



# FORMULA SHEET ( 11<sup>th</sup> Class)

Ultimate KCET Crash Course 2026

**Subject: Physics**

**Chapter: All Chapters**

## Units and Measurements

### Physical Quantities

A physical quantity is any quantity that can be measured.

Physical Quantity = Numerical value  $\times$  Unit

### SI Base Units

| Physical Quantity   | Symbol | SI Unit  | Unit Symbol |
|---------------------|--------|----------|-------------|
| Length              | $l$    | metre    | m           |
| Mass                | $m$    | kilogram | kg          |
| Time                | $t$    | Second   | s           |
| Electric current    | $I$    | Ampere   | A           |
| Temperature         | $T$    | kelvin   | K           |
| Amount of substance | $n$    | mole     | mol         |
| Luminous intensity  | $Iv$   | candela  | cd          |

### Derived Units (Important)

| Quantity     | Formula                   | SI unit      |
|--------------|---------------------------|--------------|
| Area         | $A = l \times b$          | $m^2$        |
| Volume       | $V = l \times b \times h$ | $m^3$        |
| Speed        | $v = \frac{d}{t}$         | $m/s$        |
| Acceleration | $a = \frac{v-u}{t}$       | $m/s^2$      |
| Force        | $F = ma$                  | Newton       |
| Energy       | $E = F.d$                 | Joule        |
| Power        | $P = \frac{E}{t}$         | Watt ( $W$ ) |



## Dimensional Formula

$$[Q] = M^a L^b T^c$$

**Where:**

$M$  = mass

$L$  = length

$T$  = time

$a, b, c$  = powers

## Examples

| Quantity     | Dimensional Formula |
|--------------|---------------------|
| Velocity     | $[LT^{-1}]$         |
| Acceleration | $[LT^{-2}]$         |
| Force        | $[MLT^{-2}]$        |
| Energy       | $[ML^2T^{-2}]$      |
| Power        | $[ML^2T^{-3}]$      |
| Pressure     | $[ML^{-1}T^{-2}]$   |

## Conversion of Units

$$\text{New value} = \text{Old value} \times \left( \frac{\text{Old unit}}{\text{New unit}} \right)$$

## Significant Figures (Rules)

- ❖ All non-zero digits are significant
- ❖ Zeros between non-zero digits are significant
- ❖ Leading zeros are not significant
- ❖ Trailing zeros after decimal are significant

## Rounding Rule

- ❖ If next digit  $< 5 \rightarrow$  ignore
- ❖ If  $\geq 5 \rightarrow$  increase previous digit by



## Errors in Measurement

### Absolute Error

$$\Delta x = |x_{\text{measured}} - x_{\text{true}}|$$

### Mean Absolute Error

$$\Delta x_{\text{measured}} = \frac{\sum |\Delta x|}{n}$$

### Relative Error

$$\frac{\Delta x}{x}$$

### Percentage Error

$$\text{Percentage error} = \frac{\Delta x}{x} \times 100$$

## Error in Calculations

(a) Addition / Subtraction

$$\Delta Z = \Delta A + \Delta B$$

(b) Multiplication / Division

$$\frac{\Delta Z}{Z} = \frac{\Delta A}{A} + \frac{\Delta B}{B}$$

(c) Power

$$\frac{\Delta Z}{Z} = n \frac{\Delta A}{A}$$

## Vernier Calipers

Least Count

$$LC = 1 \text{ MSD} - 1 \text{ VSD}$$

Reading

$$\text{Reading} = \text{MSR} + (\text{VSR} \times \text{LC})$$

Screw Gauge

Least Count

$$LC = \frac{\text{Pitch}}{\text{No. of divisions}}$$

Reading

$$\text{Reading} = \text{PSR} + (\text{CSR} \times \text{LC})$$



## Symbol Meanings (Quick)

### Symbol

$l, b, h$

$d$

$t$

$u, v$

$a$

$F$

$E$

$P$

$\Delta x$

MSR

VSR

PSR

CSR

### Meaning

length, breadth, height

distance

time

initial & final velocity

acceleration

force

energy

power

absolute error

Main scale reading

Vernier scale reading

Pitch scale reading

Circular scale reading



## Motion in a Straight Line

### Fundamental Definitions

| Formula   | Description   | Meaning of Symbols   |
|---|---|--|
| <b>Average Velocity:</b> $v_{avg} = \frac{\Delta x}{\Delta t}$                | Total displacement divided by the total time interval.        | $\Delta x$ : Change in position<br><b>(Displacement)</b> (m) |
|   |   | $\Delta t$ : Time interval (s)                               |
| <b>Average Speed:</b><br>$s_{avg} = \frac{\text{Total Distance}}{\Delta t}$   | Total path length divided by the total time interval.         | Total distance: Total path length traveled (m)               |
| <b>Instantaneous Velocity:</b> $v = \frac{dx}{dt}$                            | The rate of change of position with respect to time. (Vector) | $dx/dt$ : Derivative of position (x) w.r.t time (t)          |
| <b>Instantaneous Acceleration:</b><br>$a = \frac{dv}{dt} = \frac{d^2x}{dt^2}$ | The rate of change of velocity with respect to time. (Vector) | $dv/dt$ : Derivative of velocity (v) w.r.t time (t)          |
|   |   | $d^2x/dt^2$ : Second derivative of position w.r.t time       |

### Kinematic Equations for Uniform Acceleration

These equations are only valid when acceleration ( $a$ ) is constant.

| Formula  | Description  | Meaning of Symbols   |
|--|--|--|
| <b>1. Velocity-Time Relation:</b><br>$v = u + at$  | Final velocity after time $t$ .                                      | $u$ : Initial velocity (m/s)   |
|  |  | $v$ : Final velocity (m/s)   |
| <b>2. Position-Time Relation:</b><br>$s = ut + \frac{1}{2}at^2$                                    | Displacement (s) in time $t$ .                                       | $a$ : Constant acceleration (m/s <sup>2</sup> )                      |
|  |  | $t$ : Time interval (s)  |
| <b>3. Velocity-Displacement Relation (Torricelli's):</b> $v^2 = u^2 + 2as$                         | Final velocity after displacement $s$ .                              | $s$ : Displacement (m)   |
| <b>4. Displacement in the <math>n^{\text{th}}</math> second</b><br>$S_n = u + \frac{a}{2}(2n - 1)$ | Displacement traveled <i>only</i> during the $n^{\text{th}}$ second. | $n$ : The specific second (e.g., 3 <sup>rd</sup> , 5 <sup>th</sup> ) |

## Motion Under Gravity (Free Fall)

This is a special case of uniform acceleration where  $a$  is constant and equal to the acceleration due to gravity ( $g$ ). (Assuming upward is positive and downward is negative, or vice-versa, consistently.)

