

NCERT Solutions for Class 10 Maths Chapter 6 Exercise 6.2: NCERT Solutions for Class 10 Maths Chapter 6 Exercise 6.2 focus on applying the Basic Proportionality Theorem (BPT), also known as Thales' Theorem, to solve geometric problems. This exercise introduces students to the concept of dividing triangles proportionally when a line parallel to one side intersects the other two sides.

The solutions emphasize the step-by-step application of this theorem, enabling students to solve problems related to proportionality in triangles effectively. These solutions are aligned with NCERT guidelines, helping students develop logical reasoning, strengthen their understanding of triangles, and enhance problem-solving skills. It is an essential topic for exams and higher studies.

NCERT Solutions for Class 10 Maths Chapter 6 Exercise 6.2 Overview

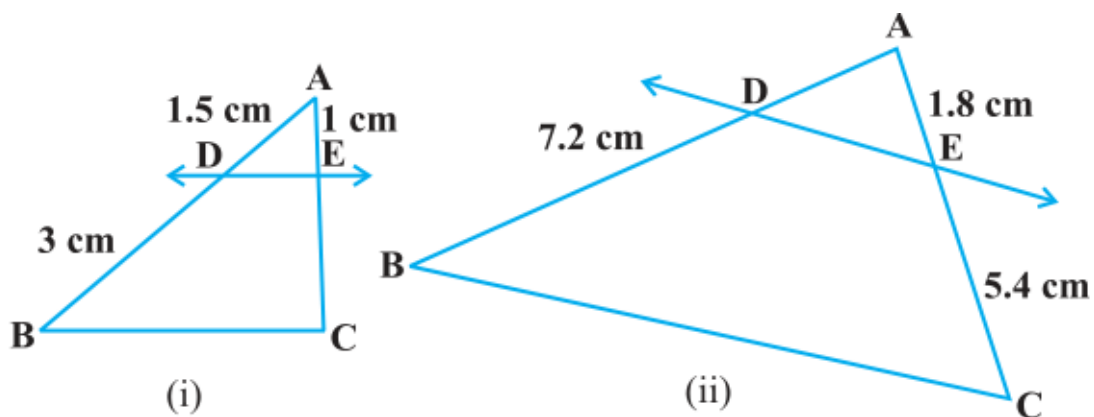
NCERT Solutions for Class 10 Maths Chapter 6 Exercise 6.2 on Triangles are crucial for mastering the Basic Proportionality Theorem (BPT), also known as Thales' Theorem. This theorem is fundamental in geometry, as it helps solve problems involving proportional division of triangles and line segments. These solutions provide clear, step-by-step explanations, ensuring a strong conceptual grasp.

Understanding BPT is important for developing logical reasoning and analytical skills, which are essential for board exams and competitive tests. It also forms a foundation for advanced topics in geometry, making this exercise a vital component of mathematical learning and real-world applications.

NCERT Solutions for Class 10 Maths Chapter 6 Exercise 6.2 Triangles

Below is the NCERT Solutions for Class 10 Maths Chapter 6 Exercise 6.2 Triangles -

1. In figure. (i) and (ii), $DE \parallel BC$. Find EC in (i) and AD in (ii).



Solution:

(i) Given, in $\triangle ABC$, $DE \parallel BC$

$\therefore AD/DB = AE/EC$ [Using Basic proportionality theorem]

$$\Rightarrow 1.5/3 = 1/EC$$

$$\Rightarrow EC = 3/1.5$$

$$EC = 3 \times 10/15 = 2 \text{ cm}$$

Hence, $EC = 2 \text{ cm}$.

(ii) Given, in $\triangle ABC$, $DE \parallel BC$

$\therefore AD/DB = AE/EC$ [Using Basic proportionality theorem]

$$\Rightarrow AD/7.2 = 1.8 / 5.4$$

$$\Rightarrow AD = 1.8 \times 7.2/5.4 = (18/10) \times (72/10) \times (10/54) = 24/10$$

$$\Rightarrow AD = 2.4$$

Hence, $AD = 2.4 \text{ cm}$.

2. E and F are points on the sides PQ and PR respectively of a $\triangle PQR$. For each of the following cases, state whether $EF \parallel QR$.

