Proof,

In $\triangle AOB$ and $\triangle COB$,

$$OA = OC \text{ (Given)}$$

$\angle AOB = \angle COB$ (Opposite sides of a parallelogram are equal)

$OB = OB$ (Common)

Therefore, $\triangle AOB \cong \triangle COB$ [SAS congruency]

Thus, $AB = BC$ [CPCT]

Similarly, we can prove,

$BC = CD$

$CD = AD$

$AD = AB$

, $AB = BC = CD = AD$

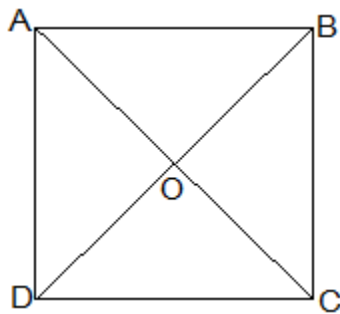
Opposite sides of a quadrilateral are equal. Hence, it is a parallelogram.

ABCD is rhombus as it is a parallelogram whose diagonals intersect at a right angle.

Hence Proved.

4. Show that the diagonals of a square are equal and bisect each other at right angles.

Solution:



Let ABCD be a square and its diagonals AC and BD intersect each other at O.

To show that,

$AC = BD$

$AO = OC$

and $\angle AOB = 90^\circ$

Proof,

In $\triangle ABC$ and $\triangle BAD$,

$AB = BA$ (Common)

$\angle ABC = \angle BAD = 90^\circ$

$BC = AD$ (Given)

$\triangle ABC \cong \triangle BAD$ [SAS congruency]

Thus,

$AC = BD$ [CPCT]

diagonals are equal.

Now,

In $\triangle AOB$ and $\triangle COD$,

$\angle BAO = \angle DCO$ (Alternate interior angles)

$\angle AOB = \angle COD$ (Vertically opposite)

$AB = CD$ (Given)

, $\triangle AOB \cong \triangle COD$ [AAS congruency]

Thus,

$AO = CO$ [CPCT].

, Diagonal bisect each other.

Now,

In $\triangle AOB$ and $\triangle COB$,

$OB = OB$ (Given)

$AO = CO$ (diagonals are bisected)

$AB = CB$ (Sides of the square)

, $\triangle AOB \cong \triangle COB$ [SSS congruency]

also, $\angle AOB = \angle COB$

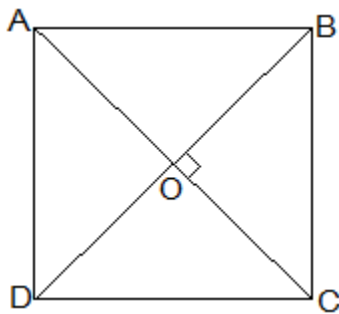
$\angle AOB + \angle COB = 180^\circ$ (Linear pair)

Thus, $\angle AOB = \angle COB = 90^\circ$

, Diagonals bisect each other at right angles

5. Show that if the diagonals of a quadrilateral are equal and bisect each other at right angles, then it is a square.

Solution:



Given that,

Let ABCD be a quadrilateral and its diagonals AC and BD bisect each other at a right angle at O.

To prove that,

The Quadrilateral ABCD is a square.

Proof,

In $\triangle AOB$ and $\triangle COD$,

$AO = CO$ (Diagonals bisect each other)

$\angle AOB = \angle COD$ (Vertically opposite)

$OB = OD$ (Diagonals bisect each other)

, $\triangle AOB \cong \triangle COD$ [SAS congruency]

Thus,

$AB = CD$ [CPCT] — (i)

also,

$$\angle OAB = \angle OCD \text{ (Alternate interior angles)}$$

$$\Rightarrow AB \parallel CD$$

Now,

In $\triangle AOD$ and $\triangle COD$,

$$AO = CO \text{ (Diagonals bisect each other)}$$

$$\angle AOD = \angle COD \text{ (Vertically opposite)}$$

$$OD = OD \text{ (Common)}$$

$$\therefore \triangle AOD \cong \triangle COD \text{ [SAS congruency]}$$

Thus,

$$AD = CD \text{ [CPCT]} \text{ — (ii)}$$

also,

$$AD = BC \text{ and } AD = CD$$

$$\Rightarrow AD = BC = CD = AB \text{ — (ii)}$$

$$\text{also, } \angle ADC = \angle BCD \text{ [CPCT]}$$

$$\text{and } \angle ADC + \angle BCD = 180^\circ \text{ (co-interior angles)}$$

$$\Rightarrow 2\angle ADC = 180^\circ$$

$$\Rightarrow \angle ADC = 90^\circ \text{ — (iii)}$$

One of the interior angles is a right angle.