**Acceleration:**  $a = -g$  (always pointing downwards)

$g \approx 9.8\text{m/s}^2$  or  $10\text{m/s}^2$  (as specified in the problem)

**Maximum Height (H max):** The final velocity ( $v$ ) at the highest point is zero.

$$H_{\max} = \frac{u^2}{2g}$$

**Time of Ascent ( $t_a$ ):** Time taken to reach maximum height.

$$t_a = \frac{u}{g}$$

**Time of Flight ( $T$ ):** Total time in air ( $T = t_a + t_d$ , where  $t_d$  is time of descent).

$$T = 2u/g$$

**The kinematic equations become:**

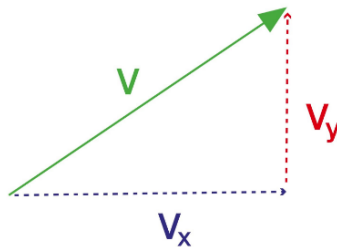
$$v = u - gt$$

$$h = ut - \frac{1}{2}gt^2$$

$$v^2 = u^2 - 2gh$$

## Relative Velocity

Relative velocity is the velocity of an object A with respect to an object B



| Formula   | Description  | Meaning of Symbols                        |
|---|--|---|
| <b>Velocity of A w.r.t B:</b><br>$v_{AB} = v_A - v_B$ | Vector difference between the individual velocities. | $v_{AB}$ : Relative velocity of A w.r.t B |



| Formula | Description | Meaning of Symbols                    |
|---------|-------------|---------------------------------------|
|         |             | $v_A$ : Absolute velocity of object A |
|         |             | $v_B$ : Absolute velocity of object B |

\*\*For two objects moving in the same direction: The magnitude of relative velocity is

$$|v_A - v_B|$$

\*\*For two objects moving in the opposite direction: The magnitude of relative velocity is

$$|v_A + v_B|.$$

| Graph Type                  | Slope Represents             | Area Under Graph Represents                   |
|-----------------------------|------------------------------|---|
| Position-Time ( $x-t$ )     | Velocity ( $v = dx/dt$ )     | N/A   |
| Velocity-Time ( $v-t$ )     | Acceleration ( $a = dv/dt$ ) | Displacement ( $\Delta x = \int v dt$ )       |
| Acceleration-Time ( $a-t$ ) | Jerk                         | Change in Velocity ( $\Delta v = \int a dt$ ) |

## Motion in a Plane

### Vectors



Vectors are the foundation of 2D motion

| Concept         | Formula   | Symbol Meanings                                    |
|-----------------|---|--|
| Magnitude       | \$  | A  |
| Resultant (Sum) | $R = \sqrt{P^2 + Q^2 + 2PQ \cos \theta}$                | $P, Q$ : Magnitudes; $\theta$ : Angle between them |
| Direction of R  | $\tan \alpha = \frac{Q \sin \theta}{P + Q \cos \theta}$ | $\alpha$ : Angle of $R$ with vector $P$            |
| Dot Product     | $A \cdot B = AB \cos \theta$                            | Result is a scalar                                 |
| Cross Product   | \$  | $A \cdot B = AB \cos \theta$                       |

### Projectile Motion (Ground-to-Ground)

Assumes a particle is projected with velocity  $u$  at an angle  $\theta$  to the horizontal.

Time of Flight ( $T$ )

$$T = \frac{2u \sin \theta}{g}$$

Maximum Height ( $H$ ):

$$H = \frac{u^2 \sin^2 \theta}{2g}$$

Horizontal Range ( $R$ )

$$R = \frac{u^2 \sin 2\theta}{g}$$

Note: Max range occurs at  $\theta = 45^\circ$ .

Equation of Trajectory:

$$y = x \tan \theta - \frac{gx^2}{2u^2 \cos^2 \theta}$$

Symbols:

$u$ : Initial velocity

$\theta$ : Angle of projection

$g$ : Acceleration due to gravity ( $\approx 9.8 \text{ m/s}^2$ ):

$x, y$ : Horizontal and vertical coordinates at time  $t$ .

Horizontal Projectile (From Height  $h$ )

When an object is thrown horizontally from a tower of height  $h$ .



Time to reach ground:  $t = \sqrt{\frac{2h}{g}}$

Horizontal Range:  $R = u\sqrt{\frac{2h}{g}}$

Velocity at any time  $t: v = \sqrt{u^2 + (gt)^2}$

### Uniform Circular Motion (UCM)

Motion in a circle with constant speed.

| Quantity           | Formula                            | Symbol Meanings                                      |
|--------------------|------------------------------------|--|
| Angular Velocity   | $\omega = \frac{v}{r} = 2\pi f$    | $v$ : Linear velocity; $r$ : Radius; $f$ : Frequency |
| Centripetal Accel. | $a_c = \frac{v^2}{r} = \omega^2 r$ | Always directed toward the center                    |
| Centripetal Force  | $F_e = \frac{mv^2}{r}$             | $m$ : Mass of the object                             |
| Time Period        | $T = \frac{2\pi}{\omega}$          | Time for one full revolution                         |

### Relative Motion In 2d

Useful for "Rain-Man" or "River-Boat" problems.

Velocity of A w.r.t B:  $v_{AB} = v_A - v_B$

River Crossing (Shortest Path):  $\sin \theta = \frac{v_r}{v_m}$

( $v_r$ : River velocity,  $v_m$ : Man's velocity in still water)

River Crossing (Shortest Time):  $t = d/v_m$

( $d$ : Width of the river)

Would you like me to generate a set of practice problems based on these formulas?

## Newton's Law Motion

### Newton's Second Law & Momentum

Newton's laws form the backbone of classical mechanics. The most mathematically significant is the Second Law.

- ❖ Linear Momentum:  $p = mv$
- ❖ Newton's second Law :  $F_{net} = \frac{dp}{dt} = ma$  ( for constant mass)
- ❖ Impulse ( $J$ ):  $J = \int Fdt = \Delta p = m(v_f - v_i)$

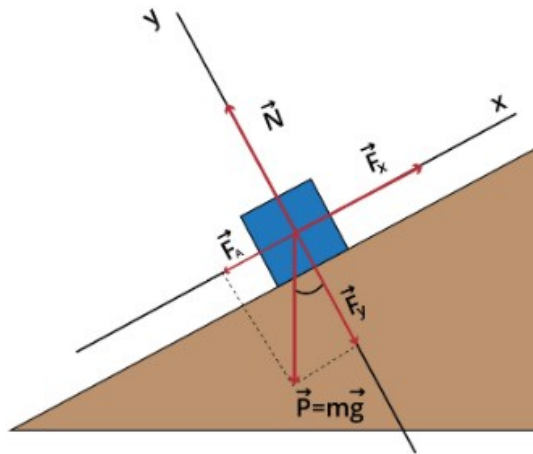
### Symbols:

- ❖  $m$  : Mass of the object
- ❖  $v$  : Velocity
- ❖  $a$  : Acceleration
- ❖  $F_{net}$  : Net external force
- ❖  $t$  : Time

### Common Forces & Free Body Diagrams (FBD)

When solving problems, identifying the forces acting on a body is crucial.

