

ULTIMATE KCET



CRASH COURSE 2026

Mathematics

One Shot

LPP

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Question



Corner points of the feasible region determined by the system of linear constraints are $(0,3)$, $(1,1)$ and $(3,0)$. Let $z = px + qy$, where $p, q > 0$. Condition on p and q so that the minimum of z occurs at $(3,0)$ and $(1,1)$ is [2020]

A $p = \frac{q}{2}$

B $p = 3q$

C $p = q$

D $p = 2q$

$(3,0)$ $\underline{z_{\min}} = 3p + 0 = 3p$

$(1,1)$ $\underline{z_{\min}} = p + q$

$$3p = p + q$$

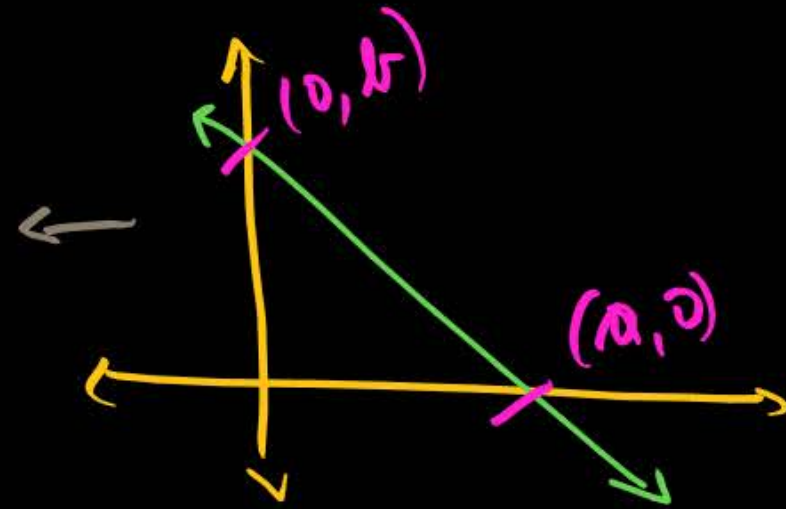
$$2p = q$$

$$p = \frac{q}{2}$$

Intercept form of straight line



$$\frac{x}{a} + \frac{y}{b} = 1$$



Given Inequation



convert into eqⁿ



Find intercepts

$(a, 0)$ & $(0, b)$

$$2x + 3y \leq 24$$

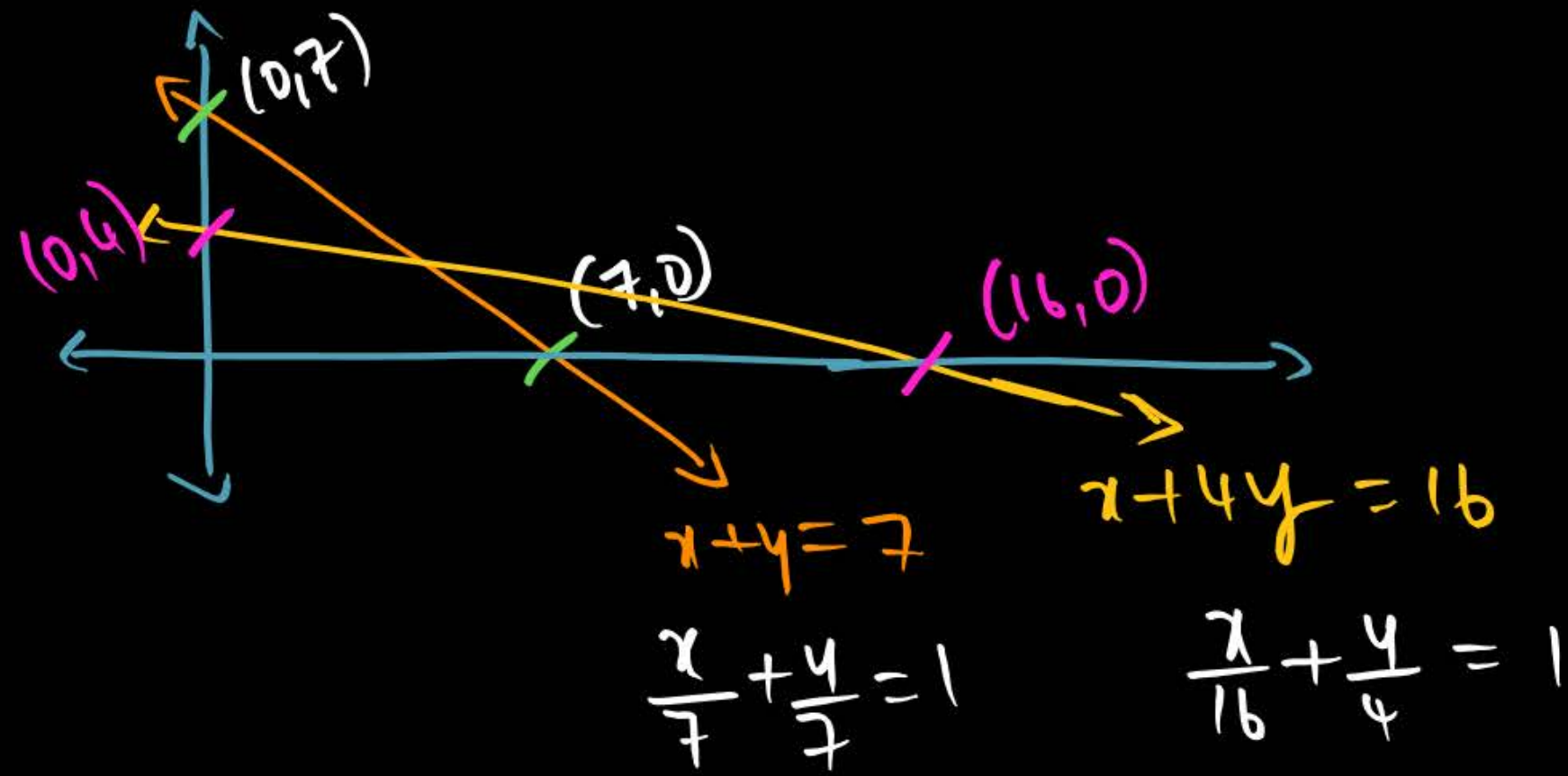


$$2x + 3y = 24$$

\div by 24

$$\frac{x}{12} + \frac{y}{8} = 1$$

$(12, 0)$ & $(0, 8)$



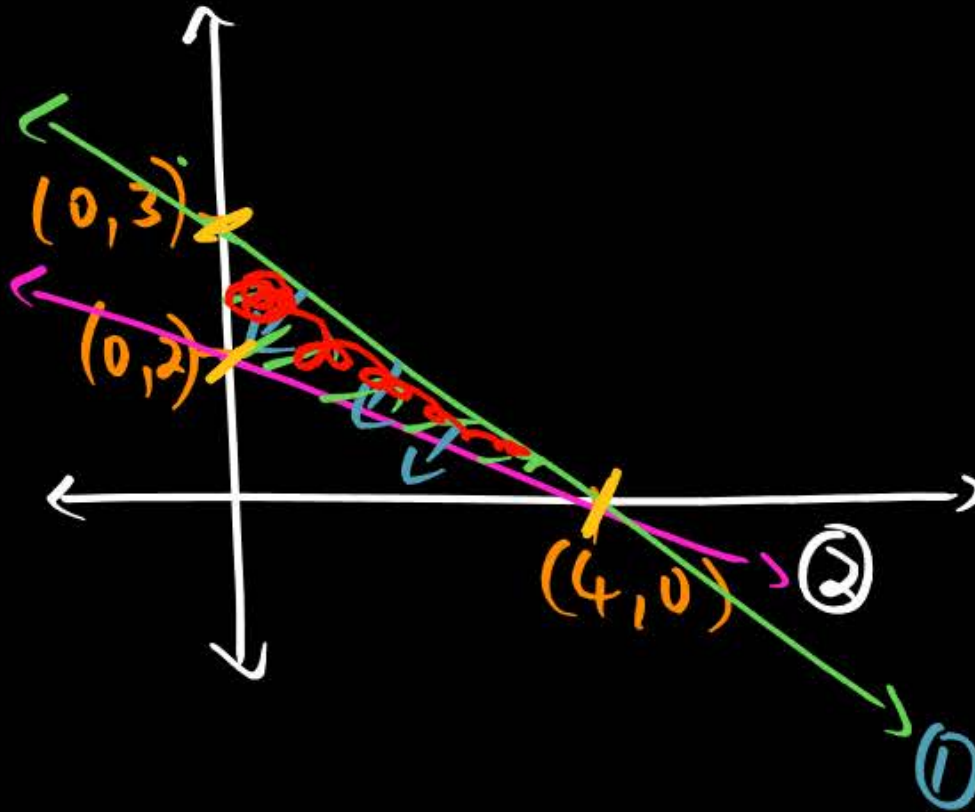
$$3x + 4y \leq 12$$

⇓

$$\frac{x}{4} + \frac{y}{3} \leq 1 \rightarrow \textcircled{1}$$

$$4x + 8y \geq 16$$

$$\frac{x}{4} + \frac{y}{2} \geq 1 \rightarrow \textcircled{2}$$

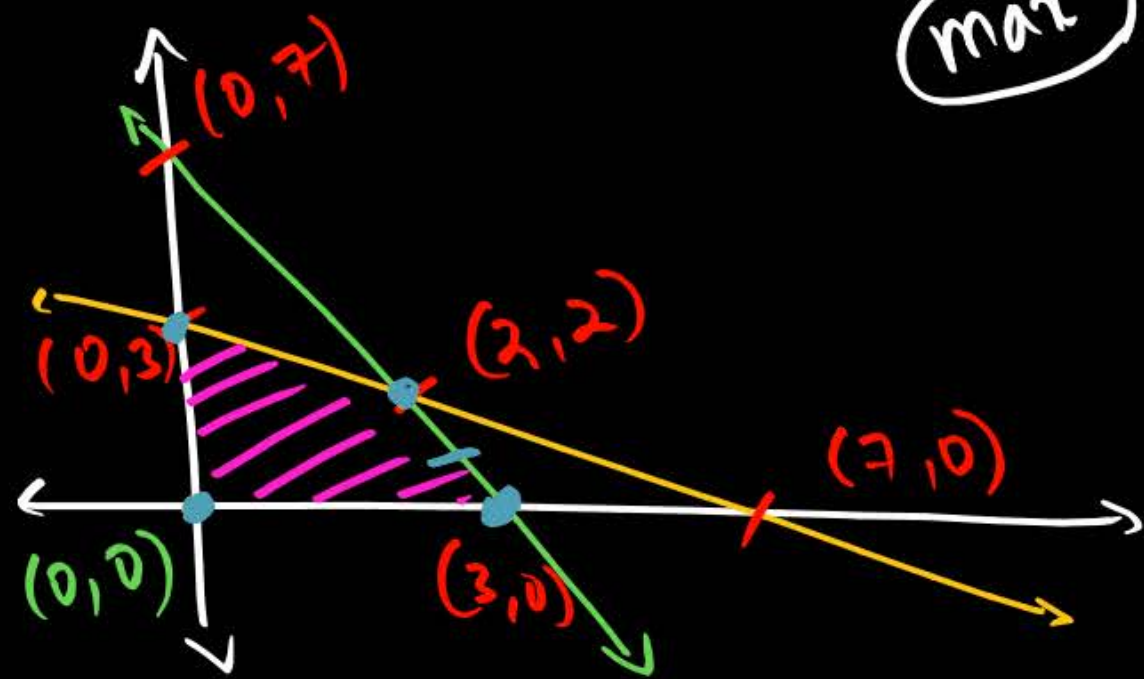


Corner Points

(0, 3)

(0, 2)

(4, 0)



