

RS Aggarwal Solutions for Class 10 Maths Chapter 11 Exercise 11.1: RS Aggarwal Solutions for Class 10 Maths Chapter 11 Arithmetic Progressions Exercise 11.1 provide students with clear and detailed solutions to problems related to arithmetic sequences.

These solutions help students understand the fundamental concepts of arithmetic progressions, such as finding the common difference, the n th term, and the sum of the first n terms of the sequence. The step-by-step approach used in these solutions makes it easier for students to grasp the methods and apply them to similar problems, enhancing their problem-solving skills and preparing them effectively for their exams.

RS Aggarwal Solutions for Class 10 Maths Chapter 11 Exercise 11.1 Overview

RS Aggarwal Solutions for Class 10 Maths Chapter 11 Exercise 11.1, prepared by the subject experts from Physics Wallah, provide clear and detailed explanations to help students understand arithmetic progressions. These solutions break down complex problems into easy steps, making it simple for students to learn the basics of arithmetic sequences.

By using these solutions, students can improve their problem-solving skills and feel more confident in solving similar problems in exams. The straightforward guidance in these solutions ensures that students have a good grasp of arithmetic progressions, helping them do well in their studies.

RS Aggarwal Solutions for Class 10 Maths Chapter 11 Exercise 11.1 PDF

The PDF link for RS Aggarwal Solutions for Class 10 Maths Chapter 11 Exercise 11.1 is available below. This PDF provides clear and detailed solutions to the problems in this exercise, helping students understand arithmetic progressions.

By following these step-by-step explanations, students can easily grasp the concepts and improve their problem-solving skills. These solutions are an excellent resource for preparing for exams and ensuring a strong understanding of the topic.

RS Aggarwal Solutions for Class 10 Maths Chapter 11 Exercise 11.1 PDF

RS Aggarwal Solutions for Class 10 Maths Chapter 11 Arithmetic Progressions Exercise 11.1

Here we have provided RS Aggarwal Solutions for Class 10 Maths Chapter 11 Arithmetic Progressions Exercise 11.1 for the ease of students so that they can prepare better for their exams.

Q. Show that each of the progressions given below is an AP. Find the first term, common difference and next term of each.

(i) 9, 15, 21, 27,

(ii) 11, 6, 1, -4,

(iii) -1, -56, -23, -12, ...

(iv) $\sqrt{2}$, $\sqrt{8}$, $\sqrt{18}$, $\sqrt{32}$, ...

(v) $\sqrt{20}$, $\sqrt{45}$, $\sqrt{80}$, $\sqrt{125}$,

Solution:

(i) 9, 15, 21, 27,

Clearly $(15 - 9) = (21 - 15) = (27 - 21) = 6$ which is constant

Thus, each term differs from its preceding term by 6.

So, the given progression is an AP.

Next term of the AP = $27 + 6 = 33$

Its first term = 9, common difference = 6 and the next term is 33.

(ii) 11, 6, 1, -4,

Clearly $(6 - 11) = (1 - 6) = (-4 - 1) = -5$ which is constant.

Thus, each term differs from its preceding term by -5.

So the given progression is an AP.

Next term of the AP = $-4 + (-5) = -9$

Its first term = 11, common difference = -5 and the next term is -9

(iii) -1, $-\frac{5}{6}$, $-\frac{2}{3}$, $-\frac{1}{2}$,

Clearly $-\frac{5}{6} - (-1) = -\frac{2}{3} - (-\frac{5}{6}) = -\frac{1}{2} - (-\frac{2}{3}) = \frac{1}{6}$

Thus, each term differs from its preceding term by $\frac{1}{6}$. So, the given progression is an AP.

First term = -1

Common difference = $\frac{1}{6}$

Next term of the AP = $-1/2 + 1/6 = -2/6 = -1/3$

(iv) $\sqrt{2}, \sqrt{8}, \sqrt{18}, \sqrt{32}, \dots$

The given progression $\sqrt{2}, \sqrt{8}, \sqrt{18}, \sqrt{32}, \dots$

This sequence can be re-written as $\sqrt{2}, 2\sqrt{2}, 3\sqrt{2}, 4\sqrt{2}, \dots$

Thus, each term differs from its preceding term by $\sqrt{2}$. So, the given progression is an AP.

