

# ULTIMATE KCET

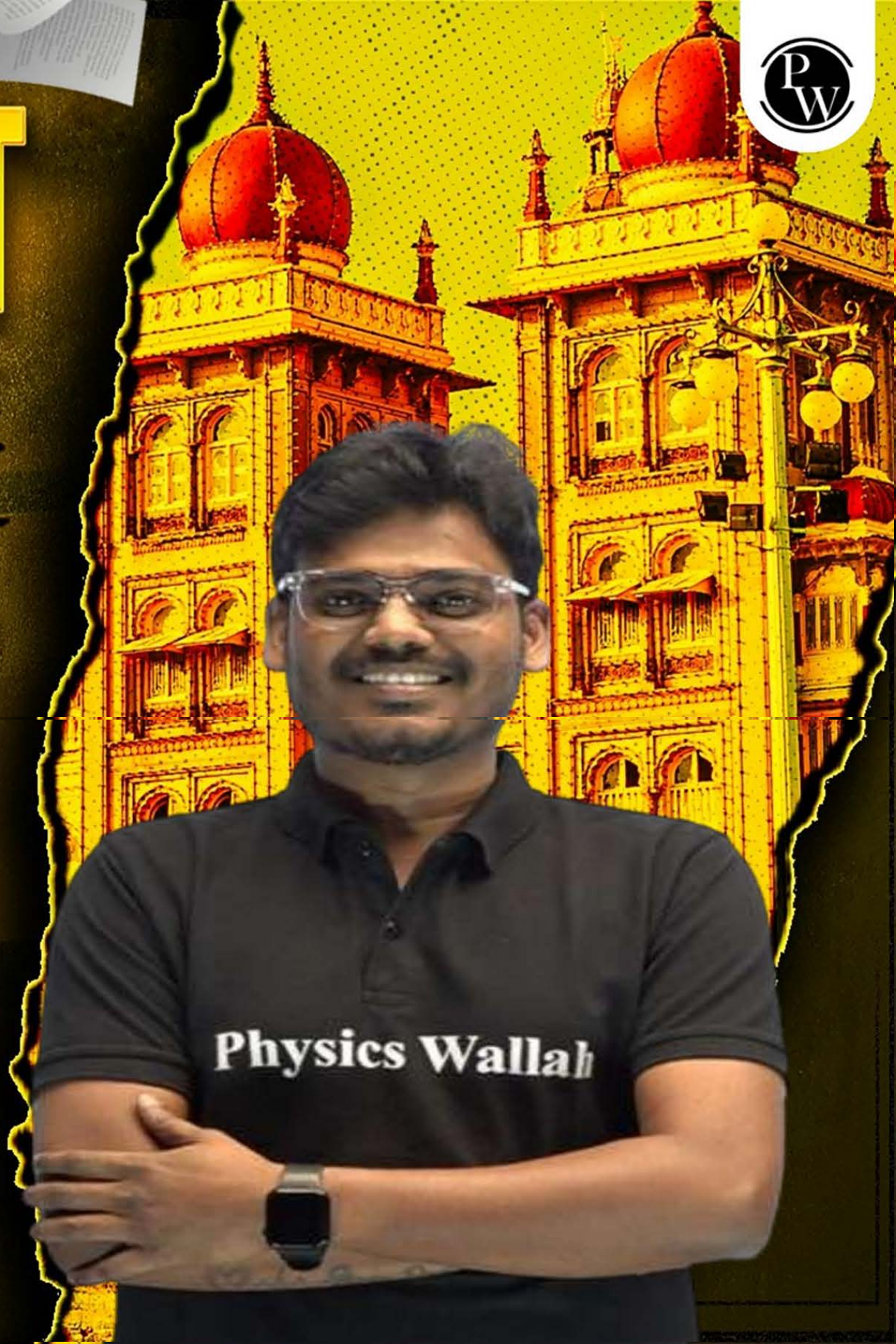
CRASH COURSE 2026

Physics

Lecture : 01

**MOTION IN A  
PLANE [ ]**

By: AK Sir



# Recap *of previous lecture*

- 1 RECTIFIER'S AND ITS TYPES
- 2 QUESTIONS
- 3 UNITS AND MEASUREMENT
- 4 MOTION IN A STRAIGHT LINE



# Topics

*to be covered*

- 1 QUESTIONS ON 1D MOTION
- 2 SCALARS AND VECTORS
- 3 PROJECTILE MOTION
- 4 PYQ's + MCQ's





# GRAPHS OF KINEMATICS

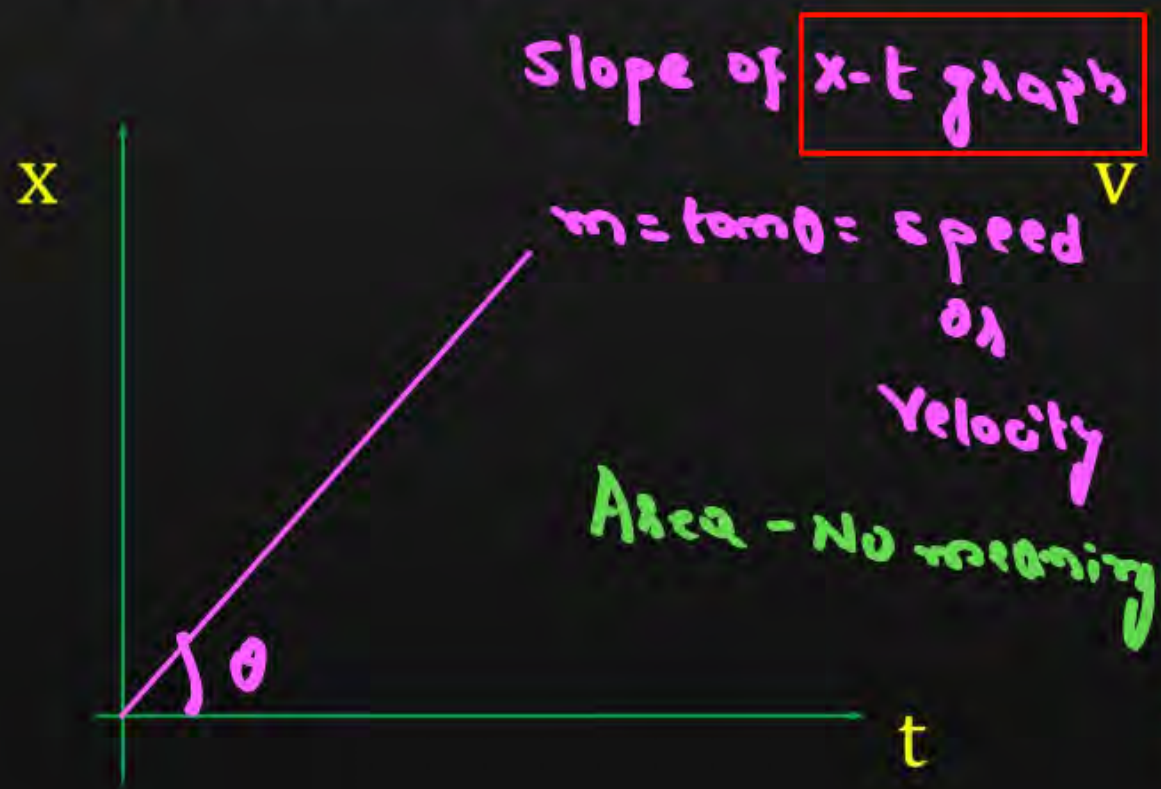
Slope,  $m = \tan\theta = \frac{\Delta y}{\Delta x} \rightarrow$  Diff

Area under graph  $\rightarrow$  Integration.