Thus, from (i), (ii) and (iii), given quadrilateral ABCD is a square.

Hence Proved.

6. Diagonal AC of a parallelogram ABCD bisects $\angle A$ (see Fig. 8.19). Show that

(i) it bisects $\angle C$ also,

(ii) ABCD is a rhombus.

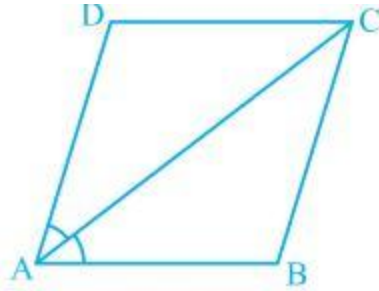


Fig. 8.19

Solution:

(i) In $\triangle ADC$ and $\triangle CBA$,

$AD = CB$ (Opposite sides of a parallelogram)

$DC = BA$ (Opposite sides of a parallelogram)

$AC = CA$ (Common Side)

, $\triangle ADC \cong \triangle CBA$ [SSS congruency]

Thus,

$\angle ACD = \angle CAB$ by CPCT

and $\angle CAB = \angle CAD$ (Given)

$\Rightarrow \angle ACD = \angle BCA$

Thus,

AC bisects $\angle C$ also.

(ii) $\angle ACD = \angle CAD$ (Proved above)

$\Rightarrow AD = CD$ (Opposite sides of equal angles of a triangle are equal)

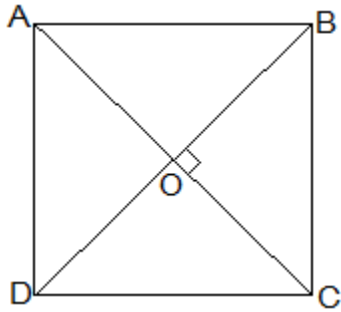
Also, $AB = BC = CD = DA$ (Opposite sides of a parallelogram)

Thus,

ABCD is a rhombus.

7. ABCD is a rhombus. Show that diagonal AC bisects $\angle A$ as well as $\angle C$ and diagonal BD bisects $\angle B$ as well as $\angle D$.

Solution:



Given that,

ABCD is a rhombus.

AC and BD are its diagonals.

Proof,

$AD = CD$ (Sides of a rhombus)

$\angle DAC = \angle DCA$ (Angles opposite of equal sides of a triangle are equal.)

also, $AB \parallel CD$

$\Rightarrow \angle DAC = \angle BCA$ (Alternate interior angles)

$\Rightarrow \angle DCA = \angle BCA$

, AC bisects $\angle C$.

Similarly,

We can prove that diagonal AC bisects $\angle A$.

Following the same method,

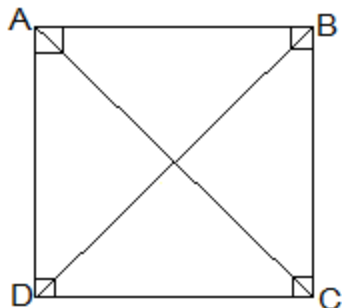
We can prove that the diagonal BD bisects $\angle B$ and $\angle D$.

8. ABCD is a rectangle in which diagonal AC bisects $\angle A$ as well as $\angle C$. Show that:

(i) ABCD is a square

(ii) Diagonal BD bisects $\angle B$ as well as $\angle D$.

Solution:



(i) $\angle DAC = \angle DCA$ (AC bisects $\angle A$ as well as $\angle C$)

$\Rightarrow AD = CD$ (Sides opposite to equal angles of a triangle are equal)

also, $CD = AB$ (Opposite sides of a rectangle)

, $AB = BC = CD = AD$

Thus, ABCD is a square.