Corner Points	$Z = ax + by$
$(0, 3)$	7
$(2, 2)$	10 \rightarrow
$(3, 0)$	10 \rightarrow
$(0, 0)$	0

} max

The max value of Z

occurs at $(2, 2)$ & $(3, 0)$

& also at all the points on the line segment

joining the point $(2, 2)$ & $(3, 0)$

\Downarrow
 Here there are infinitely many solutions

Question



Corner points of the feasible region for an LPP are $(0,2)$, $(3,0)$, $(6,0)$, $(6,8)$ and $(0,5)$. Let $z = 4x + 6y$ be the objective function. The minimum value of z occurs at

A ~~✗~~ Only $(0,2)$

B ~~✗~~ Only $(3,0)$

C ~~✗~~ The mid-point of the line segment joining the points $(0,2)$ and $(3,0)$

D ✓ Any point on the line segment joining the points $(0,2)$ and $(3,0)$

	$z = 4x + 6y$
$(0,2)$	12
$(3,0)$	12
$(6,0)$	24
$(6,8)$	$24 + 48 = 72$
$(0,5)$	30

Question



The corner points of the feasible region of an LPP are $(0,2)$, $(3,0)$, $(6,0)$, $(6,8)$ and $(0,5)$, then the **minimum** value of $z = 4x + 6y$ occurs at

A ~~finite number of points~~

B ~~only one point~~

C infinite number of points

D ~~only two points~~

	$z = 4x + 6y$
$(0, 2)$	12
$(3, 0)$	12
$(6, 0)$	24
$(6, 8)$	72
$(0, 5)$	30

Handwritten note: A bracket groups the values 12 and 12, with an arrow pointing to the word "min".