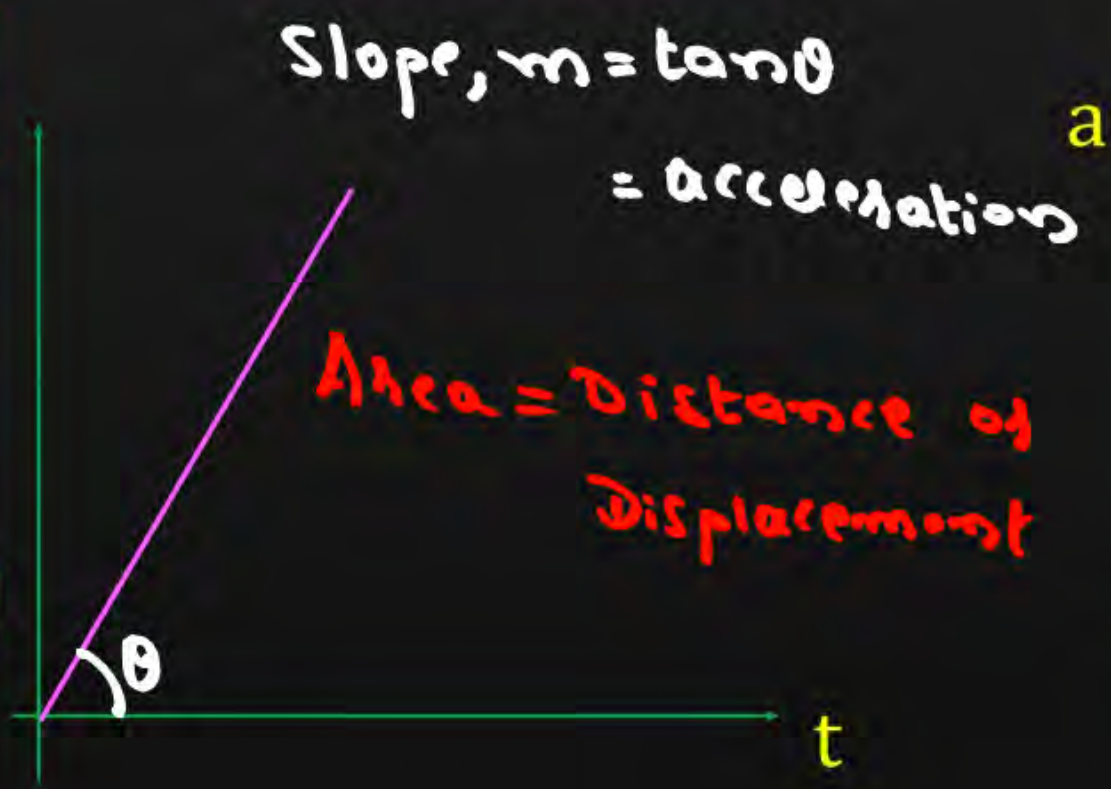
1. Position - time

2. Velocity - time

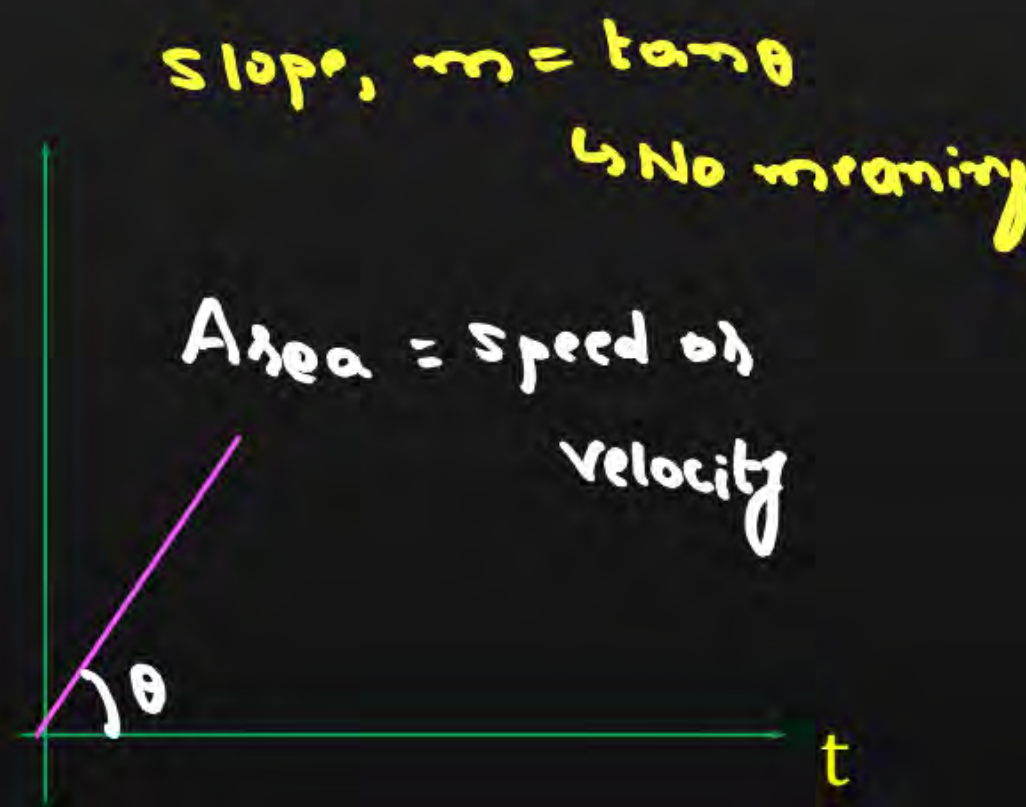
3. Acceleration - time



$v-t$  graph



$a-t$  graph



# Graph



$$v = \frac{dx}{dt}$$

$$a = \frac{dv}{dt}$$

Slope

Slope

Position-time

Velocity - time

Acceleration - time

Area

Area

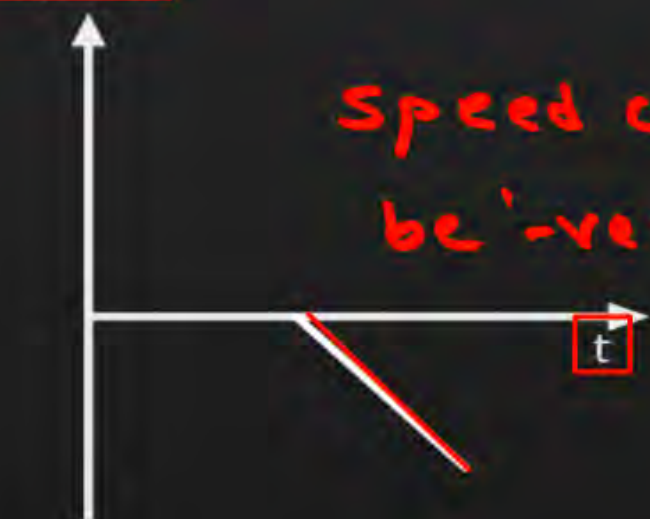
$$x = \int v \cdot dt$$

$$v = \int a \cdot dt$$



# GRAPHS THAT ARE IMPOSSIBLE

Speed



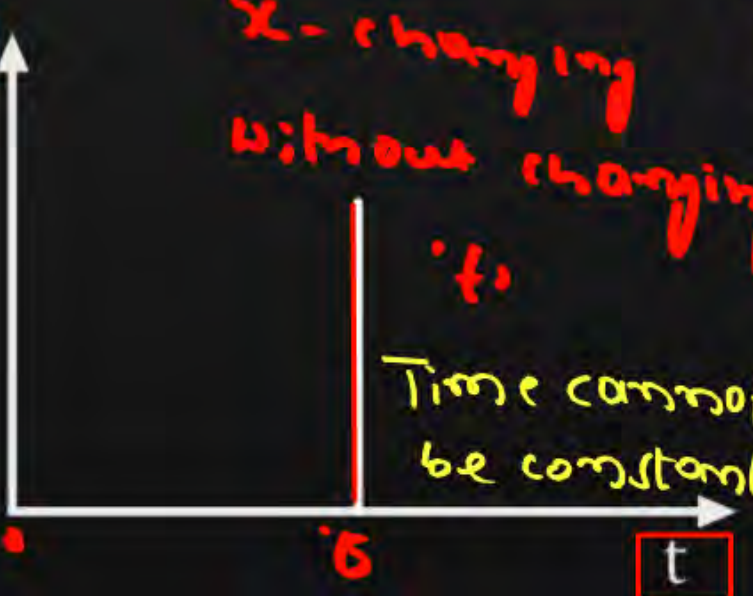
Speed cannot be '-ve'

Distance



Distance cannot be '-ve'

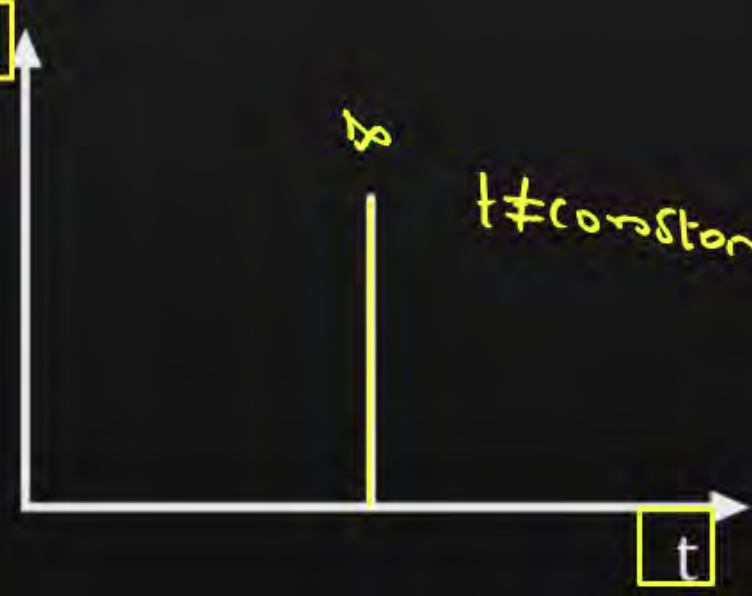
X



X - changing without changing 't'

Time cannot be constant

v



t ≠ constant

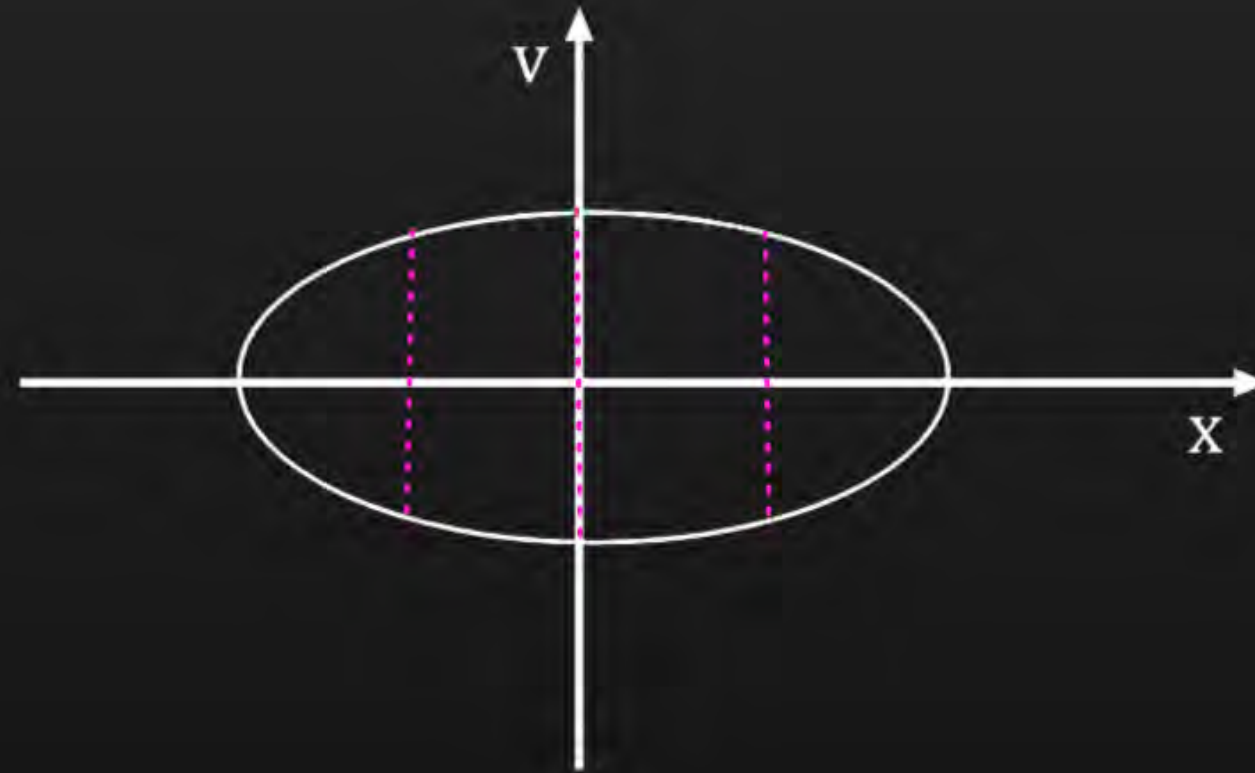
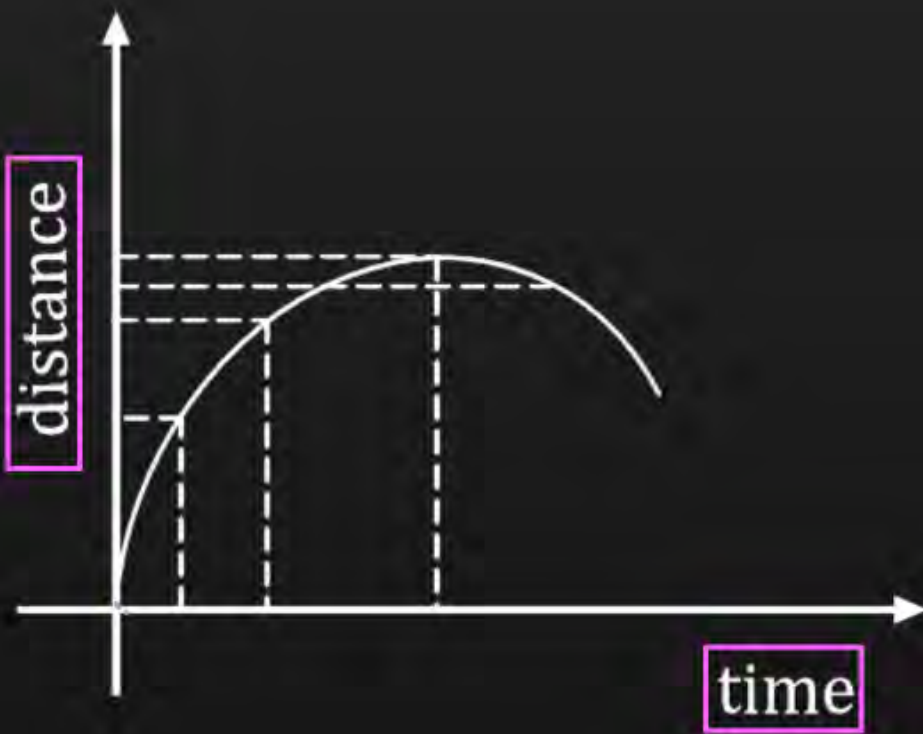
a