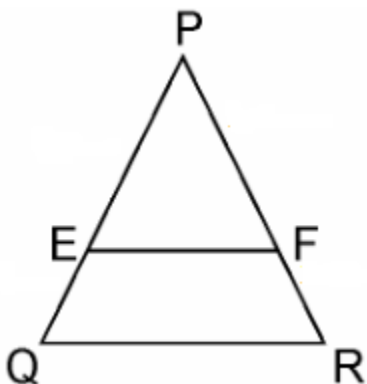
(i) $PE = 3.9 \text{ cm}$, $EQ = 3 \text{ cm}$, $PF = 3.6 \text{ cm}$ and $FR = 2.4 \text{ cm}$

(ii) $PE = 4 \text{ cm}$, $QE = 4.5 \text{ cm}$, $PF = 8 \text{ cm}$ and $RF = 9 \text{ cm}$

(iii) $PQ = 1.28 \text{ cm}$, $PR = 2.56 \text{ cm}$, $PE = 0.18 \text{ cm}$ and $PF = 0.63 \text{ cm}$

Solution:

Given, in ΔPQR , E and F are two points on side PQ and PR respectively. See the figure below;



(i) Given, PE = 3.9 cm, EQ = 3 cm, PF = 3.6 cm and FR = 2.4 cm

Therefore, by using Basic proportionality theorem, we get,

$$PE/EQ = 3.9/3 = 39/30 = 13/10 = 1.3$$

$$\text{And } PF/FR = 3.6/2.4 = 36/24 = 3/2 = 1.5$$

So, we get, $PE/EQ \neq PF/FR$

Hence, EF is not parallel to QR.

(ii) Given, PE = 4 cm, QE = 4.5 cm, PF = 8 cm and RF = 9 cm

Therefore, by using Basic proportionality theorem, we get,

$$PE/QE = 4/4.5 = 40/45 = 8/9$$

$$\text{And, } PF/RF = 8/9$$

So, we get here,

$$PE/QE = PF/RF$$

Hence, EF is parallel to QR.

(iii) Given, PQ = 1.28 cm, PR = 2.56 cm, PE = 0.18 cm and PF = 0.36 cm

From the figure,

$$EQ = PQ - PE = 1.28 - 0.18 = 1.10 \text{ cm}$$

And, $FR = PR - PF = 2.56 - 0.36 = 2.20$ cm

So, $PE/EQ = 0.18/1.10 = 18/110 = 9/55$ (i)

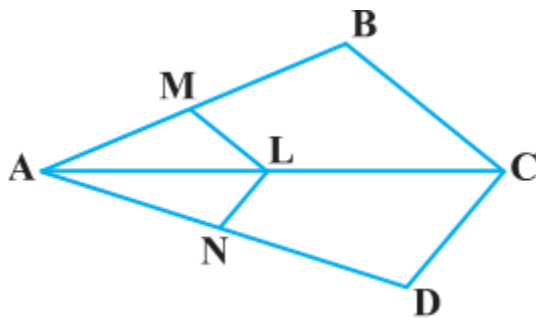
And, $PE/FR = 0.36/2.20 = 36/220 = 9/55$ (ii)

So, we get here,

$$PE/EQ = PF/FR$$

Hence, EF is parallel to QR.

3. In the figure, if $LM \parallel CB$ and $LN \parallel CD$, prove that $AM/AB = AN/AD$



Solution:

In the given figure, we can see, $LM \parallel CB$,

By using basic proportionality theorem, we get,

$$AM/AB = AL/AC$$
.....(i)

Similarly, given, $LN \parallel CD$ and using basic proportionality theorem,

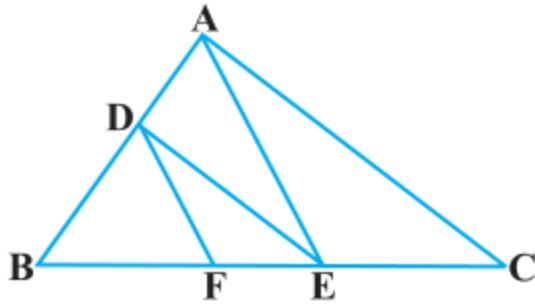
$$\therefore AN/AD = AL/AC$$
.....(ii)

From equation (i) and (ii), we get,

$$AM/AB = AN/AD$$

Hence, proved.

4. In the figure, $DE \parallel AC$ and $DF \parallel AE$. Prove that $BF/FE = BE/EC$



Solution:

In $\triangle ABC$, given as, $DE \parallel AC$

Thus, by using Basic Proportionality Theorem, we get,

$$\therefore BD/DA = BE/EC \dots\dots\dots (i)$$

In $\triangle BAE$, given as, $DF \parallel AE$

Thus, by using Basic Proportionality Theorem, we get,

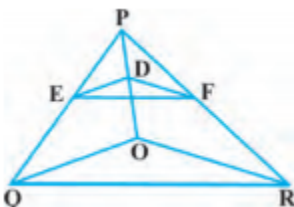
$$\therefore BD/DA = BF/FE \dots\dots\dots (ii)$$

From equation (i) and (ii), we get

$$BE/EC = BF/FE$$

Hence, proved.