Question



Consider the following statements:

$z = ax + by$

Power of x & y is one

Statement (I): In a LPP, the objective function is always **linear**.

Statement (II): In a LPP, the linear inequalities on variables are called **constraints**.

Which of the following is correct?

- A** Statement (I) is true, Statement (II) is true
- B** Statement (I) is true, Statement (II) is false
- C** Both Statements (I) and (II) are false
- D** Statement (I) is false, Statement (II) is true

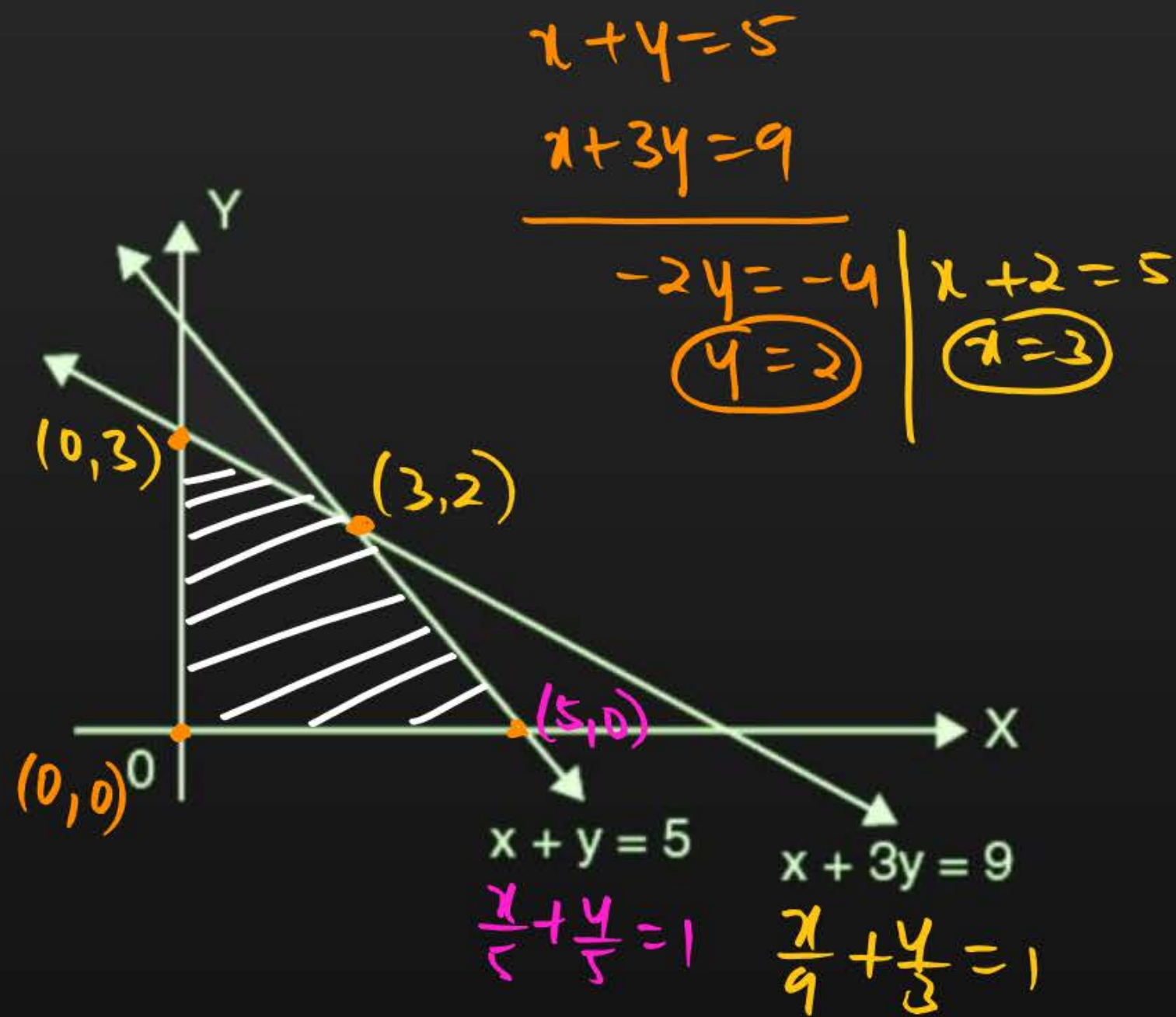
Question



The feasible region of an LPP is shown in the figure. If $Z = 11x + 7y$, then the maximum value of Z occurs at

- A** (3, 2)
- B** (0, 5)
- C** (3, 3)
- D** (5, 0)

	$11x + 7y$
(0, 3)	21
(3, 2)	$33 + 14 = 57$
(0, 0)	0
(5, 0)	55



Question

The shaded region is the solution set of the inequalities.