t ≠ constant

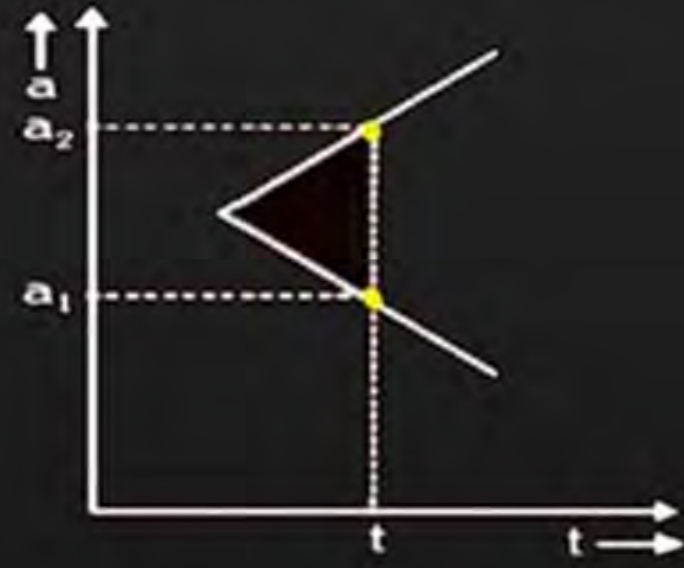
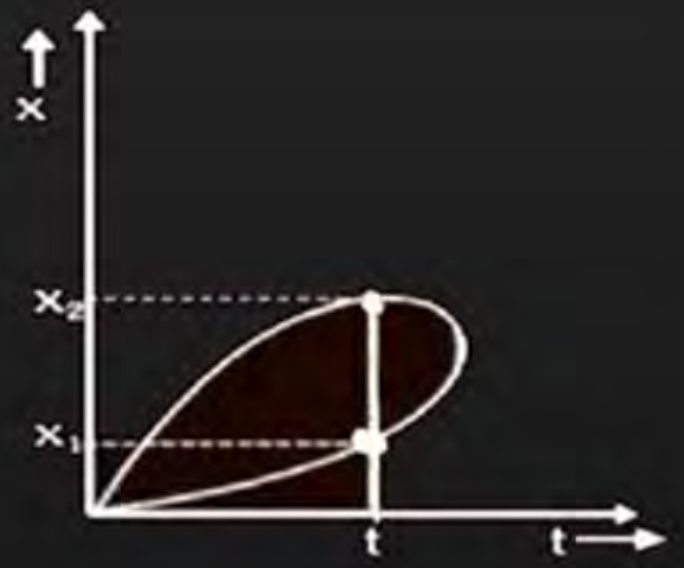
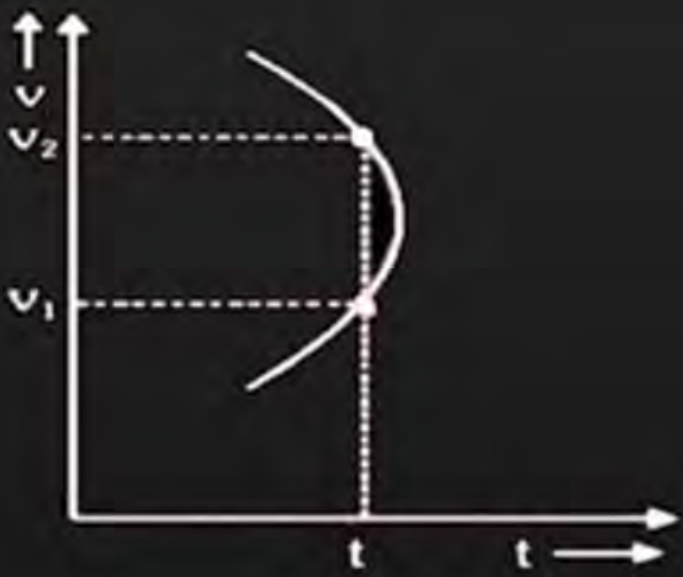


# GRAPHS THAT ARE IMPOSSIBLE





# GRAPHS THAT ARE IMPOSSIBLE



**QUESTION**

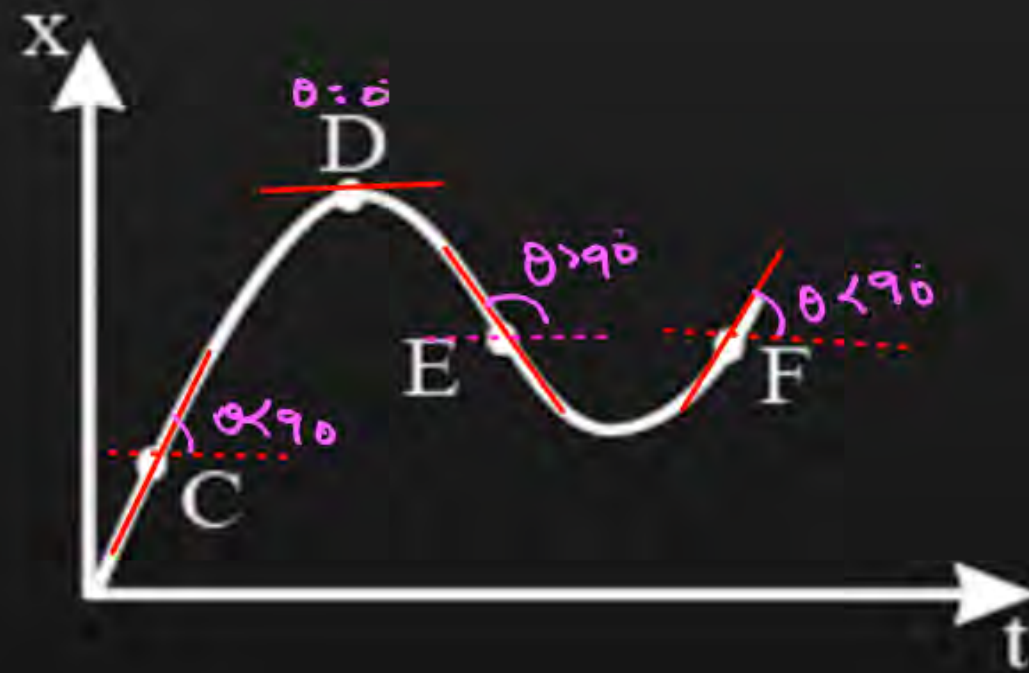
The displacement time graph of a moving particle is shown below. The instantaneous velocity of the particle is negative at the point.

**A** C

**B** D

**C** E

**D** F



**QUESTION**

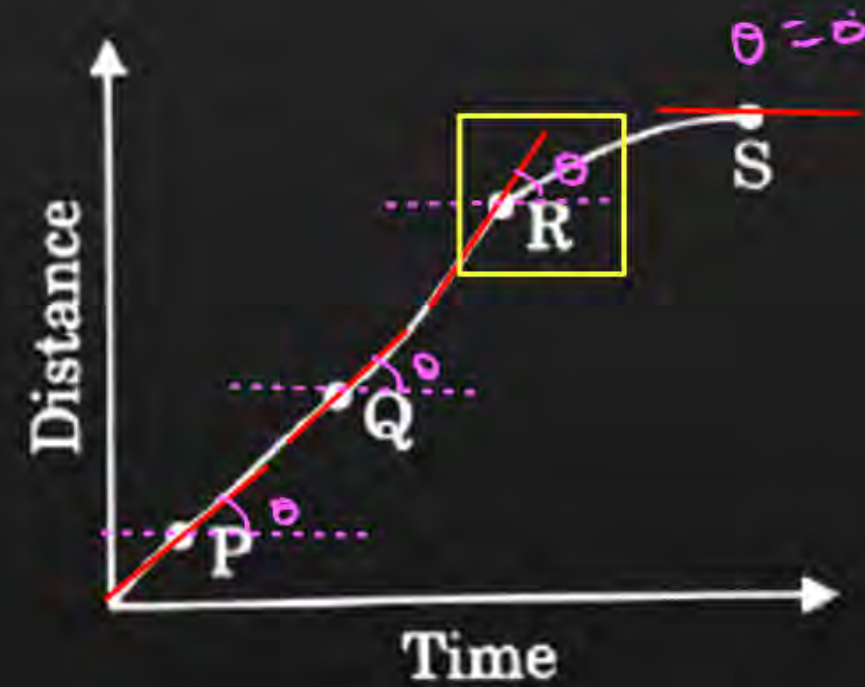
A particle shows distance-time curve as shown in the figure. The maximum instantaneous velocity of the particle is around the point

**A**  $P$

**B**  $S$

**C**  $R$

**D**  $Q$



## QUESTION

For a body moving along a straight line, the following  $v-t$  graph is obtained

According to the graph, the displacement during

$\hookrightarrow$  Area.

$\hookrightarrow A \rightarrow B$

$\times$

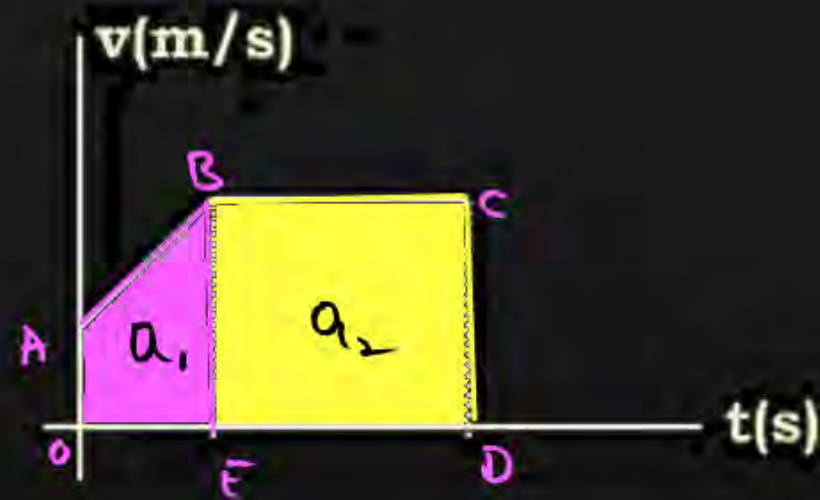
$\hookrightarrow B \rightarrow C$

**A** uniform acceleration is greater than that during uniform motion

**B** uniform acceleration is less than that during uniform motion

**C** uniform acceleration is equal to that during uniform motion

**D** uniform motion is zero



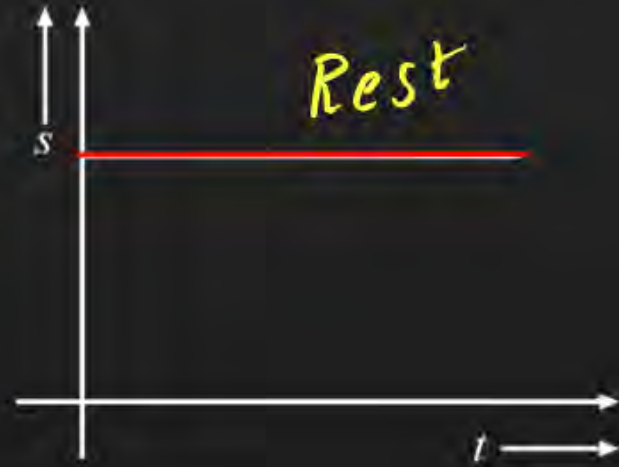
**QUESTION**

Which of the following graph represents **uniform motion** (here  $s$  is position)

**A**



**B**



**C**



**D**



## QUESTION

The v-t graph of a moving object is given in figure. The maximum acceleration is

- A** 1 cm/sec<sup>2</sup>
- B** 2 cm/sec<sup>2</sup>
- C** 3 cm/sec<sup>2</sup>
- D** 6 cm/sec<sup>2</sup>