First term = $\sqrt{2}$

Common difference = $\sqrt{2}$

Next term of an AP = $4\sqrt{2} + \sqrt{2} = 5\sqrt{2}$

(v) $\sqrt{20}, \sqrt{45}, \sqrt{80}, \sqrt{125}, \dots$

This sequence can be re-written as $2\sqrt{5}, 3\sqrt{5}, 4\sqrt{5}, 5\sqrt{5}, \dots$

Clearly $d = 3\sqrt{5} - 2\sqrt{5} = \sqrt{5}$

Thus, each term differs from its preceding term by $\sqrt{5}$. So, the given progression is an AP.

First term = $\sqrt{20}$

Common difference = $\sqrt{5}$

Next term of the AP = $5\sqrt{5} + \sqrt{5} = 6\sqrt{5} = \sqrt{180}$

Q. Find:

(i) the 20th term of the AP, 9, 13, 17, 21,

(ii) the 35th term of the AP 20, 17, 14, 11, ...

(iii) the 18th term of the AP $\sqrt{2}, \sqrt{18}, \sqrt{50}, \sqrt{98}, \dots$

(iv) the 9th term of the AP 34, 54, 74, 94,

(v) the 15th term of the AP -40, -15, 10, 35,

Solution:

(1)-Given, AP, 9, 13, 17, 21,

a(first term)=9

d(common difference)=13-9=4

therefore,

$$T_n = a + (n-1)d$$

now putting the value of a and d, we get the

$$\text{The 20th term, } T_{20} = 9 + (20-1)4$$

$$= 9 + 19 \times 4$$

$$= 9 + 76$$

$$= 85$$

(2)-

Ap is 20, 17, 14, 11

We know that common difference $d = T_2 - T_1$

$$\text{Hence } d = 17 - 20 = -3$$

We also know that $T_n = a + (n-1)d$

$$\text{Therefore } T_{35} = 20 + (35-1) \times -3$$

$$= 20 + (34 \times -3) = 20 + (-102) = -82$$

35th term of given AP is - 82

(3)- AP $\sqrt{2}, \sqrt{18}, \sqrt{50}, \sqrt{98}, \dots$

AP can be rewritten as $\sqrt{2}, \sqrt{2 \times 9}, \sqrt{2 \times 25}, \sqrt{2 \times 49}, \dots$

i.e, $\sqrt{2}, 3\sqrt{2}, 5\sqrt{2}, 7\sqrt{2}, \dots$

First term, $a = \sqrt{2}$

Common difference, $d = 3\sqrt{2} - \sqrt{2} = 2\sqrt{2}$

$$T_n = a + (n-1)d$$

$$T_{18} = \sqrt{2} + (18-1)2\sqrt{2}$$

$$\sqrt{2} + 17 \times 2\sqrt{2} = \sqrt{2} + 34\sqrt{2} = 35\sqrt{2}$$

(4)AP: 34, 54, 74, 94,

$$a = 34$$

$$d = 54 - 34 = 24 = 12$$

Now,

$$T_9 = a + 8d$$

$$= 34 + 8 \times 12$$

$$= 34 + 96$$

$$= 130$$

$$= 130$$

(5) AP: -40, -15, 10, 35,

$$a = -40 \text{ and } d = -15 - (-40) = -15 + 40 = 25$$

$$T_n = a + (n-1)d$$

$$= -40 + (10-1)25$$

$$= -40 + (9)25$$

$$= -40 + 225$$

$$= 185$$

Q. (i) Find the 37th term of the AP 5, 412, 4, 312, 3,

(ii) Find the 25th term of the AP 5, 412, 4, 312, 3, ...