$$\begin{aligned} 5x + 4y &\geq 20 \\ x &\leq 6 \\ y &\leq 3 \end{aligned}$$

1st Qnd

$$x \geq 0$$

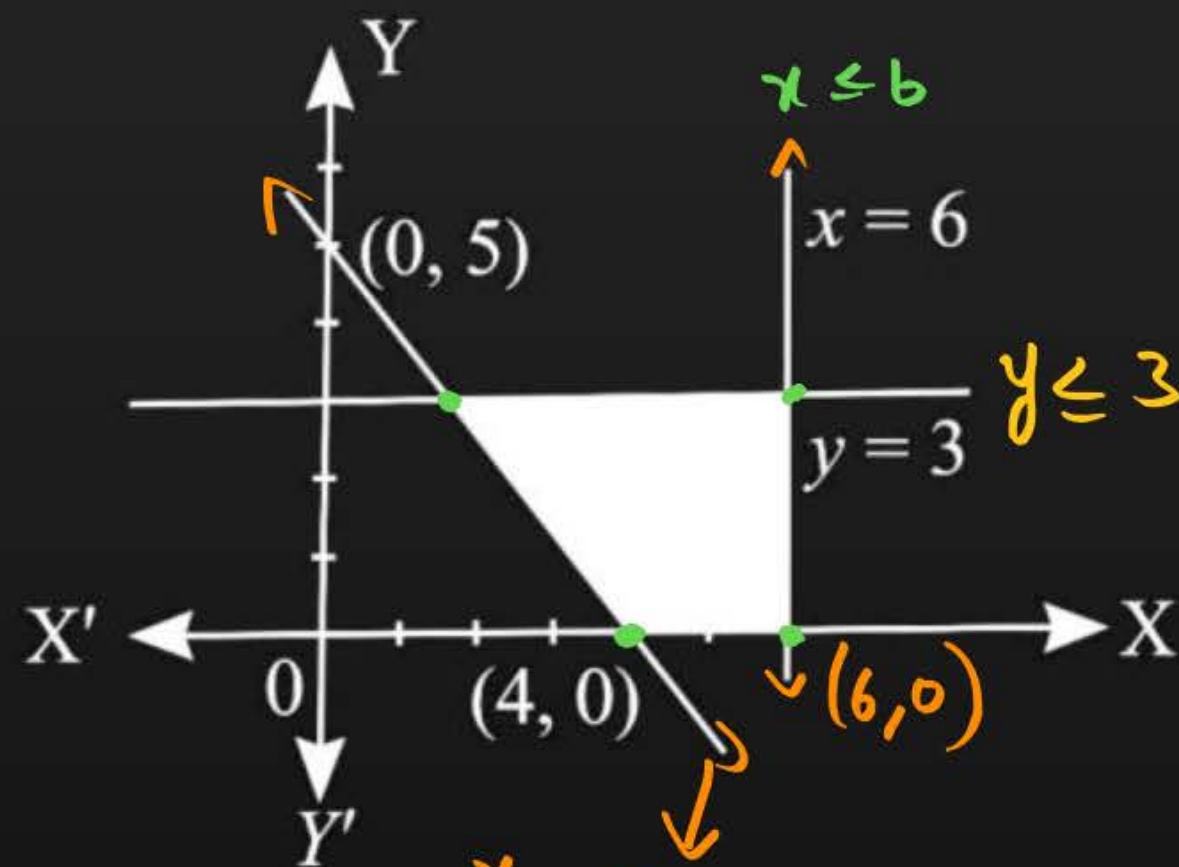
$$y \geq 0 \quad [2021]$$

A $5x + 4y \geq 20, x \leq 6, y \geq 3, x \geq 0, y \geq 0$

B $5x + 4y \leq 20, x \leq 6, y \leq 3, x \geq 0, y \geq 0$

C $5x + 4y \geq 20, x \leq 6, y \leq 3, x \geq 0, y \geq 0$

D $5x + 4y \geq 20, x \geq 6, y \leq 3, x \geq 0, y \geq 0$



$$\begin{aligned} \frac{x}{4} + \frac{y}{5} &= 1 \\ 5x + 4y &= 20 \end{aligned}$$

Question



$$2x - 3y = -6$$

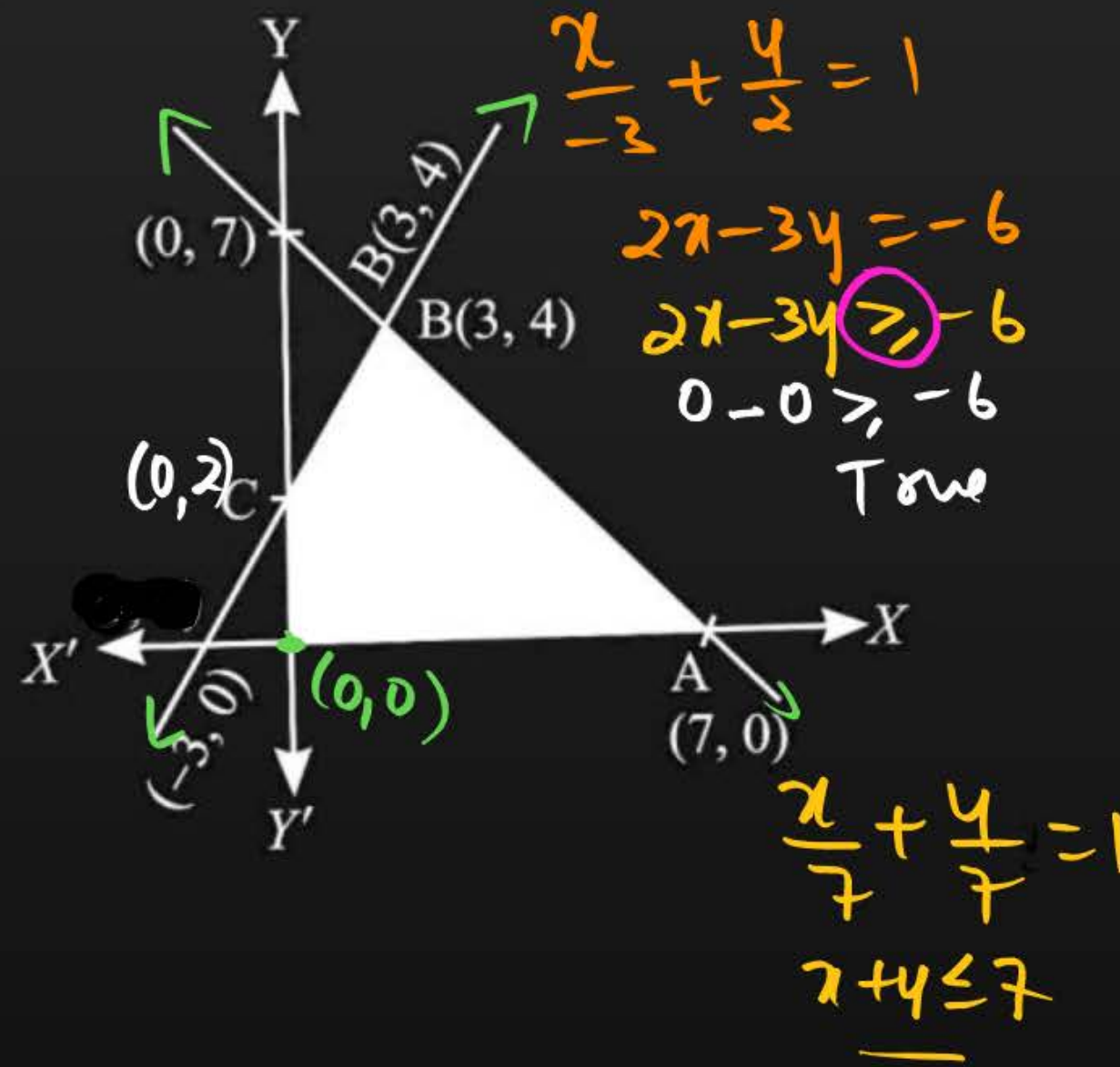
$$0 \geq -6$$

The shaded region in the figure given is the solution of which of the inequations?