5. In the figure, $DE \parallel OQ$ and $DF \parallel OR$, show that $EF \parallel QR$.



Solution:

Given,

In $\triangle PQO$, $DE \parallel OQ$

So by using Basic Proportionality Theorem,

$$PD/DO = PE/EQ \dots\dots\dots (i)$$

Again given, in ΔPOR , $DF \parallel OR$,

So by using Basic Proportionality Theorem,

$$PD/DO = PF/FR \dots\dots\dots (ii)$$

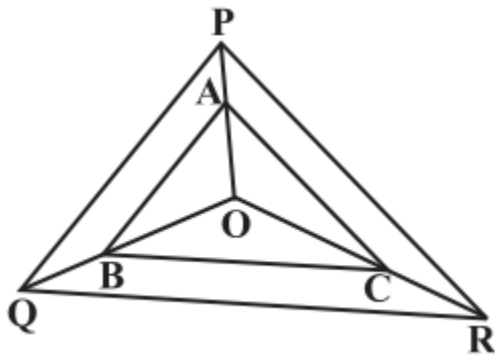
From equation (i) and (ii), we get,

$$PE/EQ = PF/FR$$

Therefore, by converse of Basic Proportionality Theorem,

$EF \parallel QR$, in ΔPQR .

6. In the figure, A, B and C are points on OP, OQ and OR respectively such that $AB \parallel PQ$ and $AC \parallel PR$. Show that $BC \parallel QR$.



Solution:

Given here,

In ΔOPQ , $AB \parallel PQ$

By using Basic Proportionality Theorem,

$$OA/AP = OB/BQ \dots\dots\dots (i)$$

Also given,

In ΔOPR , $AC \parallel PR$

By using Basic Proportionality Theorem

$$\therefore OA/AP = OC/CR \dots\dots\dots (ii)$$

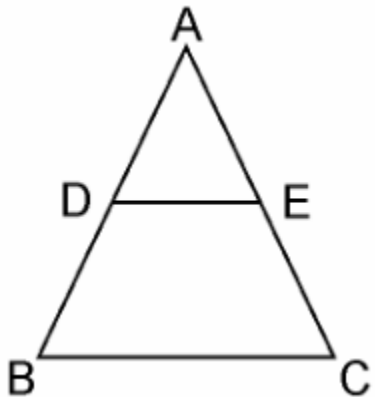
From equation (i) and (ii), we get,

$$OB/BQ = OC/CR$$

Therefore, by converse of Basic Proportionality Theorem,

In $\triangle OQR$, $BC \parallel QR$.

7. Using Basic proportionality theorem, prove that a line drawn through the mid-points of one side of a triangle parallel to another side bisects the third side. (Recall that you have proved it in Class IX).



Solution:

Given, in $\triangle ABC$, D is the midpoint of AB such that $AD = DB$.

A line parallel to BC intersects AC at E as shown in above figure such that $DE \parallel BC$.

We have to prove that E is the mid point of AC.

Since, D is the mid-point of AB.

$$\therefore AD = DB$$

$$\Rightarrow AD/DB = 1 \dots\dots\dots (i)$$

In $\triangle ABC$, $DE \parallel BC$,

By using Basic Proportionality Theorem,

$$\text{Therefore, } AD/DB = AE/EC$$

From equation (i), we can write,

$$\Rightarrow 1 = AE/EC$$

$$\therefore AE = EC$$

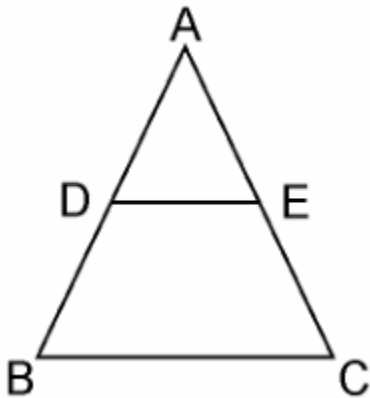
Hence, proved, E is the midpoint of AC.

8. Using Converse of basic proportionality theorem, prove that the line joining the mid-points of any two sides of a triangle is parallel to the third side. (Recall that you have done it in Class IX).

Solution:

Given, in $\triangle ABC$, D and E are the mid points of AB and AC respectively, such that,

$AD=BD$ and $AE=EC$.



We have to prove that: $DE \parallel BC$.