Solution:

$$\text{Here, } a = 5, d = 412 - 5 = 92 - 5 = -12$$

$$(i) T_{37} = a + (37-1)d = 5 + 36 \times (-12) = 5 - 432 = -427$$

$$(ii) T_{25} = a + (25-1)d = 5 + 24 \times (-12) = 5 - 288 = -283$$

Q. Find the value of p for which the numbers $2p-1$, $3p+1$, 11 are in AP.

Hence, find the numbers.

Solution:

$\because 2p-1, 3p+1, 11$ are in A.P.,

$$(3p+1) - (2p-1) = 11 - (3p+1) \Rightarrow p+2 = -3p+10 \Rightarrow 4p=8. \therefore p=2$$

So, the numbers are $2p-1=2 \times 2-1=3$, $3p+1=3 \times 2+1=7$ and 11.

Q. Find the n th term of each of the following APs:

(i) 5, 11, 17, 23, .. (ii) 16, 9, 2, -5, ...

Solution:

(i) Here, $a=5$, $d=11-5=6$
 $T_n = a + (n-1)d = 5 + (n-1) \times 6 = 6n - 1$

(ii) Here, $a=16$, $d=9-16=-7$
 $T_n = a + (n-1)d = 16 + (n-1) \times (-7) = 23 - 7n$

Q. If the n th term of a progression is $(4n-10)$ show that it is an AP. Find its (i) first term (ii) common difference and (iii) 16th term.

Solution:

Given, $a_n = 4n - 10$
 $a_{n-1} = 4(n-1) - 10 = 4n - 14$

Now, $a_n - a_{n-1} = (4n - 10) - (4n - 14) = 4$

So, the common difference is 4.

First term, $a_1 = 4 \times 1 - 10 = -6$

Now, 16th term, $T_{16} = 4 \times 16 - 10 = 64 - 10 = 54$

Q. How many terms are there in the AP 6, 10, 14, 18, ..., 174?

Solution:

Here, $a=6$, $d=10-6=4$, $T_n=174$

Now, $T_n = a + (n-1)d \Rightarrow 174 = 6 + (n-1) \times 4 \Rightarrow 168 = 4(n-1) \Rightarrow n-1 = 42 \therefore n = 43$

Q. How many terms are there in the AP=18, 1512, 13, ..., -47?

Solution:

The given AP is AP=18, 1512, 13, ..., -47

First term, $a=18$

Common difference, $d=13-18=-5$

Suppose there are n terms in the given AP.

Then, $a_n = -47$

$$\therefore a_n = a + (n-1)d$$

$$\Rightarrow 18 + (n-1) \times (-52) = -47$$

$$\Rightarrow (-52)(n-1) = -65$$

$$\Rightarrow n-1 = -65 \times (-25) = 26$$

$$\Rightarrow n-1 = 26$$

$$\Rightarrow n = 27$$

Hence, there are 27 items in the given AP.

Q. Which term of the AP = 72, 68, 64, 60, ... is 0?

Solution:

given AP is 72, 68, 64,

$$a = 72, d = -4$$

$$\text{nth term, } a_n = a + (n-1)d$$

nth term is 0

$$0 = 72 + (n-1) \cdot (-4)$$

$$-72 = (n-1) \cdot (-4)$$

$$n-1 = 18$$

$$n = 19$$

therefore, the 19th term of given AP is 0

Q. Which term of the AP 72, 68, 64, 60, ... is 0?

Solution:

given AP is 72, 68, 64,

$$a = 72, d = -4 \text{ nth term, } a_n = a + (n-1)d$$

nth term is 0

$$0 = 72 + (n-1) \cdot (-4)$$

$$-72 = (n-1) \cdot (-4)$$

$$n-1 = 18$$

$$n=19$$

therefore, the 19th term of given AP is 0

Q. Which term of the AP = 56, 1, 116, 113, ... is 3?

Solution:

In the given AP, the first term = 56 and

the common difference, $d = (1 - 56 = -16)$

Let its n th term be 3.

$$\text{Now, } T_n = 3$$

$$\Rightarrow \text{nth term, } a_n = a + (n-1)d$$

$$\Rightarrow 56 + (n-1) \times (-16) = 3$$

$$\Rightarrow 56 - 16n + 16 = 3$$

$$\Rightarrow 72 - 16n = 3$$

$$\Rightarrow 16n = 69$$

Hence, the 14th term of the given AP is 3.