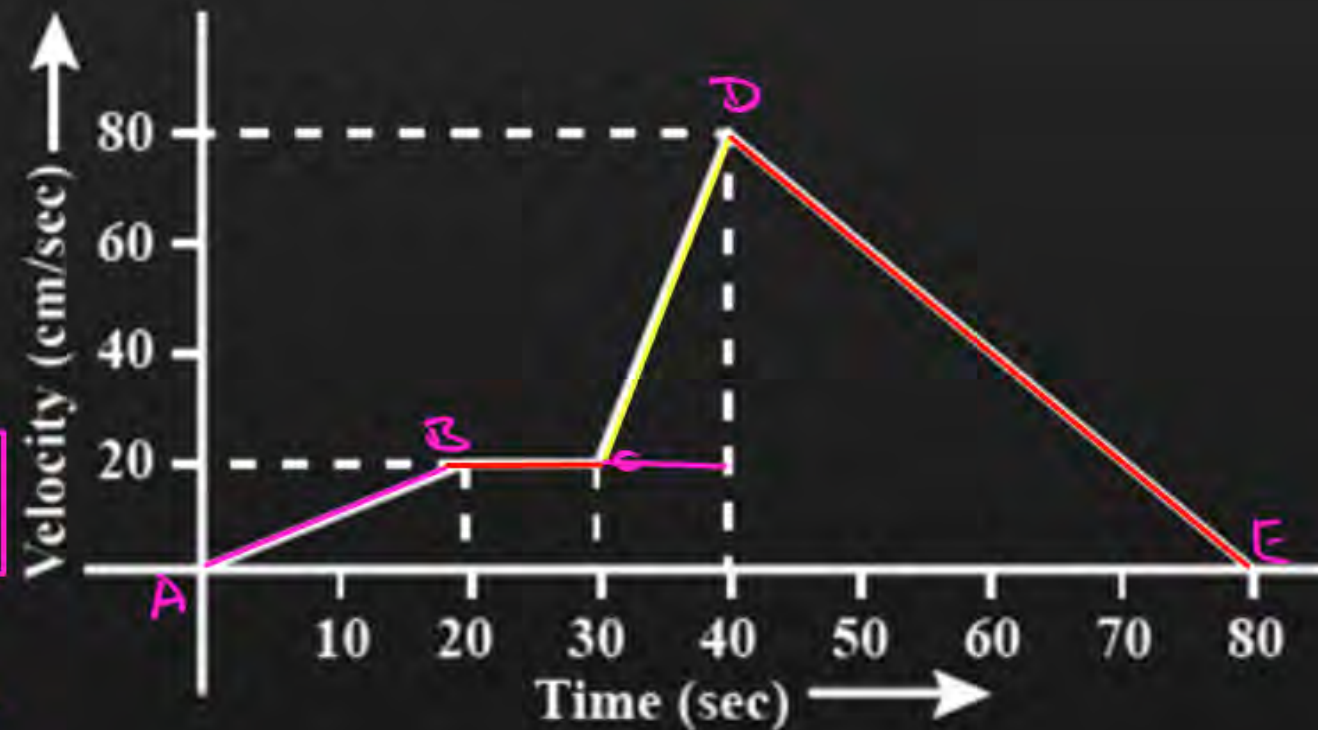
A → B

$$a = \frac{20}{20} = 1 \text{ cm/s}^2$$

B → C, a = 0

$$C \rightarrow D, a = \frac{60}{10} = 6 \text{ cm/s}^2$$

$$D \rightarrow E, a = -\frac{80}{40} = -2 \text{ cm/s}^2$$



## QUESTION

A particle starts from rest. Its acceleration ( $a$ ) versus time ( $t$ ) is as shown in the figure. The maximum speed of the particle will be

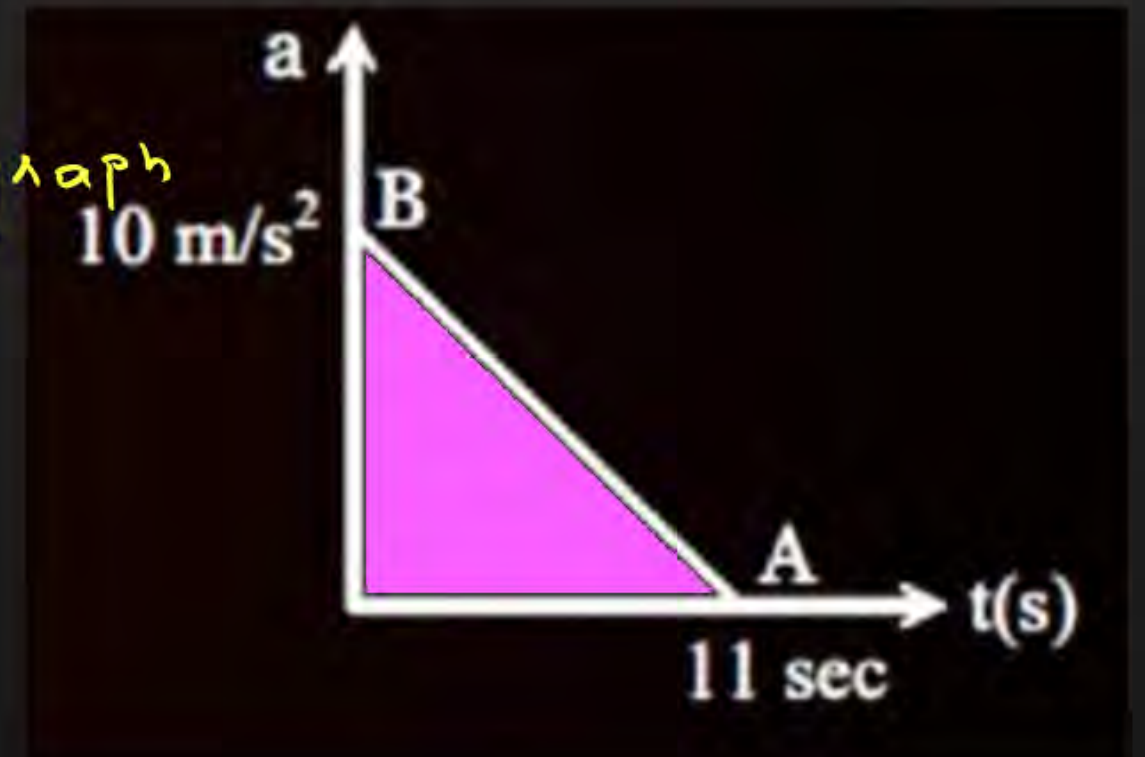
- A** 110m/s
- B** 55m/s
- C** 550m/s
- D** 660m/s

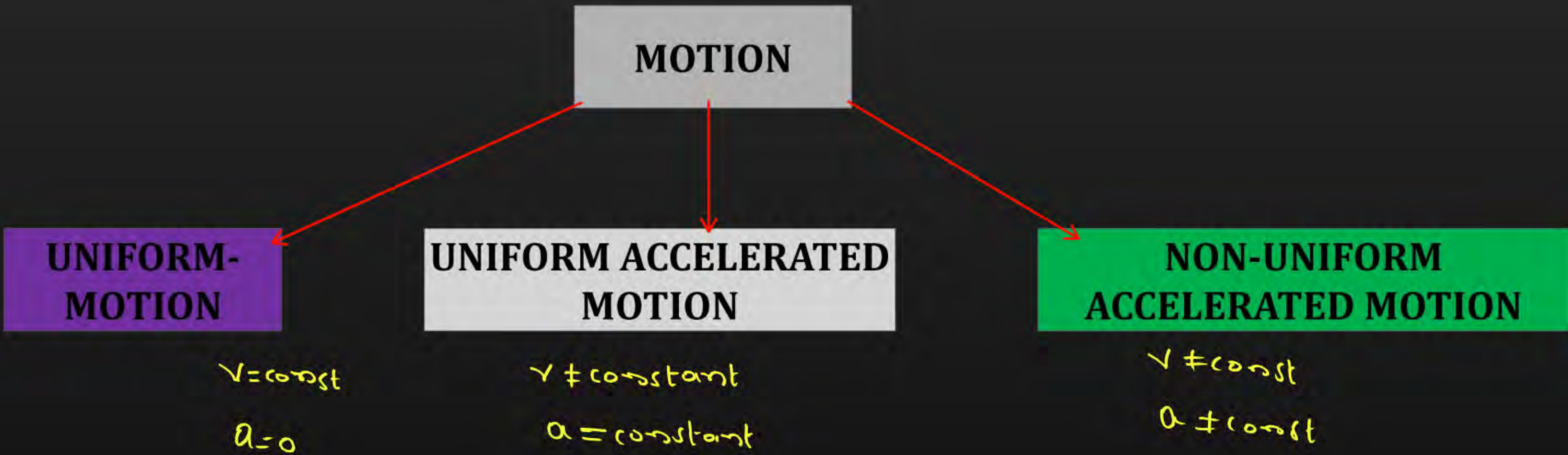
speed = Area under a-t graph

$$= \frac{1}{2} \times b \times h$$

$$= \frac{1}{2} \times 11 \times 10$$

$$= 55 \text{ m/s}$$







## KINEMATICS EQUATIONS

speed up?  
yes  
no

For a motion of a body moving with a uniform acceleration, the following three equations give the relationship between initial velocity ( $u$ ), final velocity ( $v$ ), acceleration ( $a$ ), time of journey ( $t$ ) and displacement ( $S$ )

$$v = u + at \rightarrow S \times$$

$$S = ut + \frac{1}{2}at^2 \rightarrow v \times$$

$$v^2 = u^2 + 2as \rightarrow t \times$$

$$S_n = u + \frac{a}{2}(2n-1)$$

## QUESTION

Which of the following equations **does not represent** the kinematic equations of motion?

**A**  $v = u + at$  ✓

**B**  $s = ut + \frac{1}{2}at^2$  ✓

**C**  $s = vt + \frac{1}{2}at^2$  ✗

**D**  $v^2 - u^2 = 2as$  ✓

## QUESTION

A particle starts with velocity of 10 m/s along x-direction and accelerates uniformly at the rates  $2\text{ms}^{-2}$ . The time taken by the particle to reach the velocity of 60 m/s is

A 30 s

B 6 s

C 25 s

D 3 s

$$v = u + at$$

$$60 = 10 + 2t$$

$$2t = 50$$

$$t = 25\text{ s}$$

## QUESTION

A particle is moving along a straight line with constant acceleration. At the end of 10<sup>th</sup> second its velocity becomes 20 m/s and in 10<sup>th</sup> it travels a distance of 10 m. Find the acceleration of the particle.

**A**  $40 \text{ ms}^{-2}$

**B**  $10 \text{ ms}^{-2}$

**C**  $30 \text{ ms}^{-2}$

**D**  $20 \text{ ms}^{-2}$

$$v = u + at$$

$$20 = u + a \times 10$$

$$u = 20 - 10a \quad \text{--- (2)}$$

$$\text{(2) in (1)} \quad 10 = 20 - 10a + \frac{a}{2} \times 19$$

$$10 - 20 = -\frac{20a + 19a}{2}$$

$$-10 = -\frac{a}{2}$$

$$-20 = -a \Rightarrow a = 20 \text{ ms}^{-2}$$

$$n = 10$$

$$S_n = u + \frac{a}{2} (2n - 1)$$

$$S_{10} = u + \frac{a}{2} (2 \times 10 - 1)$$

$$10 = u + \frac{a}{2} [19] \quad \text{--- (1)}$$

## QUESTION

$u=0$

$$S_n = u + \frac{a}{2}(2n-1)$$

A body A starts from **rest** with an acceleration  $a_1$ . After 2 seconds, another body B starts from **rest** with an acceleration  $a_2$ . If they travel equal distance in the 5<sup>th</sup> second, after the start of A, then the ratio of  $a_1 : a_2$  equal to