- A** $x + y \geq 7, 2x - 3y + 6 \geq 0, x \geq 0, y \geq 0$
- B** $x + y \leq 7, 2x - 3y + 6 \geq 0, x \geq 0, y \geq 0$
- C** $x + y \leq 7, 2x - 3y + 6 \leq 0, x \geq 0, y \geq 0$
- D** $x + y \geq 7, 2x - 3y + 6 \leq 0, x \geq 0, y \geq 0$

$$2x - 3y \geq -6$$

$$x + y \leq 7$$



- ① Intercept form
- ② Feasible region
- ③ Point of Intersection of 2 lines
- ④ Corner Points

Question



Minimize $z = 18x + 10y$ subject to $4x + y \geq 20, 2x + 3y \geq 30, x, y \geq 0$ [2020]

→ conditions $\textcircled{1}$
constraint

$$\frac{x}{5} + \frac{y}{20} = 1 \quad \left| \quad \frac{x}{15} + \frac{y}{10} = 1$$

$$4x + y = 20$$

$$4x + 6y = 60$$

$$-5y = -40$$

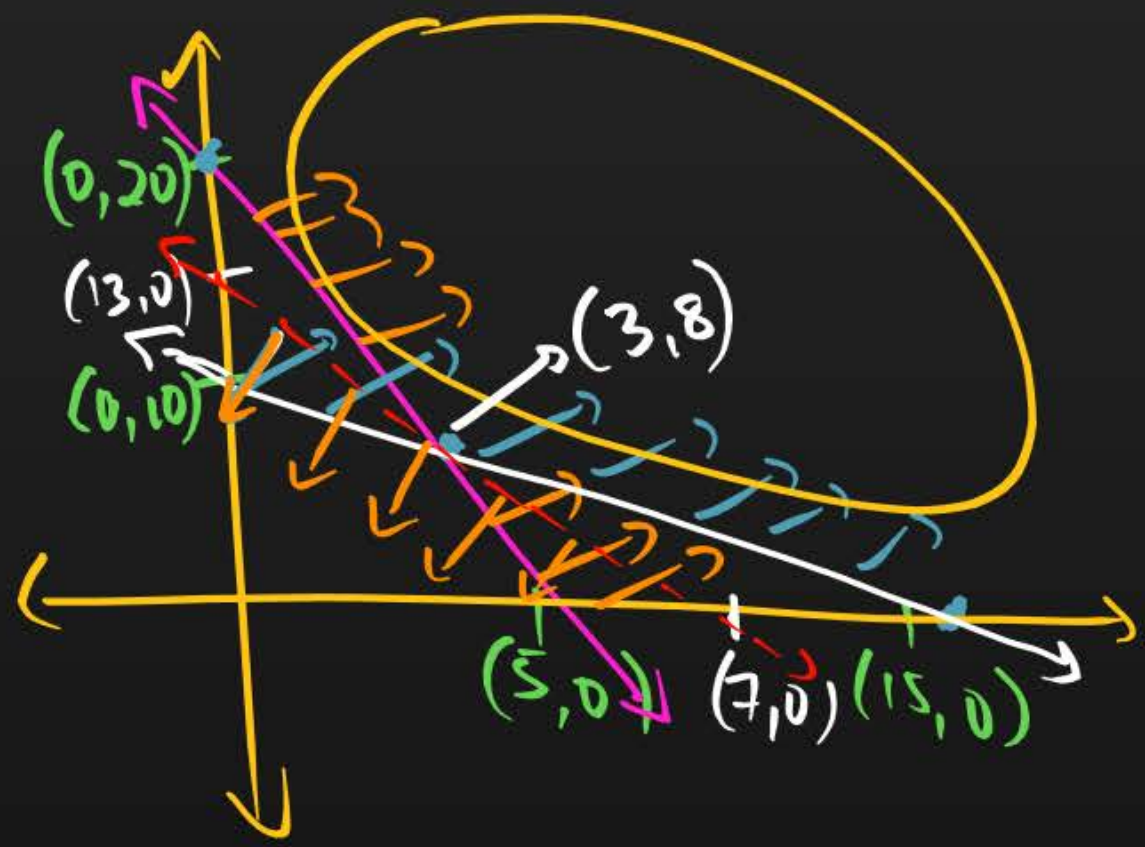
$$y = 8$$

⇓

$$4x + 8 = 20$$

$$4x = 12$$

$$x = 3$$

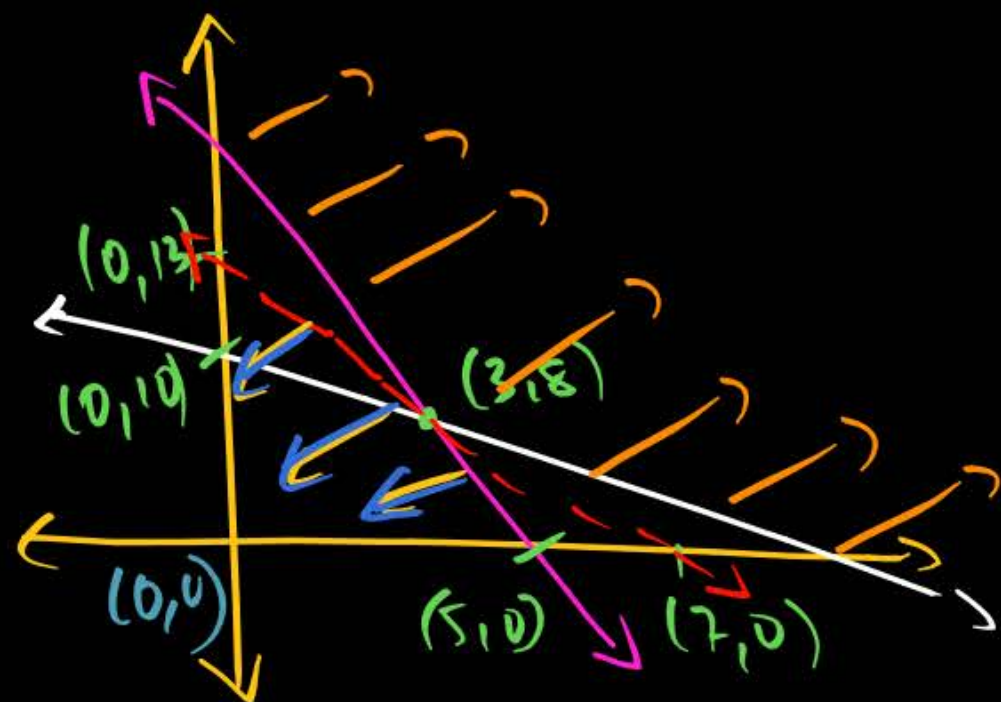


A 431

B 143

C 314

D 134



$$z = 18x + 10y$$

At $(3,8)$ we got $z = 134$

$$\Downarrow$$

$$18x + 10y \leq 134$$

min

$$\frac{x}{7} + \frac{y}{13} = 1$$

Approximately

Put $x=0, y=0$

$$0 < 134$$

True

	$18x + 10y$
$(3, 8)$	$54 + 80 = 134 \rightarrow \text{min}$
$(0, 20)$	200
$(15, 0)$	270