(ii) In $\triangle BCD$,

$BC = CD$

$\Rightarrow \angle CDB = \angle CBD$ (Angles opposite to equal sides are equal)

also, $\angle CDB = \angle ABD$ (Alternate interior angles)

$\Rightarrow \angle CBD = \angle ABD$

Thus, BD bisects $\angle B$

Now,

$\angle CBD = \angle ADB$

$\Rightarrow \angle CDB = \angle ADB$

Thus, BD bisects $\angle B$ as well as $\angle D$.

9. In parallelogram ABCD, two points P and Q are taken on diagonal BD such that $DP = BQ$ (see Fig. 8.20). Show that:

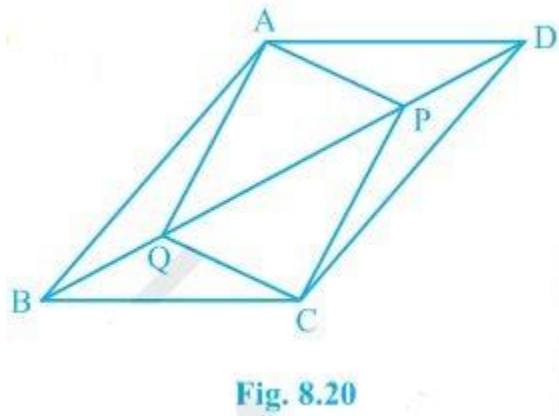
(i) $\triangle APD \cong \triangle CQB$

(ii) $AP = CQ$

(iii) $\triangle AQB \cong \triangle CPD$

(iv) $AQ = CP$

(v) $APCQ$ is a parallelogram



Solution:

(i) In $\triangle APD$ and $\triangle CQB$,

$DP = BQ$ (Given)

$\angle ADP = \angle CBQ$ (Alternate interior angles)

$AD = BC$ (Opposite sides of a parallelogram)

Thus, $\triangle APD \cong \triangle CQB$ [SAS congruency]

(ii) $AP = CQ$ by CPCT as $\triangle APD \cong \triangle CQB$.

(iii) In $\triangle AQB$ and $\triangle CPD$,

$BQ = DP$ (Given)

$\angle ABQ = \angle CDP$ (Alternate interior angles)

$AB = CD$ (Opposite sides of a parallelogram)

Thus, $\triangle AQB \cong \triangle CPD$ [SAS congruency]

(iv) As $\triangle AQB \cong \triangle CPD$

$AQ = CP$ [CPCT]

(v) From the questions (ii) and (iv), it is clear that $APCQ$ has equal opposite sides and also has equal and opposite angles. , $APCQ$ is a parallelogram.

10. ABCD is a parallelogram and AP and CQ are perpendiculars from vertices A and C on diagonal BD (see Fig. 8.21). Show that

(i) $\triangle APB \cong \triangle CQD$

(ii) $AP = CQ$

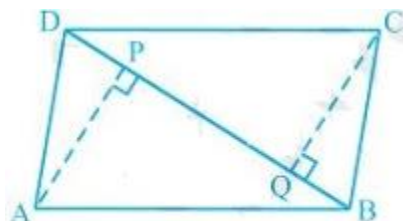


Fig. 8.21

Solution:

(i) In $\triangle APB$ and $\triangle CQD$,

$\angle ABP = \angle CDQ$ (Alternate interior angles)

$\angle APB = \angle CQD$ ($= 90^\circ$ as AP and CQ are perpendiculars)

$AB = CD$ (ABCD is a parallelogram)

, $\triangle APB \cong \triangle CQD$ [AAS congruency]

(ii) As $\triangle APB \cong \triangle CQD$.

, $AP = CQ$ [CPCT]

11. In $\triangle ABC$ and $\triangle DEF$, $AB = DE$, $AB \parallel DE$, $BC = EF$ and $BC \parallel EF$. Vertices A, B and C are joined to vertices D, E and F, respectively (see Fig. 8.22).

Show that

(i) quadrilateral ABED is a parallelogram

(ii) quadrilateral BEFC is a parallelogram

(iii) $AD \parallel CF$ and $AD = CF$

(iv) quadrilateral ACFD is a parallelogram

(v) $AC = DF$

(vi) $\triangle ABC \cong \triangle DEF$.