Q. Which term of the AP = 21, 18, 15, ... is -81?

Solution:

$$a = 21$$

$$d = 18 - 21 = -3$$

Let -81 be the n th term.

Now,

$$\text{nth term, } a_n = a + (n-1)d$$

$$-81 = 21 + (n-1) \times (-3)$$

$$-81 = 21 - 3n + 3$$

$$-81 = 24 - 3n$$

$$3n = 24 + 81$$

$$n = 1053$$

$$n=35$$

Therefore, the 35th term is -81.

Q. Which term of the AP 8, 14, 20, 26, .. will be 72 more than its 41st term?

Solution:

$$a_n = 72 + a_{41}$$

$$a_n = 72 + (a + 40d) = 72 + 248 = 320$$

$$\text{Now, } a_n = a + (n-1)d$$

$$320 = 8 + (n-1) \times 6$$

$$8 + 6n - 6 = 320$$

$$6n = 320 - 2$$

$$6n = 318$$

$$n = 53$$

So, 53rd term of this A.P. will be 72 more than its 41st term.

Q. Which term of the AP 5, 15, 25, .. will be 130 more than its 31st term?

Solution:

$$\text{Here } a = 5 \text{ and } d = (15 - 5) = 10$$

The 31st term is given by

$$T_{31} = a + (31-1)d = a + 30d = 5 + 30 \times 10 = 305$$

$$\text{Therefore, the required term} = (305 + 130) = 435$$

Let this be the n th term.

$$\text{Then } T_n = 435$$

$$\Rightarrow 5 + (n - 1) \times 10 = 435$$

$$\Rightarrow 5 + (n-1) \times 10 = 453$$

$$\Rightarrow 10n = 440$$

$$\Rightarrow n = 44$$

Hence, the 44th term will be 130 more than its 31st term.

Q. If the 10th term of an AP is 52 and 17th term is 20 more than its 13th term, find the AP.

Solution:

given, $a_{10} = 52$

$$a + 9d = 52 \dots\dots\dots(1)$$

also, $a_{17} = 20 + a_{13}$

$$a + 16d = 20 + a + 12d$$

$$16d - 12d = 20$$

$$4d = 20$$

$$d = 5$$

putting the value of d in eq. (1), we get,

$$a + 9(5) = 52$$

$$a + 45 = 52$$

$$a = 7$$

hence, the required AP is 7, 12, 17,

Q. The sum of three consecutive terms of an is 21 and the sum of the squares of these terms is 165. find these terms.

Solution:

Let three consecutive terms be $a-d$, a , $a+d$
where d is common difference

$$a-d + a + a+d = 21$$

$$3a = 21$$

$$a = 7$$

$$(a-d)^2 + a^2 + (a+d)^2 = 165$$

$$a^2 - 2ad + d^2 + a^2 + a^2 + 2ad + d^2 = 165$$

$$3a^2 + 2d^2 = 165$$

$$147 + 2d^2 = 165$$

$$2d^2 = 18$$

$$d^2=9$$

$$d=3$$

$$a-d=4$$

$$a+d=10$$

the terms are 4,7,10

Q. The angles of a quadrilateral are in AP whose common difference is 10° find the angle.

Solution:

Since the angles are in A.P., let the angles are $p, p+10, p+20, p+30$

sum of angles=360

$$\Rightarrow p + p+10 + p+20 + p+30 = 360$$

$$\Rightarrow 4p + 60 = 360$$

$$\Rightarrow 4p = 360-60 = 300$$

$$\Rightarrow p = 300/4 = 75 \text{ So the angles are}$$

$$p = 75$$

$$p+10 = 75+10 = 85$$

$$p+20 = 75+20 = 95$$

$$p+30 = 75+30 = 105$$

Q. Find four numbers in AP whose sum is 28 and the sum of whose squares is 216.

Solution:

Let the four numbers be $(a-3d), (a-d), (a+d)$ and $(a+3d)$.