- A** 5:9
- B** 5:7
- C** 9:5
- D** 9:7

$$(S_n)_A = (S_n)_B$$

$$\frac{a_1}{2}(2 \times 5 - 1) = \frac{a_2}{2}(2 \times 3 - 1)$$

$$\frac{9a_1}{2} = \frac{5a_2}{2} \Rightarrow 9a_1 = 5a_2$$

$$\frac{a_1}{a_2} = \frac{5}{9}$$

$$\frac{a_1}{a_2} = \frac{5}{9}$$



# MOTION UNDER GRAVITY

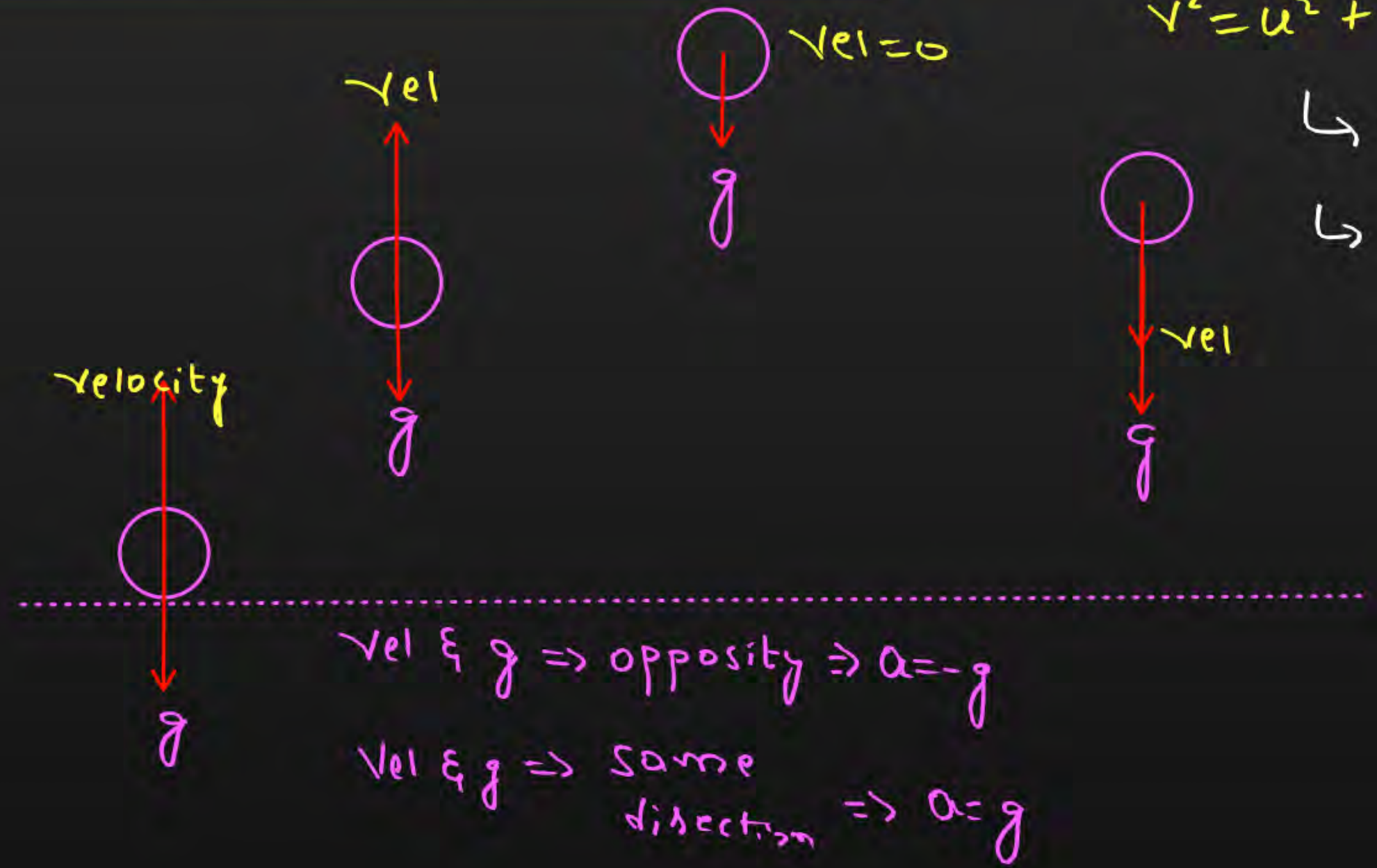
$$v = u + at$$

$$s = ut + \frac{1}{2}at^2$$

$$v^2 = u^2 + 2as$$

$$\hookrightarrow a = g$$

$$\hookrightarrow s = H$$



## QUESTION

A body is thrown vertically upwards from the ground. It reaches a maximum height of 20m in 5s. After what time it will reach the ground from its maximum height position?

**A** 2.5 s

**B** 5 s

**C** 10 s

**D** 25 s

$$t_a = 5 \text{ s}$$

$$t_d = t_a = 5 \text{ s}$$

## QUESTION

If a ball is thrown vertically upwards with a velocity of 40 m/s, then velocity of the ball after 2s will be. (Take  $g = 10 \text{ m/s}^2$ )

$$a = -g$$

 $u$  $t$ 

$$v = u + at$$

$$v = 40 + (-10) \times 2$$

$$v = 40 - 20$$

$$v = 20 \text{ m/s}$$

A 15 m/s

B 20 m/s

C 25 m/s

D 28 m/s

## QUESTION

A stone is thrown vertically upwards. When stone is at a height half of its maximum height, its speed is 10 m/s, then the maximum height attained by the stone is (Take  $g = 10 \text{ m/s}^2$ )

- A** 8 m
- B** 10 m
- C** 15 m
- D** 20 m

$$a = -g$$

$$\frac{h}{2} = \frac{u^2}{2g} = \frac{(10)^2}{10} = 10$$

$$h = 10 \text{ m}$$

$$v^2 = u^2 + 2as$$

$$(0)^2 = u^2 + 2(-g)H$$

$$2gH = u^2$$

$$H = \frac{u^2}{2g}$$

## QUESTION

A boy standing at the top of a tower of  $20\text{ m}$  height drops a stone. Assuming,  $g = 10\text{ ms}^{-2}$ , the velocity with which it hits the ground is

$s = H$        $u = 0$   
 $\hookrightarrow a = g$

- A**  $20\text{ m/s}$
- B**  $40\text{ m/s}$
- C**  $5\text{ m/s}$
- D**  $10\text{ m/s}$

$$v^2 = u^2 + 2as$$

$$v^2 = (0)^2 + 2gH$$

$$v^2 = 2 \times 10 \times 20$$

$$v^2 = 400$$

$$v = \sqrt{400}$$

$$v = 20\text{ m/s}$$

**QUESTION**

$$u=0, a=g$$

Two bodies A (of mass 1 kg) and B (of mass 3 kg) are dropped from heights of 16 m and 25 m, respectively. The ratio of the time taken by them to reach the ground is

- A** -5/4
- B** 12/5
- C** 5/12
- D** 4/5

$$\frac{t_A}{t_B} = \sqrt{\frac{H_A}{H_B}} = \sqrt{\frac{16}{25}} = \frac{4}{5}$$

$$\frac{t_A}{t_B} = \frac{4}{5}$$

$$S = ut + \frac{1}{2}at^2$$

$$H = \frac{1}{2}gt^2$$

$$t^2 = \frac{2H}{g}$$

$$t = \sqrt{\frac{2H}{g}} \propto \sqrt{H}$$

**QUESTION**

$u=0, a=g$

A stone released with zero velocity from the top of a tower, reaches the ground in 4 s. The height of the tower is (Take  $g = 10 \text{ m/s}^2$ )

- A** 20 m
- B** 40 m
- C** 80 m
- D** 160 m

$$s = ut + \frac{1}{2}at^2$$

$$H = \frac{1}{2}gt^2$$

$$H = \frac{1}{2} \times 10 \times (4)^2 = 5 \times 16$$

$$H = 80 \text{ m}$$

**QUESTION**

A horizontal bridge is built across a river. A student standing on the bridge throws a small ball vertically upwards with a velocity  $4 \text{ ms}^{-1}$ . The ball strikes the water surface after 4s. The height of bridge above water surface is. (Take  $g = 10 \text{ m/s}^{-2}$ )

- A** 68 m
- B** 56 m
- C** 60 m
- D** 64 m

$$S = ut + \frac{1}{2}at^2$$

$$H = ut + \frac{1}{2}(-g)t^2$$

$$H = (4 \times 4) - \frac{1}{2} \times 10 \times 4^2$$

$$H = 16 - 5 \times 16 = 16 - 80$$

$$H = -64 \text{ m}$$

$$H = 64 \text{ m}$$

## QUESTION

A ball is thrown **vertically downward** with a velocity of 20 m/s from the top of a tower. it hits the ground after some time with a velocity of 80 m/s. the height of the tower is ( $g = 10 \text{ m/s}^2$ )

A 340 m

B 320 m

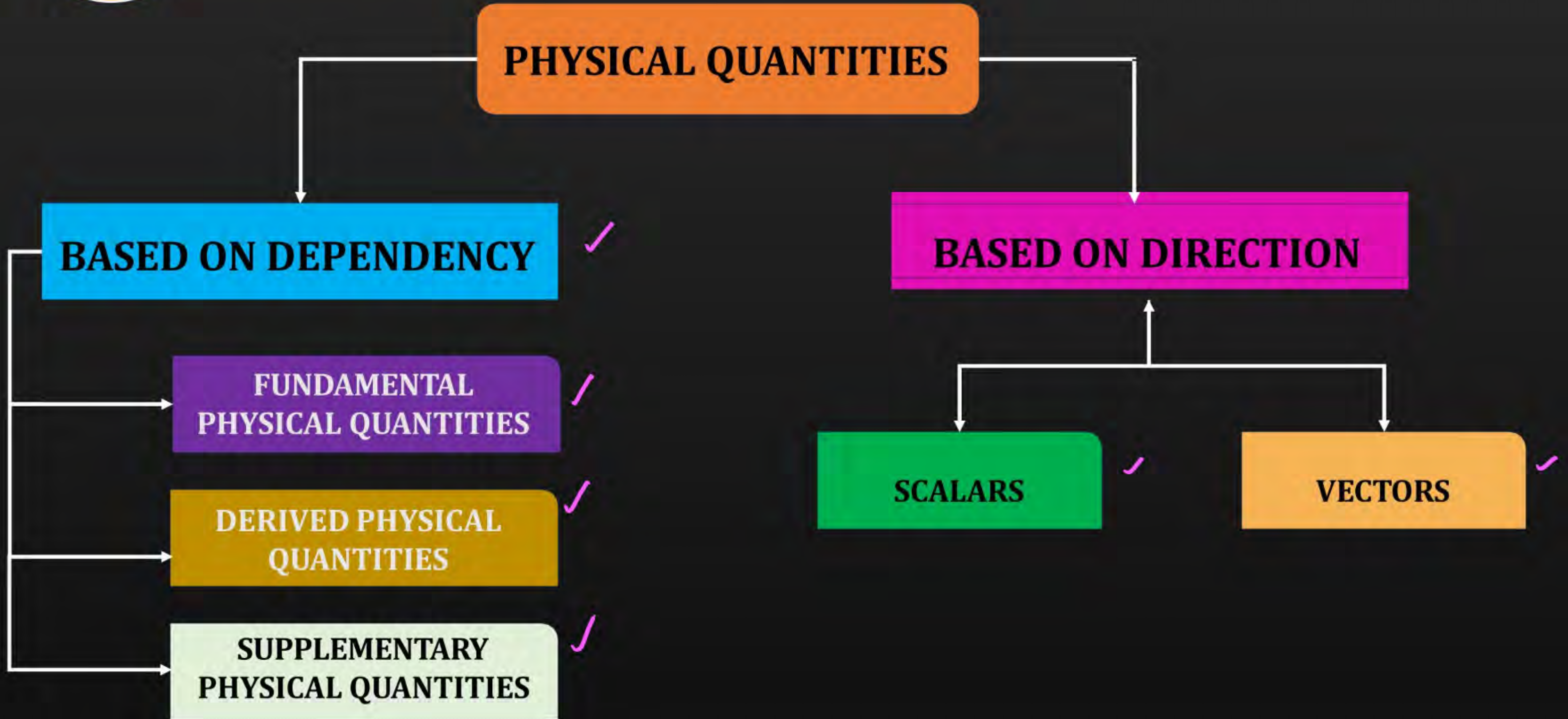
C 300 m

D 360 m

$$u$$
$$v^2 = u^2 + 2as$$
$$(80)^2 = (20)^2 + 2(10)H$$
$$6400 = 400 + 20H$$
$$6000 = 20H$$
$$H = 300\text{m}$$