- ❖ Weight ( $W$ ):  $W = mg$
- ❖ Normal Force ( $N$  or  $R$ ): Acts perpendicular to the surface of contact.
- ❖ Tension ( $T$ ): Acts along a string/rope, always pulling away from the body.
- ❖ Spring Force ( $F_s$ ):  $F_s = -kx$  (Hooke's Law)



### Friction

Friction opposes the relative motion (or the tendency of motion) between two surfaces.

- ❖ Static Friction ( $f_s$ ) /  $0 \leq f_s \leq \mu_s N$
- ❖ Limiting Friction ( $f_{\max}$ ) :  $f_{\max} = \mu_s N$
- ❖ Kinetic Friction ( $f_k$ )  $f_k = \mu_k N$
- ❖ Angle of Friction ( $\lambda$ ): ( $\lambda$ ):  $\tan \lambda = \mu_s$
- ❖ Angle of Repose ( $\alpha$ ): The maximum angle of an incline at which a block remains stationary.  $\tan \alpha = \mu_s$

### Symbols:

- ❖  $\mu_s$  : Coefficient of static friction
- ❖  $\mu_k$  : Coefficient of kinetic friction
- ❖  $N$  : Normal reaction force

### Constraint Motion & Pulley Systems

For ideal pulleys (massless and frictionless) and inextensible strings:

Simple Pulley (Atwood Machine):  $\alpha = \frac{(m_2 - m_1)g}{m_1 + m_2}$

$$T = \frac{2m_1 + m_2 g}{m_1 + m_2}$$

Constraint Relation:  $\sum T \cdot v = 0 \quad \sum T \cdot \alpha = 0$

### Circular Motion & Banking

For a vehicle to turn safely without skidding:

- ❖ Centripetal Force:  $F_c = \frac{mv^2}{r} = m\omega^2 r$

- ❖ Bending of a Cyclist:  $\tan \theta = \frac{v^2}{rg}$

- ❖ Banking of Roads (without friction):  $\tan \theta = \frac{v^2}{rg}$

- ❖ Maximum Safe Speed on Banked Road (with friction):

$$v_{\max} = \sqrt{rg \left( \frac{\mu_o + \tan \theta}{1 - \mu_s \tan \theta} \right)}$$

**Symbols:**

- $r$  : Radius of the circular path  
 $\omega$  : Angular velocity  
 $\theta$  : Angle of banking or bending

**Pseudo Force**

Used in non-inertial (accelerating) frames of reference to make Newton's Laws applicable

Pseudo Force ( $F_p$ ):  $F_p = -ma_o$

**Symbols:**

$a_o$  : Acceleration of the observer/frame. (The force is applied in the direction opposite to the frame's acceleration).



## Work Done

Work is a scalar quantity representing the energy transferred by a force.

- ❖ Work by a Constant Force:  $W = F \cdot s = \cos \theta$
- ❖ Work by a Variable Force:  $W = \int_{s_1}^{s_2} F \cdot ds$
- ❖ Work Done by Gravity:  $W_g = \pm mgh$  (Positive if moving down, negative if moving up)
- ❖ Work Done by a Spring:  $W_s = \frac{1}{2}k(x_i^2 - x_f^2)$

## Symbols:

- ❖  $W$  : Work done (Joule,  $J$ )
- ❖  $F$  : Force vector (Newton,  $N$ )
- ❖  $s$  : Displacement vector (Meter,  $m$ )
- ❖  $\theta$  : Angle between Force and Displacement
- ❖  $k$  : Spring constant ( $N/m$ )
- ❖  $x_i, x_f$  : Initial and final deformation of the spring

## Kinetic & Potential Energy

Energy is the capacity to do work.

- ❖ Kinetic Energy (KE):  $K = \frac{1}{2}mv^2 = \frac{p^2}{2m}$
- ❖ Gravitational Potential Energy (PE):  $U = mgh$
- ❖ Elastic Potential Energy (Spring):  $U_s = \frac{1}{2}kx^2$
- ❖ Mechanical Energy ( $E$ ):  $E = K + U$

## Symbols:

- ❖  $m$  : Mass (kg)
- ❖  $v$  : Velocity ( $m/s$ )
- ❖  $p$  : Linear momentum ( $p = mv$ )
- ❖  $g$  : Acceleration due to gravity ( $\approx 9.8 \text{ m/s}^2$ )
- ❖  $h$  : Height from reference level

## Work-Energy Theorem & Conservation

These principles are the most powerful tools for solving complex mechanics problems.



- ❖ Work-Energy Theorem:  $W_{net} = \Delta K = K_f - K_i$  (Net work done by ALL forces equals change in Kinetic Energy)
- ❖ Law of Conservation of Mechanical Energy:  $K_i + U_i = K_f + U_f$  (Applicable only when only conservative forces do work)
- ❖ Conservative Force Relation:  $F = -\frac{dU}{dx}$

## Power

Power is the rate at which work is done or energy is transferred.

- ❖ Average Power:  $P_{avg} = \frac{W}{t} = \frac{\Delta E}{t}$
- ❖ Instantaneous Power:  $P = \frac{dW}{dt} = F \cdot v = Fv \cos \theta$
- ❖ Efficiency ( $\eta$ ):  $\eta = \left( \frac{P_{output}}{P_{input}} \right) \times 100\%$

## Symbols:

- ❖  $P$  : Power (Watt, W or J/s)
- ❖  $t$  : Time (s)
- ❖  $v$  : Instantaneous velocity

## Collisions (One Dimension)

- ❖ Conservation of Momentum:  $m_1v_1 + m_2v_2 = m_1v_2 + m_2v_2$
- ❖ Coefficient of Restitution ( $e$ ):  $e = \frac{\text{Velocity of separation}}{\text{Velocity of Approach}} = \frac{v_2 - v_1}{u_1 - u_2}$
- ❖ Elastic Collision:  $e = 1$  (KE is conserved)

Inelastic Collision:  $0 < e < 1$  (KE is NOT conserved)

Perfectly Inelastic:  $e = 0$  (Bodies stick together)

Would you like me to provide a summary of Vertical Circular Motion or some shortcut tricks for solving pulley-block systems using work-energy?