$$18x + 10y < 134$$
$$\frac{x}{7 \dots} + \frac{y}{13 \dots} = 1$$

$(0, 0) \Rightarrow 0 < 134$
True



Question



The **minimum** value of $z = 3x + 5y$ subject to $x + y \leq 3$, $-x + y \leq 1$, $x, y \geq 0$ is [2021]

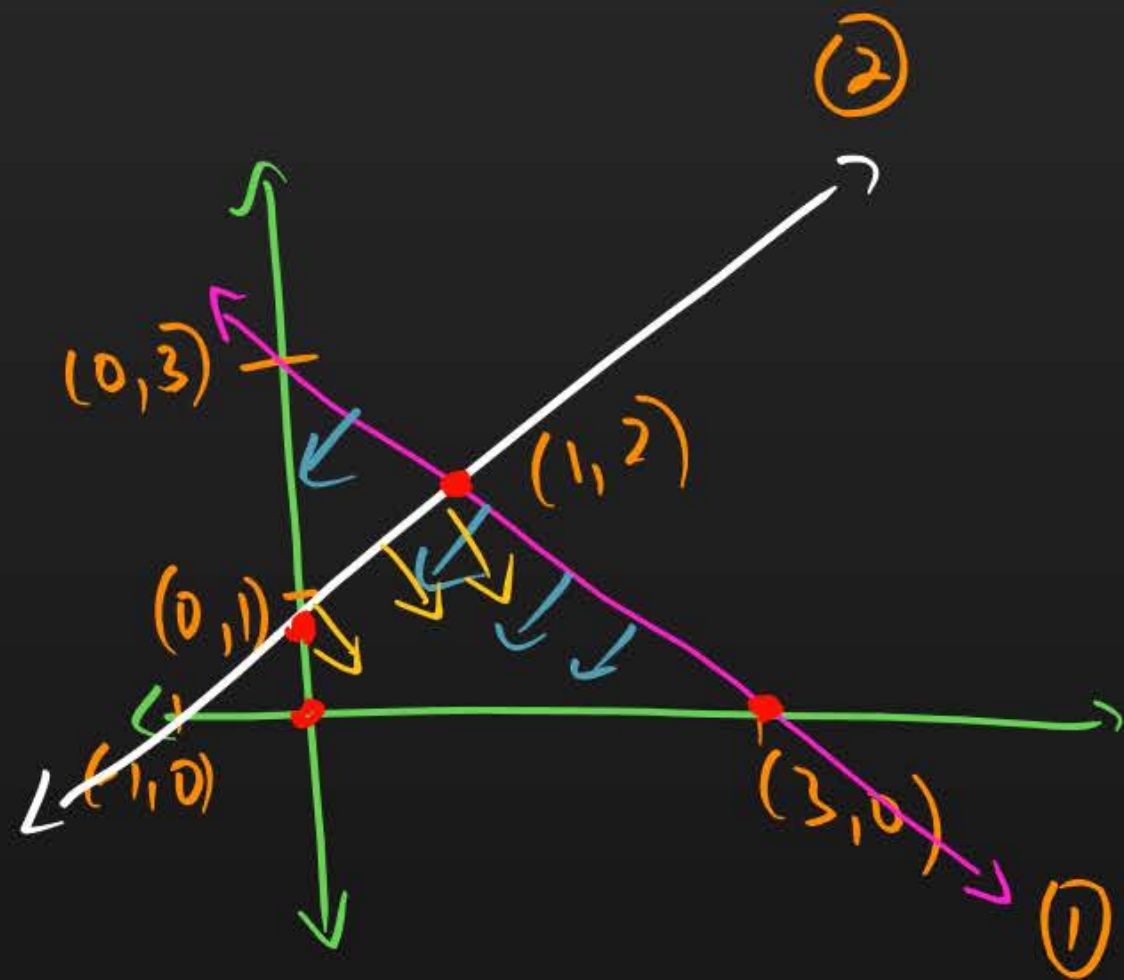
$$\begin{array}{r|l} x+y=3 & y=2 \\ -x+y=1 & x=1 \\ \hline 2y=4 & \end{array}$$

① $\frac{x}{3} + \frac{y}{3} \leq 1$ $\rightarrow 0+0 \leq 3$

② $\frac{x}{-1} + \frac{y}{1} \leq 1$ $\rightarrow 0+0 \leq 1$

\rightarrow 1st Quad

- A** 9
- B** 11
- C** 0
- D** 15



	$z = 3x + 5y$
(0,0)	0 \rightarrow min
(0,1)	5
(3,0)	9
(1,2)	$3+10=13 \rightarrow$ max