Since, D is the midpoint of AB

$\therefore AD=BD$

$\Rightarrow AD/BD = 1$ (i)

Also given, E is the mid-point of AC.

$\therefore AE=EC$

$\Rightarrow AE/EC = 1$

From equation (i) and (ii), we get,

$AD/BD = AE/EC$

By converse of Basic Proportionality Theorem,

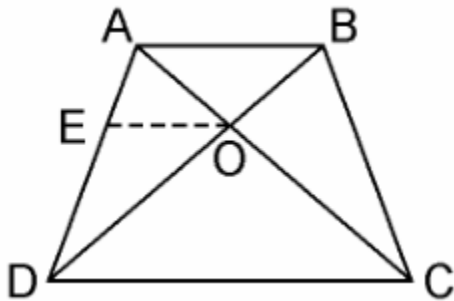
$DE \parallel BC$

Hence, proved.

9. ABCD is a trapezium in which $AB \parallel DC$ and its diagonals intersect each other at the point O. Show that $AO/BO = CO/DO$.

Solution:

Given, ABCD is a trapezium where $AB \parallel DC$ and diagonals AC and BD intersect each other at O.



We have to prove, $AO/BO = CO/DO$

From the point O, draw a line EO touching AD at E, in such a way that,

$EO \parallel DC \parallel AB$

In $\triangle ADC$, we have $OE \parallel DC$

Therefore, By using Basic Proportionality Theorem

$$AE/ED = AO/CO \dots\dots\dots(i)$$

Now, In $\triangle ABD$, $OE \parallel AB$

Therefore, By using Basic Proportionality Theorem

$$DE/EA = DO/BO \dots\dots\dots(ii)$$

From equation (i) and (ii), we get,

$$AO/CO = BO/DO$$

$$\Rightarrow AO/BO = CO/DO$$

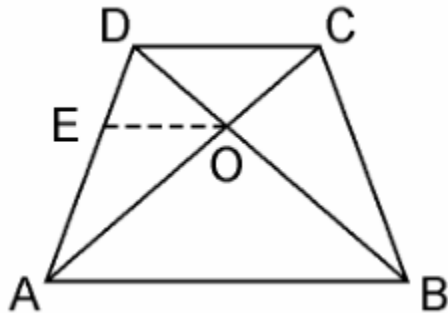
Hence, proved.

10. The diagonals of a quadrilateral ABCD intersect each other at the point O such that $AO/BO = CO/DO$. Show that ABCD is a trapezium.

Solution:

Given, Quadrilateral ABCD where AC and BD intersect each other at O such that,

$AO/BO = CO/DO$.



We have to prove here, ABCD is a trapezium

From the point O, draw a line EO touching AD at E, in such a way that,

$EO \parallel DC \parallel AB$

In $\triangle DAB$, $EO \parallel AB$

Therefore, By using Basic Proportionality Theorem

$DE/EA = DO/OB$ (i)

Also, given,

$AO/BO = CO/DO$

$\Rightarrow AO/CO = BO/DO$

$\Rightarrow CO/AO = DO/BO$

$\Rightarrow DO/OB = CO/AO$ (ii)

From equation (i) and (ii), we get

$DE/EA = CO/AO$

Therefore, By using converse of Basic Proportionality Theorem,

$EO \parallel DC$ also $EO \parallel AB$

$\Rightarrow AB \parallel DC$.

Hence, quadrilateral ABCD is a trapezium with $AB \parallel CD$.

Benefits of Using NCERT Solutions for Class 10 Maths Chapter 6 Exercise 6.2

Mastery of the Basic Proportionality Theorem (BPT):

This exercise focuses on the application of BPT, also known as Thales' Theorem, a fundamental concept in geometry. The solutions provide a clear understanding of how parallel lines divide triangles proportionally, helping students solve complex geometric problems.

Step-by-Step Problem Solving:

Each solution is explained in a structured manner, breaking down complex problems into manageable steps. This approach makes it easier for students to follow and understand the reasoning behind each step.

Strengthens Conceptual Understanding:

Practicing these solutions helps students build a strong foundation in triangle properties and proportionality, which are essential for advanced topics in geometry, trigonometry, and mensuration.

Exam-Focused Preparation:

These solutions are designed as per the NCERT syllabus and exam pattern, ensuring students are well-prepared to tackle similar questions in their board exams with accuracy and confidence.

Enhances Logical Reasoning and Analytical Skills:

By working through the problems, students develop the ability to analyze geometric relationships, draw logical conclusions, and solve problems systematically, skills that are crucial for academic success and beyond.