## System of Particles and Rotational Motion

### Center of Mass (COM)



The point where the entire mass of the system can be supposed to be concentrated. For Discrete Particles:

$$R_{cm} = \frac{\sum m_i r_i}{\sum m_i}$$

### For Continuous Bodies:

$$R_{cm} = \frac{1}{M} \int r dm$$

### Rotational Kinematics

These formulas apply when the angular acceleration ( $\alpha$ ) is constant

| Linear Motion              | Rotational Motion                             | Relationship    |
|----------------------------|---|-----------------|
| Displacement ( $s$ )       | Angular Displacement ( $\theta$ )             | $s = r\theta$   |
| Velocity ( $v$ )           | Angular Velocity ( $\omega$ )                 | $v = r\omega$   |
| Acceleration ( $a$ )       | Angular Acceleration ( $\alpha$ )             | $\alpha_t = ra$ |
| $v = u + at$               | $\omega = \omega_o + \alpha t$                | —               |
| $s = ut + \frac{1}{2}at^2$ | $\theta = \omega_o t + \frac{1}{2}\alpha t^2$ | —               |

### Moment of Inertia ( $I$ )

The rotational equivalent of mass. It depends on the distribution of mass relative to the axis of rotation

General Formula:  $I = \sum m_i r_i^2$   $I = \int r^2 dm$

Radius of Gyration ( $k$ ):  $I = Mk^2 \Rightarrow k = \sqrt{I/M}$

### Important Theorems

Parallel Axis Theorem:  $I = I_{cm} + Md^2$  (Where  $d$  is the distance between the parallel axes)

Perpendicular Axis Theorem:  $I_z = I_x + I_y$  (Only for 2D planar objects)

### Torque and Angular Momentum

These describe the "turning" effect and the "quantity of rotation."



"Torque ( $\tau$ ):

$$\tau = r \times F = rF \sin \phi$$

$$\tau = I\alpha$$

**Angular Momentum ( $L$ ):**

$$L = r \times p = I\omega$$

**Law of Conservation of Angular Momentum:** If  $\tau_{ext} = 0$  Then  $L = \text{Constant}$   $I_1\omega_1 = I_2\omega_2$

**Work, Power, and Energy**

Rotational Kinetic Energy:  $K_{rot} = \frac{1}{2}I\omega^2$

Work Done :  $W = \int \tau d\theta$

Power :  $P = \tau\omega$

Total KE (Rolling without slipping):

$$K_{total} = K_{trans} + K_{rot} = \frac{1}{2}Mv_{cm}^2 + \frac{1}{2}I_{cm}\omega^2$$

$$K_{total} = \frac{1}{2}Mv^2 \left( 1 + \frac{k^2}{R^2} \right)$$

**Symbol Meanings**

$m, M$  : Mass of particle/body

$r$  : Position vector from the axis

$v, \omega$  : Linear velocity / Angular velocity

$\alpha, \alpha$  : Linear acceleration / Angular acceleration

$I$  : Moment of Inertia

$T$  : Torque

$L$  : Angular Momentum

$k$  : Radius of gyration

$R$  : Radius of the object

## Gravitation

**Symbol**

**Meaning**

**SI Unit**



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|           |                                      |                              |
|-----------|--------------------------------------|------------------------------|
| $G$       | Universal Gravitational Constant     | $\text{N.m}^2 / \text{kg}^2$ |
| $M, m$    | Masses of the objects                | $\text{kg}$                  |
| $r, R$    | Distance between masses or radius    | $m$                          |
| $g$       | Acceleration due to gravity          | $\text{m/s}^2$               |
| $g'$      | Modified acceleration due to gravity | $\text{m/s}^2$               |
| $V$       | Gravitational Potential              | $\text{J/kg}$                |
| $U$       | Gravitational Potential Energy       | $J$                          |
| $v_e$     | Escape Velocity                      | $\text{m/s}$                 |
| $v_o$     | Orbital Velocity                     | $\text{m/s}$                 |
| $T$       | Time Period of Orbit                 | $S$                          |
| $\rho$    | Density                              | $\text{kg /m}^3$             |
| $h$       | Height above the surface             | $m$                          |
| $d$       | Depth below the surface              | $m$                          |
| $\omega$  | Angular velocity of Earth            | $\text{rad/s}$               |
| $\lambda$ | Latitude angle                       | degrees or radians           |

### Newton's Law of Gravitation

- ❖ The gravitational force of attraction between two point masses  $M$  and  $m$ , separated by a distance  $r$ :

$$F = \frac{GMm}{r^2}$$

### Vector Form (Force on $m_2$ due to $m_1$ ):

- ❖  $F_{21} = -\frac{Gm_1m_2}{r^2} \hat{r}_{12}$

where  $\hat{r}_{12}$  is a unit vector pointing from  $m_1$  to  $m_2$ .

### Acceleration Due to Gravity ( $g$ )

#### On the Earth's Surface

- ❖ The acceleration due to gravity on the surface of a planet of mass  $M$  and radius  $R$ :

$$= \frac{GM}{R^2}$$

- ❖ If the Earth's average density is  $\rho$ :  $M = \frac{4}{3}\pi R^3 \rho$



$$g = \frac{G}{R^2} \left( \frac{4}{3} \pi R^3 \rho \right) = \frac{4}{3} \pi G R \rho$$

### Variation of $g$ .

- ❖ Effect of Altitude (Height,  $h$ ) At a height  $h$  above the Earth's surface ( $R_e$  is Earth's radius):

**Exact Formula:**  $gh = \frac{GM}{(R_e + h)^2} = g \left( \frac{R_e}{R_e + h} \right)^2$

### Approximate Formula (for $h \ll R_e$ )

$$gh \approx g \left( 1 - \frac{2h}{R_e} \right)$$

Note:  $g_h$  decreases with altitude.

### Effect of Depth ( $d$ ) At a depth $d$ below the Earth's surface:

$$g_d = g \left( 1 - \frac{d}{R_e} \right)$$

Note:  $g_d$  decreases linearly with depth and is zero at the center ( $d = R_e$ ).

### Effect of Latitude ( $\lambda$ ) and Rotation

- ❖ Due to the Earth's rotation (angular velocity  $\omega$ ):
- ❖  $g' = g - R_e \omega^2 \cos^2 \lambda$
- ❖ At the poles ( $\lambda = 90^\circ$ ):  $g' = g$  (No effect)
- ❖ At the equator: ( $\lambda = 0^\circ$ ):  $g' = g - R_e \omega^2$  (Minimum  $g'$ )

### Gravitational Field and Potential

- ❖ Gravitational Field Intensity ( $E$ )

The force experienced by a unit mass ( $m = 1$ ) at a point.

$$E = \frac{F}{m}$$

### For a point mass $M$ at distance $r$ :



$$E = \frac{GM}{r^2}$$

### Gravitational Potential ( $V$ )

- ❖ The work done to bring a unit mass from infinity to a point in the field

$$V = -\int_{\infty}^r E \cdot dr$$

### For a point mass $M$ at distance $r$ :

- ❖ 
$$V = -\frac{GM}{r}$$

### Gravitational Potential Energy ( $U$ )

- ❖ The work done to assemble two masses  $M$  and  $m$  at a distance  $r$ .

$$U = mV = -\frac{GMm}{r}$$

Note: Gravitational potential and potential energy are always negative for attractive forces.

### Satellite Motion and Orbital Mechanics

- ❖ Consider a satellite of mass  $m$  orbiting a planet of mass  $M$  (typically  $M \gg m$ ) in a circular orbit of radius  $r$ .