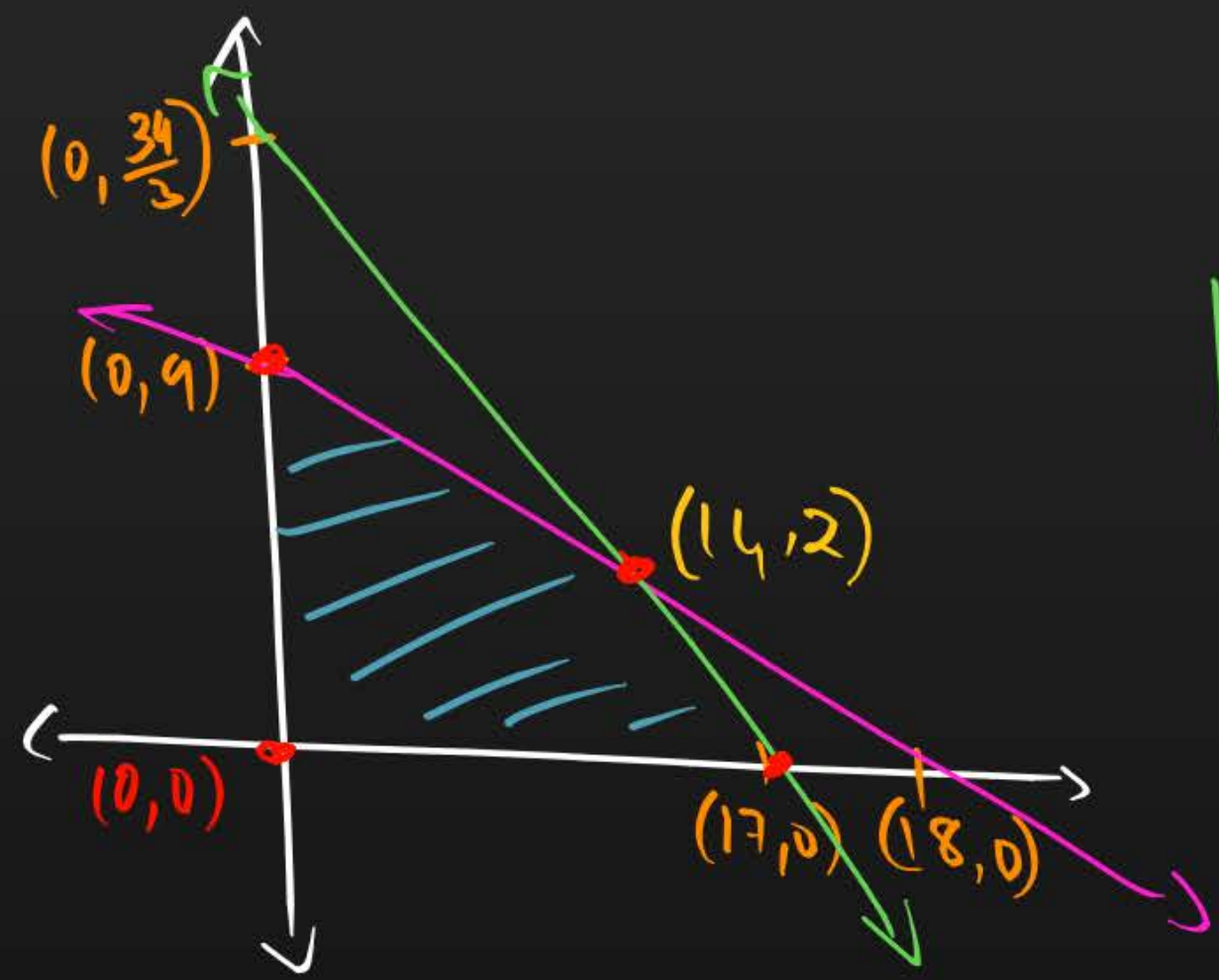
Question



$$\begin{array}{r} 2x + 4y = 36 \\ 2x + 3y = 34 \\ \hline y = 2 \end{array} \quad \begin{array}{l} x + y = 18 \\ x = 14 \end{array}$$

The maximum value of $z = 30x + 50y$ subject to $x + 2y \leq 18, 2x + 3y \leq 34, x, y \geq 0$ is [2021]

- A** 450
- B** 510
- C** 520
- D** 560



$$\frac{x}{18} + \frac{y}{9} = 1 \quad \left| \quad \frac{x}{17} + \frac{y}{11} = 1 \right.$$

	$z = 30x + 50y$
$(0, 0)$	0
$(17, 0)$	510
$(14, 2)$	$420 + 100 = 520$
$(0, 9)$	<u>450</u>

Question



The maximum value of $z = 3x + 4y$, subject to the constraints $x + y \leq 40$, $x + 2y \leq 60$ and $x, y \geq 0$ is

- A** 130
- B** 120
- C** 140
- D** 40

Question



Minimize $z = 18x + 10y$ subject to $4x + y \geq 20, 2x + 3y \geq 30, x, y \geq 0$

[2020]

A 431

B 143

C 314

D 134

Question

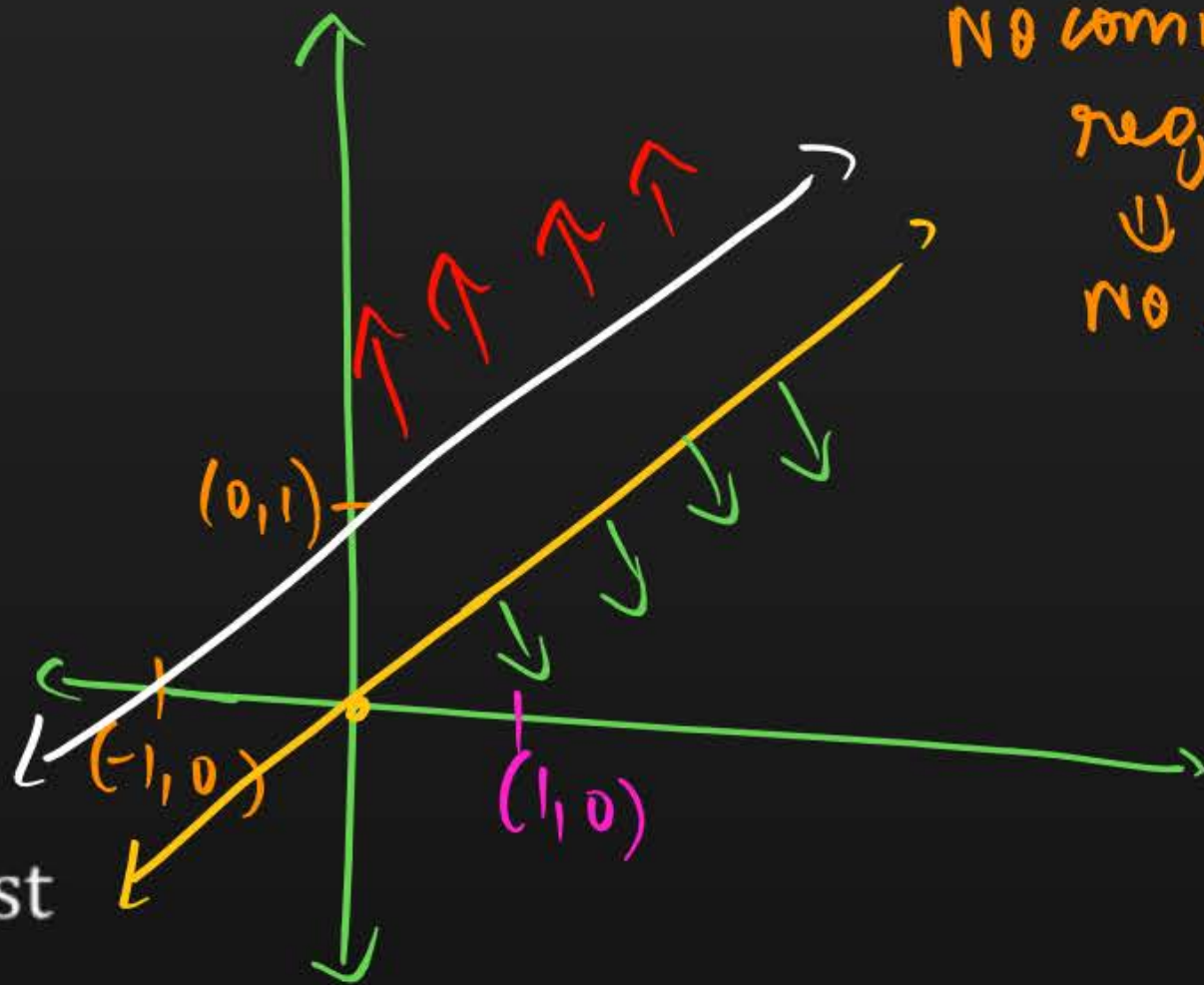
$$z = 3x + 4y \quad \left| \quad \begin{array}{l} x - y = -1 \\ \frac{x}{-1} + \frac{y}{1} = 0 \end{array} \right| \quad \begin{array}{l} -x + y = 0 \\ x = y \Rightarrow (0,0) \end{array}$$