Given:

1. Their sum is 28

$$(a-3d)+(a-d)+(a+d)+(a+3d)=28$$

$$\Rightarrow 4a=28$$

$$\therefore a=7.$$

2. Their sum of square 216

$$(a-3d)^2+(a-d)^2+(a+d)^2+(a+3d)^2=216$$

$$\Rightarrow a^2+9d^2-6ad+a^2+d^2-2ad+a^2+d^2+2ad+a^2+9d^2+6ad=216$$

$$\Rightarrow 4a^2+20d^2=216$$

$$\Rightarrow a^2+5d^2=54$$

Putting the value of a

$$49+5d^2=54$$

$$5d^2=5$$

$$d^2=1$$

$$\therefore d=\pm 1.$$

For $d=1$:

The numbers are $7+3, 7+1, 7-1, 7-3 \Rightarrow 10, 8, 6, 4$.

For $d=-1$:

The numbers are $7+3, 7+1, 7-1, 7+3 \Rightarrow 4, 6, 8, 10$.

Q. Divide 32 into four parts which are the four terms of an AP such that the product of the first and the fourth terms is to the product of the second and the third terms as 7:15.

Solution:

In case of 4 terms, we usually take $2d$ as the common difference and the average of the two middle terms should be a .

Therefore, Let $a-3d, a-d, a+d$ and $a+3d$ be the 4 terms.

Now, By Question, we have

$$(a-3d) + (a-d) + (a+d) + (a+3d) = 32$$

$$\Rightarrow 4a = 32$$

$$\Rightarrow a = 8$$

Again, By Question, we have

$$(a-3d)(a+3d) : (a-d)(a+d) = 7 : 15$$

$$\Rightarrow a^2 - 9d^2 : a^2 - d^2 = 7 : 15$$

$$\Rightarrow 15(a^2 - 9d^2) = 7(a^2 - d^2)$$

$$\Rightarrow 15a^2 - 135d^2 = 7a^2 - 7d^2$$

$$\Rightarrow 15a^2 - 7a^2 = 135d^2 - 7d^2$$

$$\Rightarrow 8a^2 = 128d^2$$

$$\Rightarrow 8(8)^2 = 128d^2 \text{ (Substituting the value of } a)$$

$$\Rightarrow 512 = 128d^2$$

$$\Rightarrow 4 = d^2$$

$$\Rightarrow d = +2, -2$$

Therefore Common Difference = $2d = (+)(-)$ 4

Therefore, The required AP is -

$$a-3d = 8 - 3(2) = 2. \text{ Or. } a-3d = 8-3(-2) = 14$$

$$a-d = 8 - 2 = 6. \text{ Or. } a-d = 8-(-2) = 10$$

$$a+d = 8+2 = 10. \text{ Or. } a+d = 8+(-2) = 6$$

$$a+3d = 8+3(2) = 14. \text{ Or. } a+3d = 8+3(-2) = 2$$

Note: In one case the Common Difference is 4 where as in the 2nd case the Common Difference is -4.

Benefits of RS Aggarwal Solutions for Class 10 Maths

Chapter 11 Exercise 11.1

- **Clear Understanding:** These solutions provide step-by-step explanations making it easier for students to understand the concepts of arithmetic progressions.
- **Improved Problem-Solving Skills:** By practicing these solutions students can enhance their problem-solving abilities and tackle similar problems with confidence.
- **Comprehensive Coverage:** The solutions cover all the problems in Exercise 11.1, ensuring that students have thorough practice and understanding of the topic.
- **Exam Preparation:** These solutions help students prepare effectively for exams by providing detailed and accurate methods to solve the problems, which can be very useful for scoring well.
- **Time Management:** By following the systematic approach in these solutions, students can learn to solve problems more efficiently, helping them manage their time better during exams.
- **Confidence Boost:** Regular practice with these solutions helps build students confidence in their mathematical abilities and prepares them for more advanced topics in the future.