### Orbital Velocity ( $v_o$ )

- ❖ Centripetal force is provided by the gravitational force  $\frac{mv_o^2}{r} = \frac{GMm}{r^2}$

$$v_o = \sqrt{\frac{GM}{r}}$$

- ❖ If the satellite is close to the planet's surface ( $r \approx R$ )

$$v_o \approx \sqrt{\frac{GM}{R}} = \sqrt{gR}$$

- ❖ Time Period of Orbit ( $T$ )

$$T = \frac{2\pi r}{v_o} = 2\pi \sqrt{\frac{r^3}{GM}}$$

### Energy of an Orbiting Satellite



❖ Kinetic Energy ( $K$ ):

$$K = \frac{1}{2}mv_o^2 = \frac{1}{2}m\left(\frac{GM}{r}\right) = \frac{GMm}{2r}$$

**Potential Energy ( $U$ ):**

$$U = -\frac{GMm}{r}$$

**Total Energy ( $E$ ):**

$$❖ E = K + U = \frac{GMm}{2r} - \frac{GMm}{r} = -\frac{GMm}{2r}$$

Note:  $K = -E$  and  $U = 2E$

**Binding Energy**

❖ The energy required to remove the satellite from the orbit to infinity

$$E_{binding} = -E = \frac{GMm}{2r}$$

**Escape Velocity ( $v_e$ )**

The minimum velocity required for a body to escape the gravitational field of a planet of mass  $M$  and radius  $R$ .

$$(\text{Total Energy} = 0: \frac{1}{2}mv_e^2 - \frac{GMm}{R} = 0)$$

$$v_e = \sqrt{\frac{2GM}{R}}$$

❖ In terms of  $g$ :  $GM = gR^2$

$$v_e = \sqrt{2gR}$$

❖ For Earth:  $v_e \approx 11.2 \text{ km/s}$

❖ Relation between  $v_e$  and  $v_o$  (near the surface):

$$v_e = \sqrt{2}v_o$$

**Kepler's Laws of Planetary Motion**



#### A. Law of Orbits (First Law)

- ❖ All planets move in elliptical orbits with the Sun at one of the foci.

#### B. Law of Areas (Second Law)

- ❖ The line joining the planet and the Sun sweeps equal areas in equal intervals of time.
- ❖ This is a consequence of the conservation of angular momentum ( $L = \text{constant}$ ).

$$\frac{dA}{dt} = \frac{L}{2m} = \text{Constant}$$

#### Law of Periods (Third Law)

The square of the time period ( $T$ ) of revolution of a planet around the Sun is directly proportional to the cube of the semi-major axis ( $a$ ) of its elliptical orbit.

$$\frac{T^2}{a^3} = \frac{4\pi^2}{GM} = \text{Constant}$$

- ❖ For circular orbits, the semi-major axis  $a$  is replaced by the radius  $r$ .



### Fundamental Definitions

Deformation is quantified using Stress (internal restoring force per unit area) and Strain (fractional change in dimension).

- ❖ Stress ( $\sigma$ ):  $\sigma = \frac{F}{A}$
- ❖ Longitudinal Strain ( $\epsilon$ ):  $\epsilon = \frac{\Delta L}{L}$
- ❖ Volumetric Strain:  $\frac{\Delta V}{V}$
- ❖ Shearing Strain ( $\theta$ )  $\theta = \frac{\Delta x}{L} \approx$  angle of twist (in radius)

### Hooke's Law & Moduli of Elasticity

Within the elastic limit, Stress is directly proportional to Strain: Stress =  $E \times$  Strain

| Type of Modulus                 | Formula   | Description  |
|---------------------------------|---|--|
| Young's Modulus ( $Y$ )         | $Y = \frac{F / A}{\Delta L / L} = \frac{FL}{F\Delta L}$ | For solids (wires/rods) under tension/compression. |
| Bulk Modulus ( $B$ or $K$ )     | $B = -\frac{P}{\Delta V / V}$                           | For volume changes; $P$ is hydraulic pressure.     |
| Shear Modulus ( $G$ or $\eta$ ) | $G = \frac{F_{Tangential} / A}{\theta}$                 | Also called Modulus of Rigidity.                   |
| Compressibility ( $k$ )         | $k = \frac{1}{B}$                                       | Reciprocal of Bulk Modulus.                        |

### Energy in Deformed Solids

When a wire is stretched, work is done against interatomic forces and stored as Elastic Potential Energy.

### Work Done / Total Energy ( $U$ ):

- ❖  $U = \frac{1}{2} \times \text{Load} \times \text{Extension} = \frac{1}{2} F \Delta L$

### Energy Density ( $u$ ): (Energy per unit volume)



$$\text{❖ } u = \frac{1}{2} \times \text{Stress} \times \text{Strain} = \frac{1}{2} Y \epsilon^2$$

### Poisson's Ratio (sigma $\sigma$ or $\nu$ )

The ratio of lateral strain (change in diameter) to longitudinal strain (change in length)

$$\text{❖ } \sigma = \frac{\text{Lateral Strain}}{\text{Longitudinal Strain}} = -\frac{\Delta d / d}{\Delta L / L}$$

Theoretical Range :  $-1 < \sigma < 0.5$

Practical Range:  $0 \leq \sigma < 0.5$

### Important Inter-relations

These are high-yield for JEE Main and NEET numericals

$$\text{❖ } Y = 3B(1 - 2\sigma)$$

$$\text{❖ } Y = 2B(1 + \sigma)$$

$$\text{❖ } \sigma = \frac{3B - 2G}{6B + 2G}$$

$$\text{❖ } \frac{9}{Y} = \frac{3}{G} + \frac{1}{B}$$

### Meaning of Symbols

- ❖  $F$ : Applied Force (or Restoring Force)
- ❖  $A$ : Cross-sectional Area ( $\pi r^2$  for a wire)
- ❖  $L, \Delta L$ : Original length and change in length
- ❖  $V, \Delta V$ : Original volume and change in volume
- ❖  $P$ : Pressure (Hydraulic Stress)
- ❖  $Y, B, G$ : Young's, Bulk, and Shear Moduli
- ❖  $\sigma$ : Poisson's Ratio (sometimes denoted by  $\nu$  or  $\mu$ )