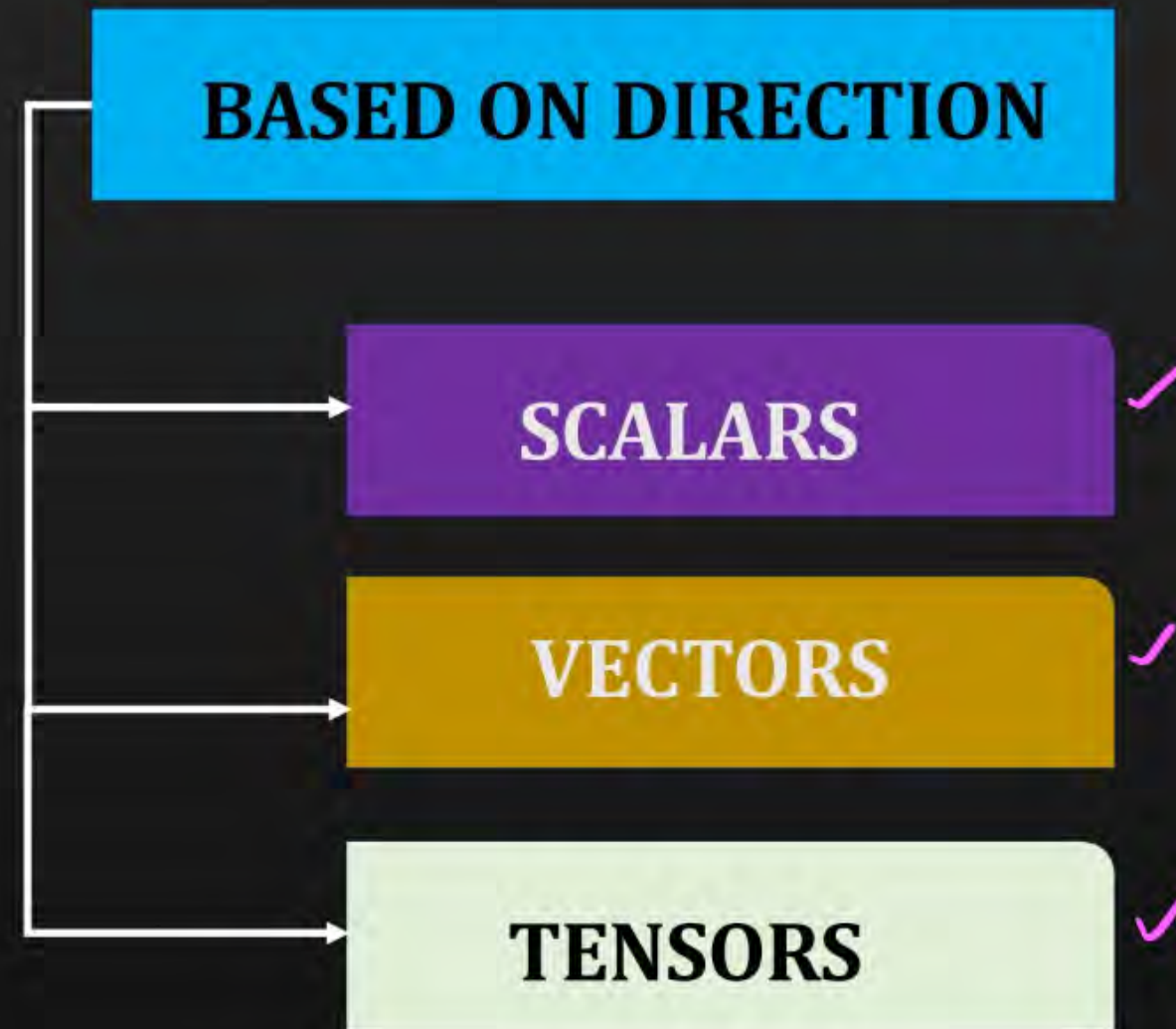


# SCALARS & VECTORS





# SCALARS & VECTORS





## SCALARS & VECTORS

All the physical quantities are classified into 2 categories on the basis of directional and algebra properties.

**1. Scalar Physical Quantity [Scalars]**: The quantity which has magnitude and may or may not have direction but follow scalar addition i.e angle independent.

Ex : Mass, Length, Time, Temperature and current, etc.



# SCALARS & VECTORS

All the physical quantities are classified into 2 categories on the basis of directional and algebra properties.

**2. Vector Physical Quantity [Vector]**: The quantity which has magnitude and have direction and follow vector laws for addition i.e angle dependent.

Ex : Displacement, Velocity, Acceleration, Force, Momentum etc.

## QUESTION

Which of the following is **not** a vector quantity?

- A** Speed
- B** Velocity
- C** Torque
- D** Displacement



## REPRESENTATION OF VECTOR

$$* \vec{A} = |\vec{A}| \hat{A}$$

$$\vec{A} = A \cdot \hat{A}$$

$$* \hat{A} = \frac{\vec{A}}{A}$$

$\vec{A}$  - Vector A

$|\vec{A}|$  - Magnitude of vector A Modulus of vector A Mod of vector A

$\hat{A}$  - Direction of vector A Unit vector along A

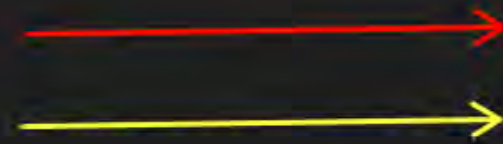


## TYPES OF VECTORS

3. Null Vector  
↳ mag = 0

4. Unit Vector,  
↳ mag = 1

1. **Equal Vectors** – Vectors have same direction and same magnitude.



2. **Parallel Vectors** – Vectors have same direction but may or may not have same magnitude





## VECTOR ADDITION

$$R = \sqrt{A^2 + B^2 + 2AB \cos \theta}$$

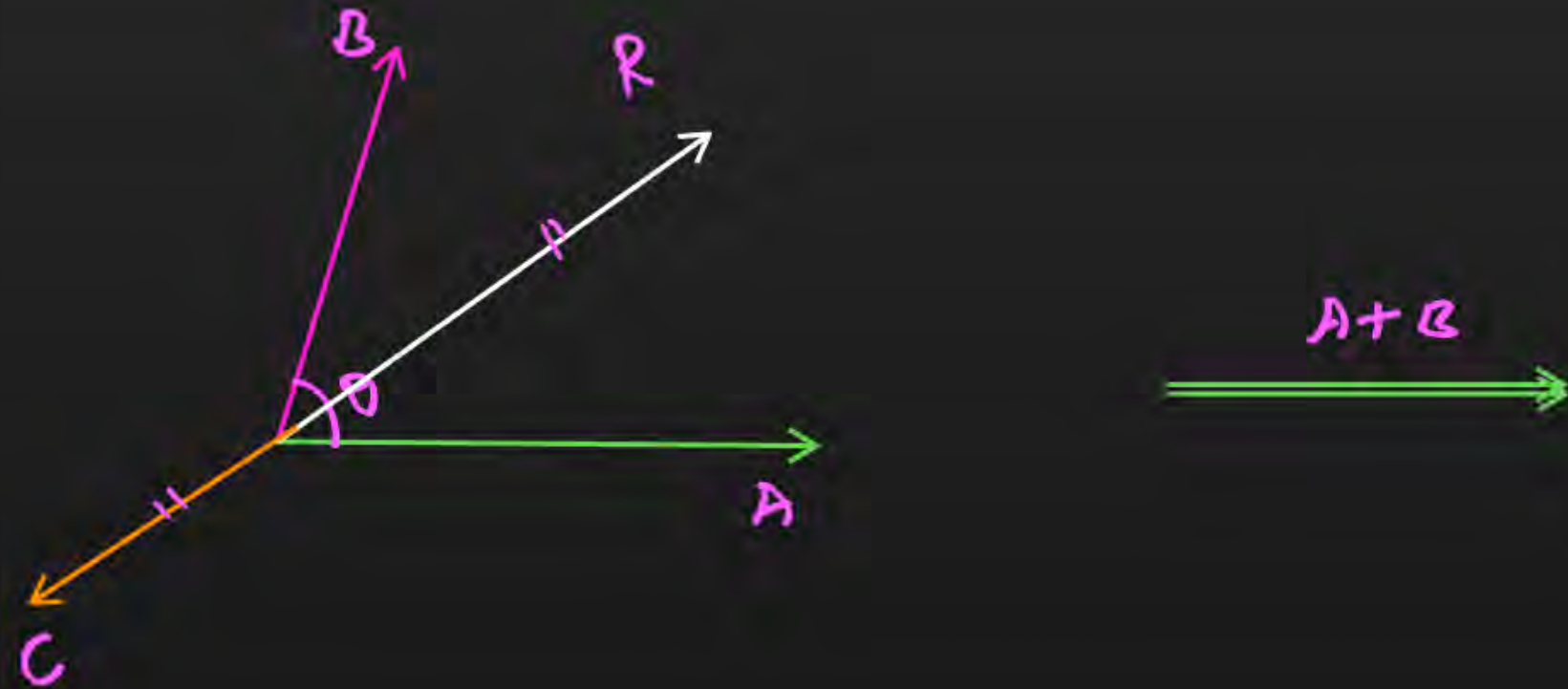
Range of vector,

$$(A - B) \leq R \leq (A + B)$$

**QUESTION**

How many minimum number of coplanar vectors having different magnitudes can be added to given zero resultant.

- A** 2
- B** 3
- C** 4
- D** 5

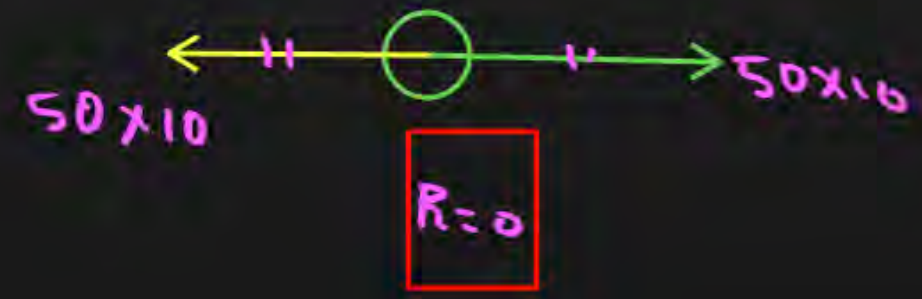


**QUESTION**

$$360 \Rightarrow \frac{2\pi}{\frac{\pi}{50}} = 100 \text{ forces}$$

100 coplanar forces each equal to 10 N act on a body. Each force makes angle  $\pi/50$  with the preceding force. What is the resultant of the forces.

- A** 1000 N
- B** 500 N
- C** 250 N
- D** Zero



## QUESTION

Which pair of the following forces will **never** give resultant force of 2 N?

	A	B		A - B	A + B
<b>A</b>	2 N	and 2 N ✓		0	→ 4
<b>B</b>	1 N	and 1 N ✓		0	→ 2
<b>C</b>	1 N	and 3 N		2	→ 4
<b>D</b>	1 N	and 4 N		3	→ 5

## QUESTION

$$\theta = 90^\circ$$

Forces  $F_1$  and  $F_2$  act on a point mass in two mutually perpendicular directions. The resultant force on the point mass will be

**A**  $F_1 + F_2$

**B**  $F_1 - F_2$

**C**  $\sqrt{F_1^2 + F_2^2}$

**D**  $F_1^2 + F_2^2$

$$R = \sqrt{F_1^2 + F_2^2 + 2F_1F_2 \cos 90^\circ}$$

$$R = \sqrt{F_1^2 + F_2^2}$$

## QUESTION

Two equal forces ( $P$  each) act at a point inclined to each other at an angle of  $120^\circ$ . The magnitude of their resultant

- A  $P/2$
- B  $P/4$
- C  $P$
- D  $2P$

$$R = \sqrt{A^2 + B^2 + 2AB \cos \theta} \quad A \neq B$$

$$R = 2A \cos\left(\frac{\theta}{2}\right), \quad A = B$$

$$R = 2P \cos\left(\frac{120^\circ}{2}\right)$$

$$R = 2P \times \frac{1}{2}$$

$$R = P$$



## DOT PRODUCT

The scalar product of two vectors  $\vec{A}$  &  $\vec{B}$  is a scalar quantity.

$$\vec{A} \cdot \vec{B} = A \cdot B \cos \theta$$

Ex:- Work done, power, energy, speed etc.



## CROSS PRODUCT

The cross product of two vectors  $\vec{A}$  &  $\vec{B}$  is can be written as.

$$\vec{A} \times \vec{B} = AB \sin \theta \hat{n}$$

Ex:- Acceleration, Torque, Linear Velocity, Force etc.



# PROJECTILE MOTION

When a body moves with constant acceleration such that its initial velocity and acceleration are non-collinear then its path is parabola and motion is known as projectile motion.