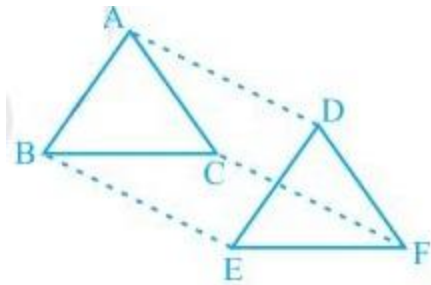


Fig. 8.22

Solution:

(i) $AB = DE$ and $AB \parallel DE$ (Given)

Two opposite sides of a quadrilateral are equal and parallel to each other.

Thus, quadrilateral ABED is a parallelogram

(ii) Again $BC = EF$ and $BC \parallel EF$.

Thus, quadrilateral BEFC is a parallelogram.

(iii) Since ABED and BEFC are parallelograms.

$\Rightarrow AD = BE$ and $BE = CF$ (Opposite sides of a parallelogram are equal)

, $AD = CF$.

Also, $AD \parallel BE$ and $BE \parallel CF$ (Opposite sides of a parallelogram are parallel)

, $AD \parallel CF$

(iv) AD and CF are opposite sides of quadrilateral ACFD which are equal and parallel to each other. Thus, it is a parallelogram.

(v) Since ACFD is a parallelogram

$AC \parallel DF$ and $AC = DF$

(vi) In $\triangle ABC$ and $\triangle DEF$,

$AB = DE$ (Given)

$BC = EF$ (Given)

$AC = DF$ (Opposite sides of a parallelogram)

, $\triangle ABC \cong \triangle DEF$ [SSS congruency]

12. ABCD is a trapezium in which $AB \parallel CD$ and $AD = BC$ (see Fig. 8.23). Show that

(i) $\angle A = \angle B$

(ii) $\angle C = \angle D$

(iii) $\triangle ABC \cong \triangle BAD$

(iv) diagonal $AC =$ diagonal BD

[Hint: Extend AB and draw a line through C parallel to DA intersecting AB produced at E.]

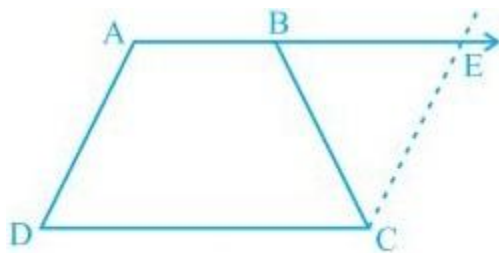


Fig. 8.23

Solution:

To Construct: Draw a line through C parallel to DA intersecting AB produced at E.

(i) $CE = AD$ (Opposite sides of a parallelogram)

$AD = BC$ (Given)

, $BC = CE$

$\Rightarrow \angle CBE = \angle CEB$

also,

$\angle A + \angle CBE = 180^\circ$ (Angles on the same side of transversal and $\angle CBE = \angle CEB$)

$\angle B + \angle CBE = 180^\circ$ (As Linear pair)

$\Rightarrow \angle A = \angle B$

(ii) $\angle A + \angle D = \angle B + \angle C = 180^\circ$ (Angles on the same side of transversal)

$\Rightarrow \angle A + \angle D = \angle A + \angle C$ ($\angle A = \angle B$)

$$\Rightarrow \angle D = \angle C$$

(iii) In $\triangle ABC$ and $\triangle BAD$,

$$AB = AB \text{ (Common)}$$

$$\angle DBA = \angle CBA$$

$$AD = BC \text{ (Given)}$$

, $\triangle ABC \cong \triangle BAD$ [SAS congruency]

(iv) Diagonal $AC =$ diagonal BD by CPCT as $\triangle ABC \cong \triangle BAD$.

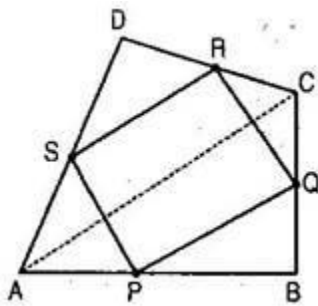
NCERT Solutions for Class 9 Maths Chapter 8 Exercise 8.1 Page: 150

1. ABCD is a quadrilateral in which P, Q, R and S are mid-points of the sides AB, BC, CD and DA (see Fig 8.29). AC is a diagonal. Show that:

(i) $SR \parallel AC$ and $SR = \frac{1}{2} AC$

(ii) $PQ = SR$

(iii) PQRS is a parallelogram.



Solution:

(i) In $\triangle DAC$,

R is the mid point of DC and S is the mid point of DA.