## Mechanical Properties of Fluids

### Pressure

#### Formula

$$P = \frac{F}{A}$$

$$P = P_o + pgh \text{ (Hydrostatic Pressure)}$$

#### Symbols

P : Pressure

#### Formula

$$P_1 = P_2$$

$$\text{Hydraulic lift : } \frac{F_1}{A_1} = \frac{F_2}{A_2}$$

#### Symbols

$F_1, F_2$  : Forces

$A_1, A_2$  : Area of pistons

### Buoyancy – Archimedes' Principle

#### Formula

$$F_B = \rho g V$$

$$\text{Apparent weight} = W - F_B$$

#### Symbols

$F_B$  : Buoyant force

$V$  : Volume of fluid displaced

$W$  : Actual weight

### Continuity Equation

#### Formula

$$A_1 v_1 = A_2 v_2 = \text{Constant}$$

$$\rho_1 A_1 v_1 = \rho_2 A_2 v_2 \text{ (Compressible)}$$

#### Symbols

$A_1, A_2$  : Cross-sectional areas

$F$  : Force

$A$  : Area

$P_o$  : Atmospheric pressure

$\rho$  : Density of fluid

$g$  : Acceleration due to gravity

$h$  : Height/depth

### Pascal's Law

$v_1, v_2$  : Fluid velocities

### Bernoulli's Equation

#### Formula

$$P + \frac{1}{2} \rho v^2 + \rho g h = \text{Constant}$$

#### Symbols

$P$  : Pressure

$\rho$  : Density

$v$  : Speed of fluid

$h$  : Height

### Torricelli's Theorem

#### Formula

$$v = \sqrt{2gh}$$

#### Symbols

$v$  : Speed of efflux

$h$  : Height of fluid column

### Viscosity

#### Newton's Law of Viscous Force

$$F = \eta A \frac{dv}{dy}$$

#### Symbols

$F$  : Viscous force

$\eta$  : Coefficient of viscosity

$A$  : Area



$\frac{dv}{dy}$  : Velocity gradient

### Poiseuille's Law (Laminar flow in tube)

$$Q = \frac{\pi r^4 (P_1 - P_2)}{8\eta L}$$

#### Symbol

$Q$  : Volume flow rate

$r$  : Radius of tube

$P_1 - P_2$  : Pressure difference

$L$  : Length of tube

### Terminal Velocity

#### Formula

For sphere falling in viscous fluid:

$$v_t = \frac{2r^2 (\rho_s - \rho_f) g}{9\eta}$$

#### Symbols

$v_t$  : Terminal velocity

$r$  : Radius

$\rho_s$  : Density of sphere

$\rho_f$  : Density of fluid

### Surface Tension

#### Formula

$$T = \frac{F}{2L} \text{ (Liquid Film)}$$

Pressure inside a soap bubble:  $\Delta P = \frac{4T}{r}$

Pressure inside a liquid drop:  $\Delta P = \frac{2T}{r}$

#### Symbols

$T$  : Surface tension

$L$  : Length

$\Delta P$  : Excess pressure

$r$  : Radius

### Capillarity

#### Formula

$$h = \frac{2T \cos \theta}{\rho g r}$$

#### Symbols

$h$  : Height rise/fall

$\theta$  : Contact angle

### Pressure at Depth & Density Relation

$$\Delta P = \rho g \Delta h$$

Average density:  $\rho = \frac{m}{V}$

### Fluid Force on Walls

Horizontal plate:  $F = PA$

Vertical plate:  $F = \rho g Ah_{cm}$



## Thermal properties of matter

### Temperature Scales and Thermal Expansion

These formulas describe how substances change physical dimensions when heated.

| Concept           | Formula  | Symbols  |
|-------------------|--|--|
| Scale Conversion  | $\frac{C}{5} = \frac{F - 32}{9} = \frac{K - 273.15}{5}$                          | $C$ : Celsius, $F$ : Fahrenheit, $K$ : Kelvin                  |
| Linear Expansion  | $\Delta L = L_o \alpha \Delta T$   | $\alpha$ : Coeff. of linear expansion, $L_o$ : Original length |
| Area Expansion    | $\Delta A = A_o \beta \Delta T$  | $\beta$ : Coeff. of area expansion ( $\beta = 2\alpha$ )       |
| Volume Expansion  | $\Delta V = V_o \gamma \Delta T$   | $\gamma$ : Coeff. of volume expansion ( $\gamma = 3\alpha$ )   |
| Density Variation | $\rho = \frac{\rho_o}{1 + \gamma \Delta T} \approx \rho_o (1 - \gamma \Delta T)$ | $\rho$ : New density, $\rho_o$ : Initial density               |

### Calorimetry

Calorimetry deals with the measurement of heat transfer during state changes or temperature shifts.

- ❖ **Specific Heat Capacity (s or c):** The heat required to raise the temperature of unit mass by 1°C.  
 $Q = ms\Delta T$
- ❖ **Latent Heat (L):** The heat required to change the phase of a substance without changing its temperature.  
 $Q = mL$
- ❖ Latent Heat of Fusion ( $L_f$ ): For Ice  $\approx 80$  cal/g
- ❖ Latent Heat of Vaporization ( $L_v$ ): For Water  $\approx 540$  cal/g
- ❖ Water Equivalent ( $W$ ):  $W = ms$  (expressed in grams of water).

### Heat Transfer: Conduction

Conduction is the transfer of heat through solids via molecular vibrations.

#### Thermal Current (H): Rate of flow of heat

$$H = \frac{dQ}{dt} = \frac{KA(T_1 - T_2)}{L}$$

- ❖  $K$ : Thermal conductivity of the material.
- ❖  $A$ : Cross-sectional area.
- ❖  $L$ : Length of the conductor.

**Thermal Resistance ( $R_{th}$ ):** Analogous to electrical resistance.



$$R_{th} = \frac{L}{KA}$$

**Series Combination:**  $R_{eq} = R_1 + R_2$

**Parallel Combination:**  $\frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2}$

### Radiation and Newton's Law of Cooling

Radiation involves heat transfer through electromagnetic waves and does not require a medium.

**Stefan-Boltzmann Law:** The energy radiated per unit area per unit time ( $E$ )

$$E = \sigma eAT^4$$

- ❖  $\sigma$ : Stefan's constant ( $5.67 \times 10^{-8} \text{ Wm}^{-2} \text{ K}^{-4}$ ).
- ❖  $e$ : Emissivity ( $0 \leq e \leq 1$ )
- ❖  $T$ : Absolute temperature in Kelvin

**Wien's Displacement Law:** Relates the temperature of a blackbody to the peak wavelength of emission.

$$\lambda_m T = b$$

$b$ : Wien's constant ( $\approx 2.89 \times 10^{-3} \text{ mK}$ )

**Newton's Law of Cooling:** The rate of loss of heat is proportional to the temperature difference between the body and surroundings

$$\frac{dT}{dt} = -k(T - T_s)$$

- ❖ **Average Form (for numerical)**  $\frac{T_1 - T_2}{t} = K \left( \frac{T_1 + T_2}{2} - T_s \right)$

### Kinetic Theory of Gases (Short Reference)

Ideal Gas Equation:  $PV = nRT$

**Root Mean Square Velocity:**  $v_{rms} = \sqrt{\frac{3RT}{M}} = \sqrt{\frac{3kT}{m}}$  f

- ❖  $k$ : Boltzmann constant.
- $m$ : Mass of a single molecule.