## PROJECTILE MOTION

OBLIQUE

HORIZONTAL



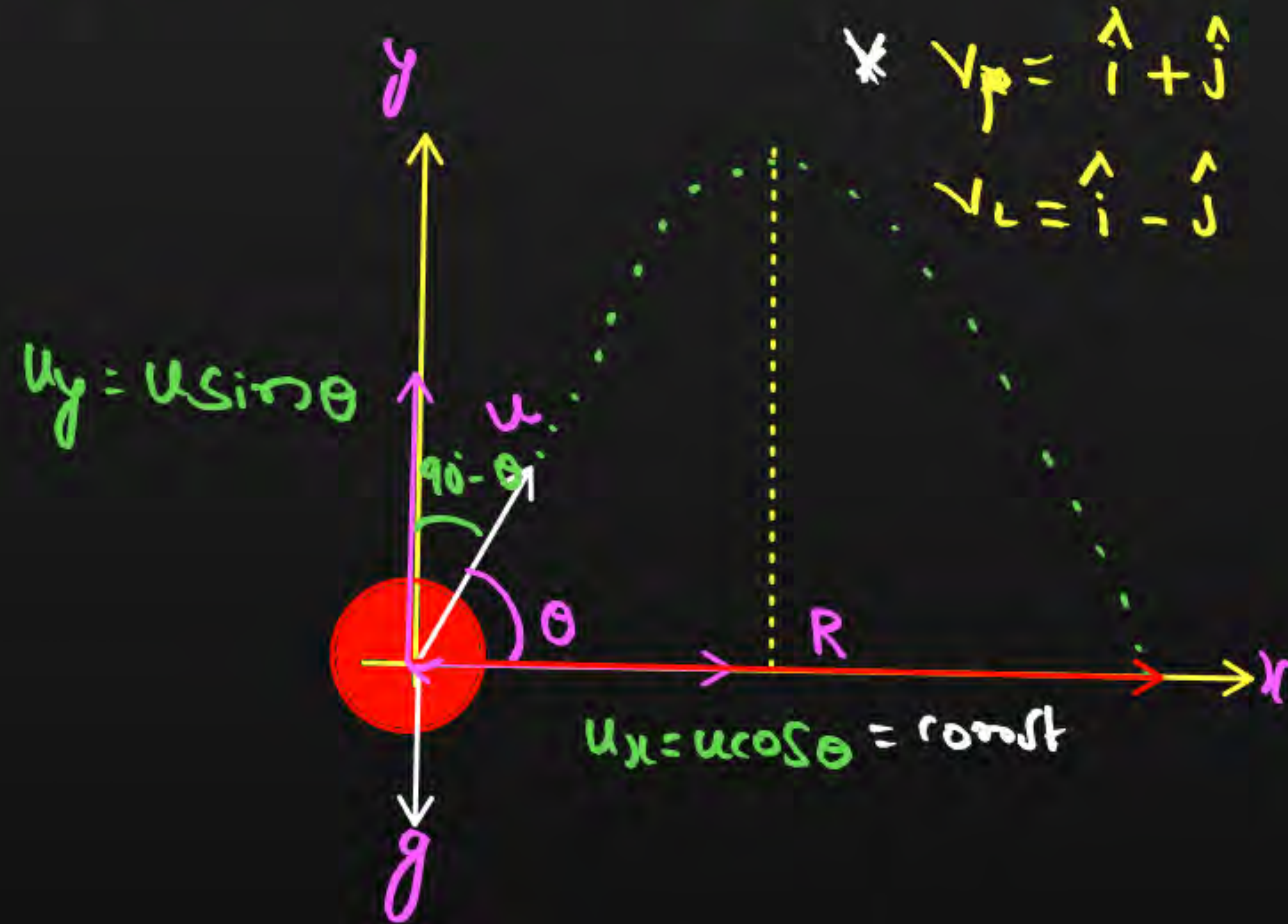
# Ground- Ground Projectile Motion

$$\tan \theta = \frac{P}{B} = \frac{u_y}{u_x}$$

$$\theta = \tan^{-1} \left( \frac{u_y}{u_x} \right)$$

Projectile Motion = Horizontal Motion + Vertical Motion

2D = 1D + 1D



$$* T = \frac{2u_y}{g} = \frac{2u \sin \theta}{g}$$

$$* H = \frac{u_y^2}{2g} = \frac{u^2 \sin^2 \theta}{2g}$$

$$* R = u_x \times T = \frac{2u_x u_y}{g} = \frac{u^2 \sin 2\theta}{g}$$

$$* y = x \tan \theta - \frac{g x^2}{2u^2 \cos^2 \theta} = x \tan \theta \left[ 1 - \frac{x}{R} \right]$$



## Ground- Ground Projectile Motion

**Time of flight (T)** : Time of flight is the time for which projectile remains in air.

At time T particle will be at ground again, i.e. displacement along Y-axis becomes zero.

$$T = \frac{2u_y}{g} = \frac{2u \sin \theta}{g}$$



## Ground- Ground Projectile Motion

**Maximum height (H)**: At maximum height vertical component of velocity becomes zero. At this instant y coordinate is, its maximum height.

$$H = \frac{u^2}{2g} = \frac{u^2 \sin^2 \theta}{2g}$$



## Ground- Ground Projectile Motion

**Horizontal range or Range (R)**: It is the displacement of particle along X-direction during its complete flight.

$$R = \frac{2u_x u_y}{g} = \frac{u^2 \sin 2\theta}{g}$$



# Ground- Ground Projectile Motion

Maximum horizontal range ( $R_{max}$ ):

\*  $R \tan \theta = 4H$

$$R_{max} = \frac{u^2}{g}$$

$$H = \frac{u^2 \sin^2 \theta}{2g}$$

$$H_{max} = \frac{u^2}{2g}$$

$$R = \frac{u^2 \sin 2\theta}{g}, \quad \sin 2\theta = 1$$

$$\sin 2\theta = \sin 90^\circ$$

$$\theta = 45^\circ$$

$$\sin^2 \theta = 1$$

$$\sin^2 \theta = \sin^2 90^\circ$$

$$\theta = 90^\circ$$



# Ground- Ground Projectile Motion

## Comparison of two projectiles :

**Horizontal range** : When two projectiles are thrown with equal speeds at angles  $\theta$  and  $(90^\circ - \theta)$  then their ranges are equal but maximum heights attained are different and time of flights are also different.

$$A = 90^\circ *$$

$$B = 90^\circ - \theta *$$

$$A + B = 90 + (90 - \theta)$$

$$180^\circ - \theta = 90$$

$$\theta = 180^\circ - 90 = 90$$

## Complementary angle

$$A + B = 90^\circ$$

$$30^\circ + 60^\circ = 90^\circ$$

$$45^\circ + 45^\circ = 90^\circ$$

$$15^\circ + 75^\circ = 90^\circ$$

⋮

$$R_0 = \frac{u^2 \sin 2\theta}{\rho}$$

$$R_{90-0} = \frac{u^2 \sin 2(90-0)}{\rho}$$

$$= \frac{u^2 \sin(180-2\theta)}{\rho}$$

$$R_{90-0} = \frac{u^2 \sin 2\theta}{\rho}$$

\* VIP

$$\therefore R_0 = R_{90-0}$$



# Ground- Ground Projectile Motion

Maximum height of projectiles :

$$H = \frac{u^2 \sin^2 \theta}{2g}$$

$$H_{\max} = \frac{u^2}{2g} \rightarrow \theta = 90^\circ$$

$$H_\theta = \frac{u^2 \sin^2 \theta}{2g}$$

$$H_{90-\theta} = \frac{u^2 \sin^2 (90-\theta)}{2g}$$

$$H_{90-\theta} = \frac{u^2 \cos^2 \theta}{2g}$$

\*  $H_\theta \neq H_{90-\theta}$



## Ground- Ground Projectile Motion

Time of flight of projectiles :

$$T_{\theta} = \frac{2u \sin \theta}{g}$$

$$T_{90-\theta} = \frac{2u \sin(90-\theta)}{g}$$

$$T_{90-\theta} = \frac{2u \cos \theta}{g}$$

\*

$$T_{\theta} \neq T_{90-\theta}$$



## Equation of Trajectory

$$y = x \tan \theta - \frac{gx^2}{2u^2 \cos^2 \theta}$$

\*  $y = x \tan \theta \left[ 1 - \frac{x}{R} \right]$



## Important points

Relation between Horizontal Range and Height

$$R \tan \theta = 4H$$

## QUESTION

$$u = u_x \hat{i} + u_y \hat{j}, \quad u_x = 6$$

$$u_y = 8$$

A body is projected from ground with velocity  $(6\vec{i} + 8\vec{j})$  m/s. Find out:

**A**

Time of flight

$$T = \frac{2u_y}{g} = \frac{2 \times 8}{10} = \frac{16}{10} = 1.6 \text{ s}$$

$$T = 1.6 \text{ s}$$

**B**

Maximum height

$$H = \frac{u_y^2}{2g} = \frac{(8)^2}{2 \times 10} = \frac{64}{20} = 3.2 \text{ m}$$

$$H = 3.2 \text{ m}$$

**C**

Horizontal range

$$R = \frac{2u_x u_y}{g} = \frac{2 \times 6 \times 8}{10} = 9.6 \text{ m}$$

$$R = 9.6 \text{ m}$$

**D**

Velocity when body reaches on ground

$$\hookrightarrow 6\hat{i} - 8\hat{j}$$

## QUESTION

A projectile is launched with an initial velocity  $\vec{v}_0 = (2 \text{ m/s}) \hat{i} + (3 \text{ m/s}) \hat{j}$  At the top of the trajectory, the velocity of the particle is (x horizontal direction, y-vertical direction):

$$u_x \hat{i} + u_y \hat{j}$$

**A**  $\sqrt{2^2 + 3^2} \text{ m/s}$

**B** 2 m/s

**C** 3 m/s

**D** 5 m/s

$$v_y = 0$$

$$v_x = u_x = u \cos \theta$$

$v_x = u_x = 2 \text{ m/s}$

**QUESTION**

An arrow is shot into the air. Its range is **200 metres** and its time of flight is **5 s**. If the value of  $g$  is assumed to be  **$10 \text{ ms}^{-2}$** , then the horizontal component of the velocity of arrow is:

- A** 25 m/s
- B** **40 m/s**
- C** 31.25 m/s
- D** 12.5 m/s

$$R = \frac{2u_x u_y}{g} = \frac{u_x}{g} \left( \frac{2u_y}{g} \right) = u_x \times T$$

$$R = u_x T$$

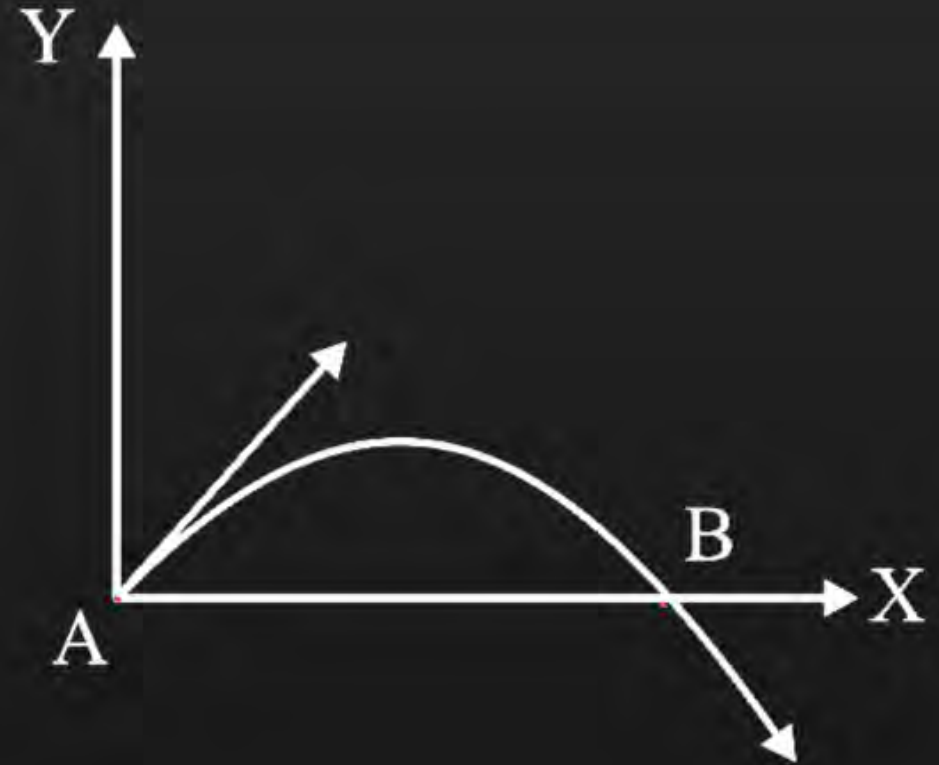
$$u_x = \frac{R}{T} = \frac{200}{5} = 40$$

$$u_x = 40 \text{ m/s}$$

## QUESTION

The velocity of a projectile at the initial point A is  $(2\hat{i} + 3\hat{j})$  m/s. Its velocity (in m/s) at point B is