Thus by mid point theorem, $SR \parallel AC$ and $SR = \frac{1}{2} AC$

(ii) In $\triangle BAC$,

P is the mid point of AB and Q is the mid point of BC.

Thus by mid point theorem, $PQ \parallel AC$ and $PQ = \frac{1}{2} AC$

also, $SR = \frac{1}{2} AC$

, $PQ = SR$

(iii) $SR \parallel AC$ ————— from question (i)

and, $PQ \parallel AC$ ————— from question (ii)

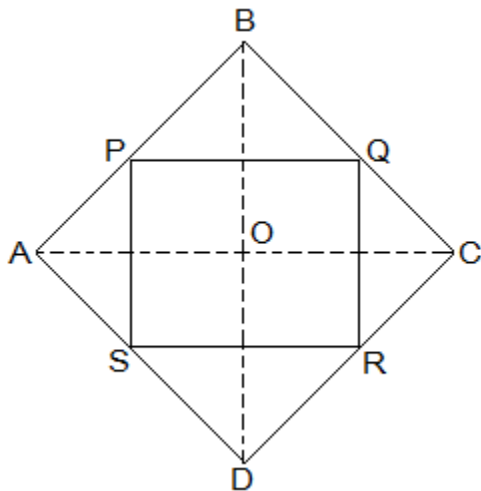
$\Rightarrow SR \parallel PQ$ – from (i) and (ii)

also, $PQ = SR$

, PQRS is a parallelogram.

2. ABCD is a rhombus and P, Q, R and S are the mid-points of the sides AB, BC, CD and DA, respectively. Show that the quadrilateral PQRS is a rectangle.

Solution:



Given in the question,

ABCD is a rhombus and P, Q, R and S are the mid-points of the sides AB, BC, CD and DA, respectively.

To Prove,

PQRS is a rectangle.

Construction,

Join AC and BD.

Proof:

In $\triangle DRS$ and $\triangle BPQ$,

$DS = BQ$ (Halves of the opposite sides of the rhombus)

$\angle SDR = \angle QBP$ (Opposite angles of the rhombus)

$DR = BP$ (Halves of the opposite sides of the rhombus)

, $\triangle DRS \cong \triangle BPQ$ [SAS congruency]

$RS = PQ$ [CPCT]————— (i)

In $\triangle QCR$ and $\triangle SAP$,

$RC = PA$ (Halves of the opposite sides of the rhombus)

$\angle RCQ = \angle PAS$ (Opposite angles of the rhombus)

$CQ = AS$ (Halves of the opposite sides of the rhombus)

, $\triangle QCR \cong \triangle SAP$ [SAS congruency]

$RQ = SP$ [CPCT]————— (ii)

Now,

In $\triangle CDB$,

R and Q are the mid points of CD and BC, respectively.

$\Rightarrow QR \parallel BD$

also,

P and S are the mid points of AD and AB, respectively.

$\Rightarrow PS \parallel BD$

$\Rightarrow QR \parallel PS$

, PQRS is a parallelogram.

also, $\angle PQR = 90^\circ$

Now,

In PQRS,

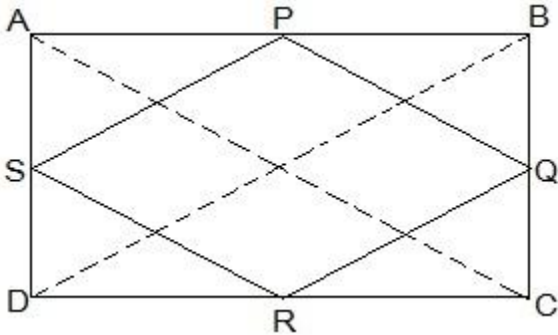
$RS = PQ$ and $RQ = SP$ from (i) and (ii)

$$\angle Q = 90^\circ$$

, PQRS is a rectangle.

3. ABCD is a rectangle and P, Q, R and S are mid-points of the sides AB, BC, CD and DA, respectively. Show that the quadrilateral PQRS is a rhombus.

Solution:



Given in the question,

ABCD is a rectangle and P, Q, R and S are mid-points of the sides AB, BC, CD and DA, respectively.

Construction,

Join AC and BD.

To Prove,

PQRS is a rhombus.