## Thermodynamics

### Important Terminology

**Internal Energy ( $U$ ):** For an ideal gas, it depends only on temperature.

$$\Delta u = nC_v\Delta T$$

### Work Done by Gas ( $W$ ):

- ❖  $W = \int PdV$
- ❖  $W > 0$  if the gas expands ( $V$  increases).
- ❖  $W < 0$  if the gas is compressed ( $V$  decreases).

### Molar Specific Heat:

- ❖ At constant volume:  $C_v = \frac{f}{2}R$
- ❖ At constant pressure:  $C_p = C_v + R = \left(\frac{f}{2} + 1\right)R$
- ❖ Mayer's Formula:  $C_p - C_v = R$
- ❖ Ratio of Specific Heats ( $\gamma$ ):  $\gamma = \frac{C_p}{C_v} = 1 + \frac{2}{f}$  (Note:  $f$  is the degrees of the freedom: 3 for monoatomic, 5 for diatomic)

### Laws of Thermodynamics

First Law of Thermodynamics (FLOT)

Based on the conservation of energy:  $\Delta Q = \Delta U + W$

- ❖  $\Delta Q$ : Heat supplied to the system.
- ❖  $\Delta U$ : Change in internal energy.
- ❖  $W$ : Work done by the system.

### Second Law of Thermodynamics

Kelvin-Planck Statement: No engine can convert all heat into work (Efficiency  $\eta < 1$ ).

Clausius Statement: Heat cannot flow spontaneously from a cold body to a hot body.



| Process    | Condition      | Work Done (W)                         | First Law Form                |
|------------|----------------|---------------------------------------|-------------------------------|
| Isochoric  | V = Constant   | 0                                     | $\Delta Q = \Delta U$         |
| Isobaric   | P = Const      | 0                                     | $\Delta Q = nC_p\Delta T$     |
| Isothermal | T = Const      | $nRT \ln\left(\frac{V_2}{V_1}\right)$ | $\Delta Q = W (\Delta U = 0)$ |
| Adiabatic  | $\Delta Q = 0$ | $\frac{P_1V_1 - P_2V_2}{\gamma - 1}$  | $w = \Delta U$                |

## Heat Engines and Refrigerators

### Carnot Engine

An ideal reversible engine operating between a hot reservoir ( $T_1$ ) and a cold reservoir ( $T_2$ ).

- ❖ Efficiency ( $\eta$ ):

$$\eta = 1 - \frac{Q_1}{Q_2} = 1 - \frac{T_2}{T_1}$$

(Temperatures must be in Kelvin)

### Refrigerator / Heat Pump

Coefficient of Performance ( $\beta$  or  $\alpha$ )

- ❖  $Q_2$ : Heat extracted from the cold reservoir.
- ❖  $W$ : Work input required.

### Symbols Glossary

- ❖  $P, V, T$ : Pressure, Volume, and Absolute Temperature.
- ❖  $n$ : Number of moles.
- ❖  $R$ : Universal Gas Constant ( $\approx 8.314$  J/mol. K).
- ❖  $f$ : Degrees of freedom.
- ❖  $\gamma$ : Adiabatic exponent.
- ❖  $Q_1$ : Heat absorbed from the source.
- ❖  $Q_2$ : Heat rejected to the sink.



## Kinetic theory of Gases

### Ideal Gas Laws & Pressure

The core of KTG lies in the relationship between molecular motion and the pressure exerted on a container.

❖ Ideal Gas Equation:  $PV = nRT = Nk_B T$

❖ Pressure of an Ideal Gas:  $P = \frac{1}{3} \rho v_{rms}^2 = \frac{1}{3} \frac{mN}{V} v_{rms}^2$

❖ Kinetic Interpretation of Temperature: The average translational kinetic energy is directly proportional to the absolute temperature

$$E_{avg} = \frac{3}{2} k_B T$$

### Molecular Speeds

Molecules in a gas move at various speeds. We use three specific "statistical" speeds for calculations:

| Speed Type                     | Formula  | Relation       |
|--------------------------------|--|----------------|
| Root Mean Square ( $v_{rms}$ ) | $\sqrt{\frac{3RT}{M}} = \sqrt{\frac{3k_B T}{m}}$         | Largest Speed  |
| Average Speed ( $v_{avg}$ )    | $\sqrt{\frac{8RT}{\pi M}} = \sqrt{\frac{8k_B T}{\pi m}}$ | Middle Speed   |
| Most Probable ( $v_{mp}$ )     | $\sqrt{\frac{2RT}{M}} = \sqrt{\frac{2k_B T}{m}}$         | Smallest Speed |

**Memory Trick:**  $v_{rms} > v_{avg} > v_{mp}$  (Remember **RAM**: RMS > Average > Most Probable).

### Degrees of Freedom (f) and Equipartition

The Law of Equipartition states that energy is shared equally among all degrees of freedom ( $1/2 k_B T$ ) per degree of freedom).

| Gas Atomicity           | Degrees of Freedom (f) | $C_v$   | $C_p$   | $\gamma = C_p / C_v$ |
|-------------------------|------------------------|---------|---------|----------------------|
| Monoatomic (He, Ar)     | 3                      | $3/2 R$ | $5/2 R$ | 1.67                 |
| Diatomic ( $O_2, N_2$ ) | 5                      | $5/2 R$ | $7/2 R$ | 1.40                 |
| Polyatomic (Non-linear) | 6                      | $3 R$   | $4 R$   | 1.33                 |



- ❖ Internal Energy ( $U$ ):  $U = \frac{1}{2}nRT$
- ❖ Relationship between  $\gamma$  and  $f$ :  $\gamma = 1 + \frac{2}{f}$

### Mean Free Path & Collision

The average distance a molecule travels between two successive collisions.

- ❖ Mean Free Path ( $\lambda$ ):

$$\lambda = \frac{1}{\sqrt{2}\pi d^2 n}$$

- ❖  $d$ : Diameter of the molecule.
- ❖  $n$ : Number of molecules per unit volume ( $N/V$ ).
- ❖ Collision Frequency: Number of collisions per second

### Symbols Glossary

- ❖  $P$ : Pressure ( $Pa$ )
- ❖  $V$ : Volume ( $m^3$ )
- ❖  $T$ : Absolute Temperature (Kelvin)
- ❖  $n$ : Number of moles
- ❖  $N$ : Total number of molecules
- ❖  $m$ : Mass of one molecule
- ❖  $M$ : Molar mass of the gas
- ❖  $R$ : Universal Gas Constant ( $\approx 8.314 \text{ J/mol} \cdot K$ )
- ❖  $K_B$ : Boltzmann Constant ( $R/N_A \approx 1.38 \times 10^{-23} \text{ J/K}$ )
- ❖  $p$ : Density of the gas ( $mN/V$ )

## Oscillations

### Basics of SHM

The fundamental condition for a motion to be SHM is that the acceleration ( $a$ ) must be proportional to displacement ( $x$ ) and directed toward the mean position.