- A  $-2\hat{i} - 3\hat{j}$
- B  $-2\hat{i} + 3\hat{j}$
- C  $2\hat{i} - 3\hat{j}$
- D  $2\hat{i} + 3\hat{j}$



## QUESTION

Equations of motion of a projectile are given by  $x = 36t$  and  $2y = 96t - 98t^2$  m. The angle of projection is equal to

- A**  $\sin^{-1} \left( \frac{3}{4} \right)$
- B**  $\sin^{-1} \left( \frac{4}{3} \right)$
- C**  $\sin^{-1} \left( \frac{4}{5} \right)$
- D**  $\sin^{-1} \left( \frac{3}{5} \right)$

$$\tan \theta = \frac{u_y}{u_x}$$

$$\tan \theta = \frac{48}{36} = \frac{4}{3}$$

$$\sin \theta = \frac{P}{H} = \frac{4}{5}$$

$$\theta = \sin^{-1} \left( \frac{4}{5} \right)$$

$$u_x = \frac{dx}{dt}$$

$$u_x = 36(1)$$

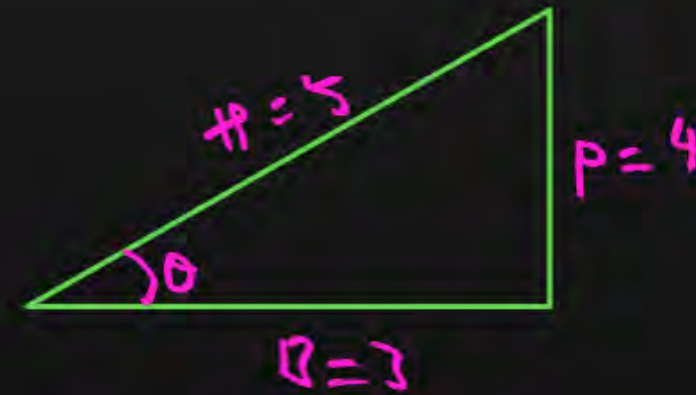
$$u_x = 36 \text{ m/s}$$

$$y = 48t - 49t^2$$

$$u_y = \frac{dy}{dt}$$

$$u_y = 48(1) - 98(1)$$

$$\text{At } t=0 \text{ s, } u_y = 48 \text{ m/s}$$



## QUESTION

A ball is projected with a velocity,  $10 \text{ ms}^{-1}$ , at an angle of  $60^\circ$  with the vertical direction. Its speed at the highest point of its trajectory will be

A Zero

$v_y = 0$

B  $5\sqrt{3} \text{ ms}^{-1}$

C  $5 \text{ ms}^{-1}$

D  $10 \text{ ms}^{-1}$

$$\hookrightarrow v_x = u_x = u \cos \theta$$

$$= 10 \times \cos 30^\circ$$

$$= 10 \times \frac{\sqrt{3}}{2}$$

$$= 5\sqrt{3} \text{ m/s}$$

$$90^\circ - \theta = 90^\circ - 60^\circ = \underline{\underline{30^\circ}}$$

## QUESTION

A ball is thrown at an angle of  $30^\circ$  to the horizontal. It falls on the ground at a distance of  $90\text{m}$ . If the ball is thrown with the same initial speed at an angle  $60^\circ$  to the vertical, it will fall on the ground at a distance of

- A 120 m
- B 27 m
- C  $90\text{ m}$
- D 30 m

$$R_\theta = R_{90-\theta}$$
$$R_{30^\circ} = R_{60^\circ} = 90\text{m}$$

## QUESTION

Two particles are projected with same initial velocity at an angle  $30^\circ$  and  $60^\circ$  with the horizontal. then,

- A their heights will be equal ✗
- B their ranges will be equal ✓
- C their time of flights will be equal ✗
- D their ranges will be different ✗

## QUESTION

Two bodies of same mass are projected with the same velocity at an angle  $30^\circ$  and  $60^\circ$  respectively. The ratio of their horizontal range will be

- A  $1 : 1$
- B  $1 : 2$
- C  $1 : 3$
- D  $2 : \sqrt{3}$

## QUESTION

For angle of projection  $20^\circ$ , range of a projectile is  $R$ . For the same range, another angle of projection should be

**A**  $40^\circ$

**B**  $50^\circ$

**C**  $60^\circ$

**D**  $70^\circ$

$$A + B = 90$$

$$A + 20 = 90$$

$$A = 70$$

## QUESTION

If four balls A, B, C and D are projected with same speed, but angles of  $15^\circ$ ,  $30^\circ$ ,  $45^\circ$  and  $60^\circ$  with the horizontal respectively, the two balls which will fall at **the same place** will be-

*R = same*

**A** A and B ✗

**B** A and D ✗

**C** B and D ✓

**D** A and C ✗

## QUESTION

The horizontal range is four times the maximum height reached by a projectile. The angle of projection is

A  $90^\circ$

B  $75^\circ$

C  $60^\circ$

D  $45^\circ$

$$R \tan \theta = 4H$$

$$4H \tan \theta = 4H$$

$$\tan \theta = 1$$

$$\theta = 45^\circ$$

## QUESTION

If  $R$  is the maximum horizontal range of a particle, then the greatest height attained by it is:

$$\theta = 45^\circ$$

**A**  $R$

**B**  $2R$

**C**  $R/2$

**D**  $R/4$

$$R \tan \theta = 4H$$

$$R_{\text{max}} = 4H_{\text{max}}$$

$$H_{\text{max}} = \frac{R_{\text{max}}}{4}$$

## QUESTION

The equation of a projectile is  $y = \sqrt{3}x - \frac{gx^2}{2}$ . The angle of projection is:

A  $30^\circ$

B  $60^\circ$

C  $45^\circ$

D None

$$y = \tan\theta \cdot x - \frac{gx^2}{2}$$

$$\tan\theta = \sqrt{3}$$

$$\tan\theta = \tan 60^\circ$$

$$\theta = 60^\circ$$

## QUESTION

The equation of a projectile is  $y = 16x - \frac{x^2}{4}$ . The horizontal range is:

**A** 16 m

**B** 8 m

**C** 64 m

**D** 12.8 m

$$y = 16x \left[ 1 - \frac{x}{4 \times 16} \right]$$

$$y = 16x \left[ 1 - \frac{x}{64} \right]$$

$$y = \tan \theta \cdot x \left[ 1 - \frac{x}{R} \right]$$

$$R = 4 \times 16 = 64 \text{ m}$$

**QUESTION**

For ground to ground projectile motion equation of path is  $y = 12x - \frac{3}{4}x^2$ . Given that  $g = 10 \text{ ms}^{-2}$ . What is the **range** of the projectile?

- A** 36m
- B** 30.6 m
- C** 16 m
- D** 12.4 m

$$y = 12x \left[ 1 - \frac{\cancel{3}x^2}{4 \times \cancel{1} \times \frac{x}{4}} \right]$$

$$y = 12x \left[ 1 - \frac{x}{16} \right]$$

$$y = \tan \theta x \left[ 1 - \frac{x}{R} \right]$$

$$R = 16 \text{ m}$$

## QUESTION

A bullet is fired from a gun at the speed of 280 m/s in the direction  $30^\circ$  above the horizontal. The maximum height attained by the bullet is ( $g = 9.8 \text{ ms}^{-2}$ ,  $\sin 30^\circ = 0.5$ )

- A 3000 m
- B 2800 m
- C 2000 m
- D 1000 m

$$\sin 30^\circ = \frac{1}{2}$$

$$\sin^2 30^\circ = \left(\frac{1}{2}\right)^2 = \frac{1}{4}$$

$$H = \frac{u^2 \sin^2 \theta}{2g}$$

$$H = \frac{(280)^2 \sin^2 30^\circ}{2 \times 9.8}$$

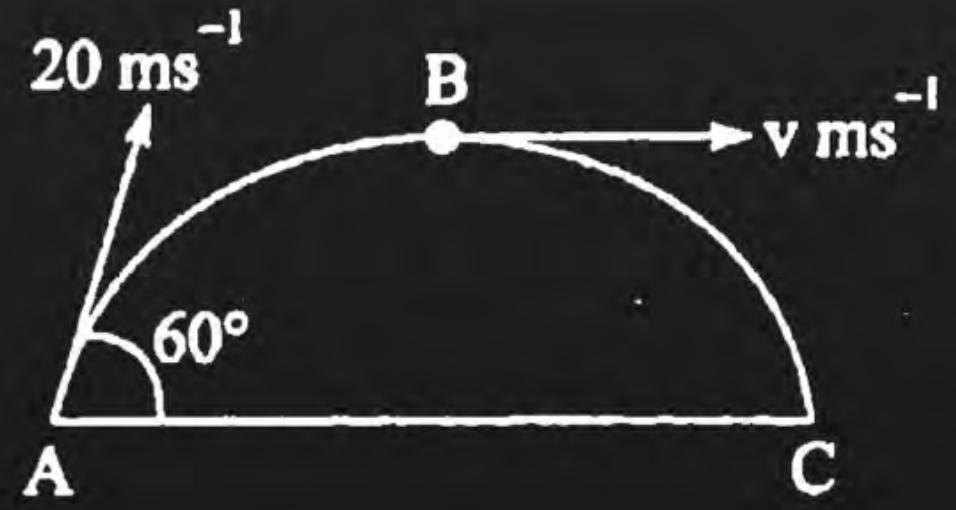
$$H = 1000 \text{ m}$$

**QUESTION**

H.V

A ball is projected from point A with velocity  $20 \text{ ms}^{-1}$  at an angle  $60^\circ$  to the horizontal direction. At the highest point B of the path (as shown in figure), the velocity  $v \text{ ms}^{-1}$  of the ball will be:

- A** 20
- B**  $10\sqrt{3}$
- C** Zero
- D** 10



## QUESTION

The horizontal range and the maximum height of a projectile are equal. The angle of projection of the projectile is:

$$R \tan \theta = 4H$$

**A**  $\theta = \tan^{-1} \left( \frac{1}{4} \right)$

**B**  $\theta = \tan^{-1} (4)$

**C**  $\theta = \tan^{-1} (2)$

**D**  $\theta = 45^\circ$

## QUESTION

A missile is fired for maximum range with an initial velocity of 20 m/s. If  $g = 10 \text{ m/s}^2$ , the range of the missile is:

- A 40 m
- B 50 m
- C 60 m
- D 20 m

## QUESTION

For angles of projection of a projectile at angles  $(45^\circ - \theta)$  and  $(45^\circ + \theta)$ , the horizontal ranges described by the projectile are in the ratio of:

- A** 1:1
- B** 2:3
- C** 1:2
- D** 3:2

## QUESTION

H.C.

The maximum range of a gun on horizontal terrain is 16 km . If  $g = 10 \text{ ms}^{-2}$ , then muzzle velocity of a shell must be:

- A**  $100 \text{ ms}^{-1}$
- B**  $200\sqrt{2} \text{ ms}^{-1}$
- C**  $400 \text{ ms}^{-1}$
- D**  $800 \text{ ms}^{-1}$

**Thank**

**You**