Proof:

In $\triangle ABC$

P and Q are the mid-points of AB and BC, respectively

, $PQ \parallel AC$ and $PQ = \frac{1}{2} AC$ (Midpoint theorem) — (i)

In $\triangle ADC$,

$SR \parallel AC$ and $SR = \frac{1}{2} AC$ (Midpoint theorem) — (ii)

So, $PQ \parallel SR$ and $PQ = SR$

As in quadrilateral PQRS one pair of opposite sides is equal and parallel to each other, so, it is a parallelogram.

, $PS \parallel QR$ and $PS = QR$ (Opposite sides of parallelogram) — (iii)

Now,

In $\triangle BCD$,

Q and R are mid points of side BC and CD, respectively.

, $QR \parallel BD$ and $QR = \frac{1}{2} BD$ (Midpoint theorem) — (iv)

$AC = BD$ (Diagonals of a rectangle are equal) — (v)

From equations (i), (ii), (iii), (iv) and (v),

$PQ = QR = SR = PS$

So, PQRS is a rhombus.

Hence Proved

4. ABCD is a trapezium in which $AB \parallel DC$, BD is a diagonal and E is the mid-point of AD. A line is drawn through E parallel to AB intersecting BC at F (see Fig. 8.30). Show that F is the mid-point of BC.

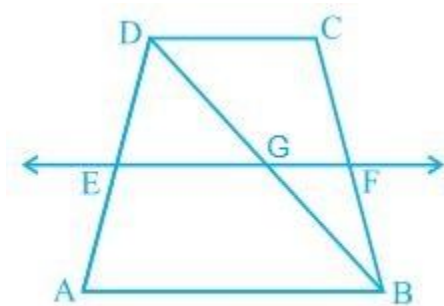


Fig. 8.30

Solution:

Given that,

ABCD is a trapezium in which $AB \parallel DC$, BD is a diagonal and E is the mid-point of AD.

To prove,

F is the mid-point of BC.

Proof,

BD intersected EF at G.

In $\triangle BAD$,

E is the mid point of AD and also $EG \parallel AB$.

Thus, G is the mid point of BD (Converse of mid point theorem)

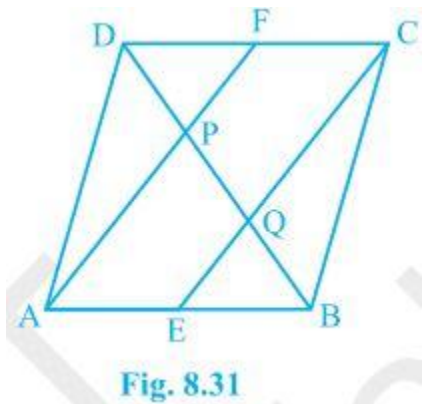
Now,

In $\triangle BDC$,

G is the mid point of BD and also $GF \parallel AB \parallel DC$.

Thus, F is the mid point of BC (Converse of mid point theorem)

5. In a parallelogram ABCD, E and F are the mid-points of sides AB and CD, respectively (see Fig. 8.31). Show that the line segments AF and EC trisect the diagonal BD.



Solution:

Given that,

ABCD is a parallelogram. E and F are the mid-points of sides AB and CD, respectively.

To show,

AF and EC trisect the diagonal BD.

Proof,

ABCD is a parallelogram

, $AB \parallel CD$

also, $AE \parallel FC$

Now,

$AB = CD$ (Opposite sides of parallelogram ABCD)

$$\Rightarrow \frac{1}{2} AB = \frac{1}{2} CD$$

$\Rightarrow AE = FC$ (E and F are midpoints of side AB and CD)

AECF is a parallelogram (AE and CF are parallel and equal to each other)

$AF \parallel EC$ (Opposite sides of a parallelogram)

Now,

In $\triangle DQC$,

F is mid point of side DC and $FP \parallel CQ$ (as $AF \parallel EC$).

P is the mid-point of DQ (Converse of mid-point theorem)

$$\Rightarrow DP = PQ \text{ — (i)}$$

Similarly,

In $\triangle APB$,

E is midpoint of side AB and $EQ \parallel AP$ (as $AF \parallel EC$).