- ❖ **Restoring Force:**  $F = -kx$
- ❖ **Standard Differential Equation:**  $\frac{d^2x}{dt^2} + \omega^2x = 0$
- ❖ **Angular Frequency ( $\omega$ ):**  $\omega = \sqrt{\frac{k}{m}}$

### Kinematics of SHM

These formulas define the position, speed, and acceleration of a particle at any time  $t$ .

| Quantity            | Formula  | Remarks   |
|---------------------|--|---|
| <b>Displacement</b> | $x = A \sin(\omega t + \phi)$                      | $A$ : Amplitude, $\phi$ : Initial phase             |
| <b>Velocity</b>     | $v = \omega \sqrt{A^2 - x^2}$                      | Max at mean ( $x = 0$ ): $v_{\max} = A\omega$       |
| <b>Acceleration</b> | $a = -\omega^2x$                                   | Max at extremes ( $x = A$ ): $a_{\max} = \omega^2A$ |
| <b>Time Period</b>  | $T = \frac{2\pi}{\omega} = 2\pi\sqrt{\frac{m}{k}}$ | Time for one complete cycle                         |
| <b>Frequency</b>    | $f = \frac{1}{T} = \frac{\omega}{2\pi}$            | Measured in Hertz ( $Hz$ )                          |

### Energy in SHM

In an ideal SHM, energy oscillates between kinetic and potential forms, but the total mechanical energy remains constant.

- ❖ **Kinetic Energy ( $K$ ):**  $K = \frac{1}{2}m\omega^2(A^2 - x^2) = \frac{1}{2}k(A^2 - x^2)$
- ❖ **Potential Energy ( $U$ ):**  $U = \frac{1}{2}kx^2 = \frac{1}{2}m\omega^2x^2$
- ❖ **Total Energy ( $E$ ):**  $E = K + U = \frac{1}{2}kA^2 = \frac{1}{2}m\omega^2A^2$

Note:  $E$  is independent of both time ( $t$ ) and displacement ( $x$ ).

### Common Oscillating Systems

- ❖ Series Combination:  $\frac{1}{k_{eq}} = \frac{1}{k_1} + \frac{1}{k_2}$
- ❖ Parallel Combination:  $k_{eq} = k_1 + k_2$
- ❖ Cut Spring: If a spring is cut into  $n$  equal pieces, each piece has a spring constant  $nk$ .

### Pendulums:

- ❖ Spring-Mass System  $T = 2\pi\sqrt{\frac{L}{g}}$  (L: length, g: gravity)
- ❖ Physical (Compound) Pendulum:  $T = 2\pi\sqrt{\frac{I}{mgd}}$
- ❖  $I$ : Moment of inertia about the hinge.
- ❖  $d$ : Distance from hinge to Center of Mass
- ❖ Torsional Pendulum:  $T = 2\pi\sqrt{\frac{I}{C}}$  (C : Torsional Constants)

### Damped and Forced Oscillations (JEE Specific)

- ❖ Damped SHM Displacement:  $x(t) = Ae^{-bt/2m} \cos(\omega't + \phi)$
- ❖  $b$ : Damping constant
- ❖  $\omega' = \sqrt{\frac{k}{m} - \frac{b^2}{4m^2}}$
- ❖ Resonance: Occurs when the driving frequency matches the natural frequency ( $\omega_\alpha = \omega_o$ ), leading to maximum amplitude.

### Symbols Glossary

- $A$  : Amplitude (maximum displacement from mean).
- $\omega$  : Angular frequency ( $rad/s$ ).
- $\phi$  : Phase constant (initial state of motion).
- $k$  : Spring constant or force constant ( $N/m$ ).
- $T$  : Time period ( $s$ ).
- $x$  : Instantaneous displacement ( $m$ ).
- $m$  : Mass of the oscillating body ( $kg$ )



## Waves

### Basic Definitions

**Wavelength ( $\lambda$ ):** Distance between two consecutive crests/troughs.

**Time Period ( $T$ ):** Time taken for one oscillation.

**Frequency ( $f$ ):** Number of oscillations per second  $\rightarrow f = \frac{1}{T}$

### Wave Speed

General Formula:  $v = \lambda f$

**Speed of Wave on Stretched String:**  $v = \sqrt{\frac{T_s}{\mu}}$

where  $T_s$  = tension in string, and  $\mu$  = linear mass density.

**Speed of Sound in Gas:**  $v = \sqrt{\gamma \frac{P}{\rho}}$

**Alternate form using temperature (in  $^{\circ}\text{C}$ ):**  $v \approx 331 + 0.6T$

### Wave Equation

Standard form of a progressive harmonic wave:

**Travelling in +x direction:**  $y(x, t) = A \sin(kx - \omega t + \phi)$

**Travelling in -x direction:**  $y(x, t) = A \sin(kx + \omega t + \phi)$

**Where:**

$$k = \frac{2\pi}{\lambda}, \omega = 2\pi f$$

### Superposition & Interference

**Resultant amplitude (for coherent waves):**  $A = \sqrt{A_1^2 + A_2^2 + 2A_1 A_2 \cos \phi}$

**Intensity formula:**  $I \propto A^2$

### Beats

**Beat frequency:**  $f_{beats} = |f_1 - f_2|$

### Standing Waves

**General condition:**  $L = n \frac{\lambda}{2}$



(for a string fixed at both ends or air column closed at both ends)

**For closed organ pipe (one end closed):**  $L = (2n - 1) \frac{\lambda}{4}$

**For open organ pipe (both ends open):**  $L = n \frac{\lambda}{2}$

### Harmonic Frequencies:

#### System

#### Frequency

Open Organ Pipe

$$f_n = n \frac{v}{2L}$$

Closed Organ Pipe

$$f_n = (2n - 1) \frac{v}{4L}$$

Stretched String

$$f_n = n \frac{v}{2L}$$

### Doppler Effect

General Formula:  $f_n = f \left( \frac{v \pm v_o}{v \pm v_s} \right)$

#### Signs:

Observer moving toward source → use + in numerator

Source moving toward observer → use - in denominator

(Sound waves only; medium speed = v)

### Energy in Waves

**Intensity of progressive wave:**  $I = \frac{1}{2} \mu A^2 \omega^2 v$

## Symbols and Meanings

### Symbol

$A$

$\lambda$

$f$

$T$

$v$

$k$

$\omega$

$\phi$

$\mu$

$T_s$

$\gamma$

$\rho$

$P$

$V_o$

$V_s$

$I$

$n$

### Meaning

Amplitude

Wavelength

Frequency

Time period

Wave speed

Wave number =  $2\pi/\lambda$

Angular frequency =  $2\pi f$

Phase constant

Linear mass density (kg/m)

Tension in string

Ratio of specific heats

Density of medium

Pressure of gas

Velocity of observer

Velocity of source

Intensity of wave

Harmonic number (1,2,3...)