Q is the mid-point of PB (Converse of mid-point theorem)

$$\Rightarrow PQ = QB \text{ — (ii)}$$

From equations (i) and (ii),

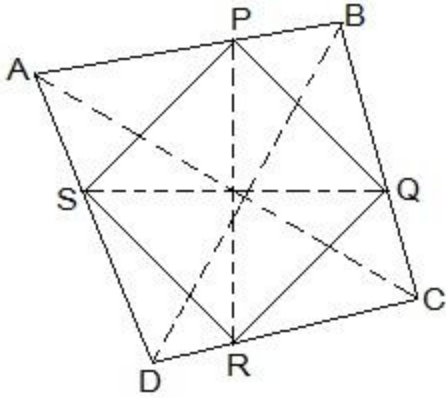
$$DP = PQ = BQ$$

Hence, the line segments AF and EC trisect the diagonal BD.

Hence Proved.

6. Show that the line segments joining the mid-points of the opposite sides of a quadrilateral bisect each other.

Solution:



Let ABCD be a quadrilateral and P, Q, R and S the mid points of AB, BC, CD and DA, respectively.

Now,

In $\triangle ACD$,

R and S are the mid points of CD and DA, respectively.

, $SR \parallel AC$.

Similarly we can show that,

$PQ \parallel AC$,

$PS \parallel BD$ and

$QR \parallel BD$

, PQRS is parallelogram.

PR and QS are the diagonals of the parallelogram PQRS. So, they will bisect each other.

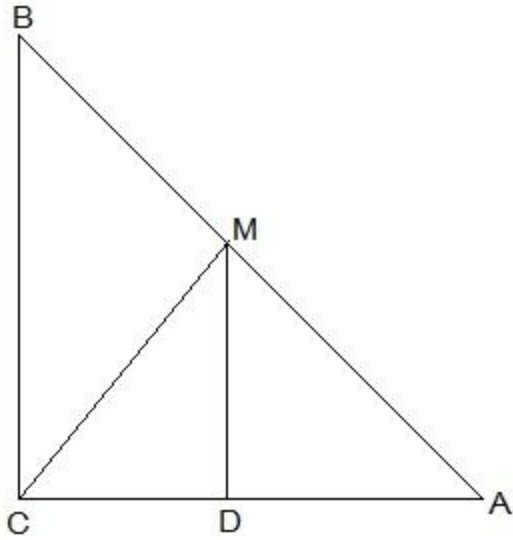
7. ABC is a triangle right angled at C. A line through the mid-point M of hypotenuse AB and parallel to BC intersects AC at D. Show that

(i) D is the mid-point of AC

(ii) $MD \perp AC$

(iii) $CM = MA = \frac{1}{2} AB$

Solution:



(i) In $\triangle ACB$,

M is the midpoint of AB and $MD \parallel BC$

, D is the midpoint of AC (Converse of mid point theorem)

(ii) $\angle ACB = \angle ADM$ (Corresponding angles)

also, $\angle ACB = 90^\circ$

, $\angle ADM = 90^\circ$ and $MD \perp AC$

(iii) In $\triangle AMD$ and $\triangle CMD$,

$AD = CD$ (D is the midpoint of side AC)

$\angle ADM = \angle CDM$ (Each 90°)

$DM = DM$ (common)

, $\triangle AMD \cong \triangle CMD$ [SAS congruency]

$AM = CM$ [CPCT]

also, $AM = \frac{1}{2} AB$ (M is midpoint of AB)

Hence, $CM = MA = \frac{1}{2} AB$

Benefits of NCERT Solutions for Class 9 Maths Chapter 8 Quadrilaterals

- **Clear Understanding of Concepts:** These solutions help students gain a clear understanding of the various properties and theorems related to quadrilaterals. By studying these solutions, students can grasp the fundamentals of quadrilaterals making it easier to solve related problems.
- **Step-by-Step Solutions:** The solutions provide a step-by-step approach to solving problems making it easier for students to follow and understand the methodology. This detailed explanation helps in building a strong foundation in geometry.
- **Effective Exam Preparation:** Using these solutions students can effectively prepare for their exams. The solutions cover all the important questions from the chapter ensuring that students are well-prepared for any type of question that may appear in the exams.
- **Doubt Clarification:** These solutions are designed to clear any doubts students may have while solving problems related to quadrilaterals. By referring to these solutions, students can get their doubts resolved and strengthen their understanding of the topic.
- **Time Management:** By practicing with these solutions, students can learn to manage their time effectively during exams. The step-by-step approach helps in solving problems more efficiently, allowing students to complete their exams within the given time frame.