$Ax + By + C = 0$
Slope = $m = -\frac{A}{B}$



Maximize $z = 3x_1 + 4x_2$, if possible, Subject to the constraints
 $x_1 - x_2 \leq -1, -x_1 + x_2 \leq 0; x_1, x_2 \geq 0$.

- A** 105
- B** 100
- C** 156
- D** Does not exist



No common region
 \Downarrow
no solution

[2019]
 $x - y + 1 = 0 \quad \left| \quad \begin{array}{l} -x + y = 0 \\ m_1 = \frac{-1}{-1} = 1 \\ m_2 = -\frac{(-1)}{1} = 1 \end{array} \right.$

$m_1 = m_2$

Put $(x, y) = (1, 0)$

$$\begin{array}{l} x_1 - x_2 \leq -1 \\ 0 - 0 \leq -1 \\ 0 \leq -1 \\ \text{False} \end{array}$$

$$\begin{array}{l} -x + x_2 \leq 0 \\ -1 + 0 \leq 0 \\ -1 \leq 0 \\ \text{True} \end{array}$$

Question

$$z = 7x_1 - 3x_2$$

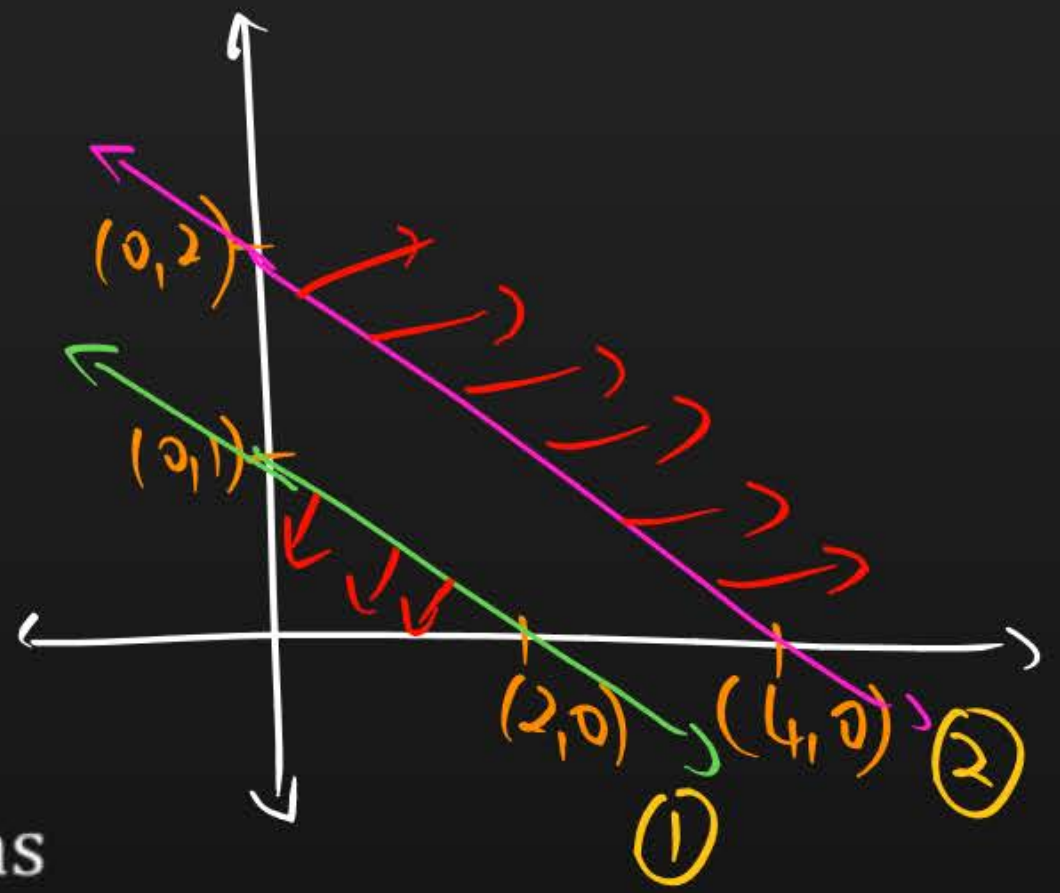
$$\begin{aligned} \textcircled{1} \quad & x_1 + 2x_2 \leq 2 \\ & 2x_1 + 4x_2 \geq 8 \end{aligned} \quad \textcircled{2}$$

Maximize $z = 7x_1 - 3x_2$. Subject to, $x_1 + 2x_2 \leq 2, 2x_1 + 4x_2 \geq 8, x_1 \geq 0, x_2 \geq 0$.

$$\begin{aligned} \frac{x_1}{2} + \frac{x_2}{1} &= 1 & \left| & \right. & \frac{x_1}{4} + \frac{x_2}{2} &= 1 \end{aligned}$$

[2019]

- A** Unique solution
- B** Unbounded solution
- C** Infeasible solution
- D** Infinite number of solutions



Question

Maximize $z = -x + 2y$ subject to the constraints

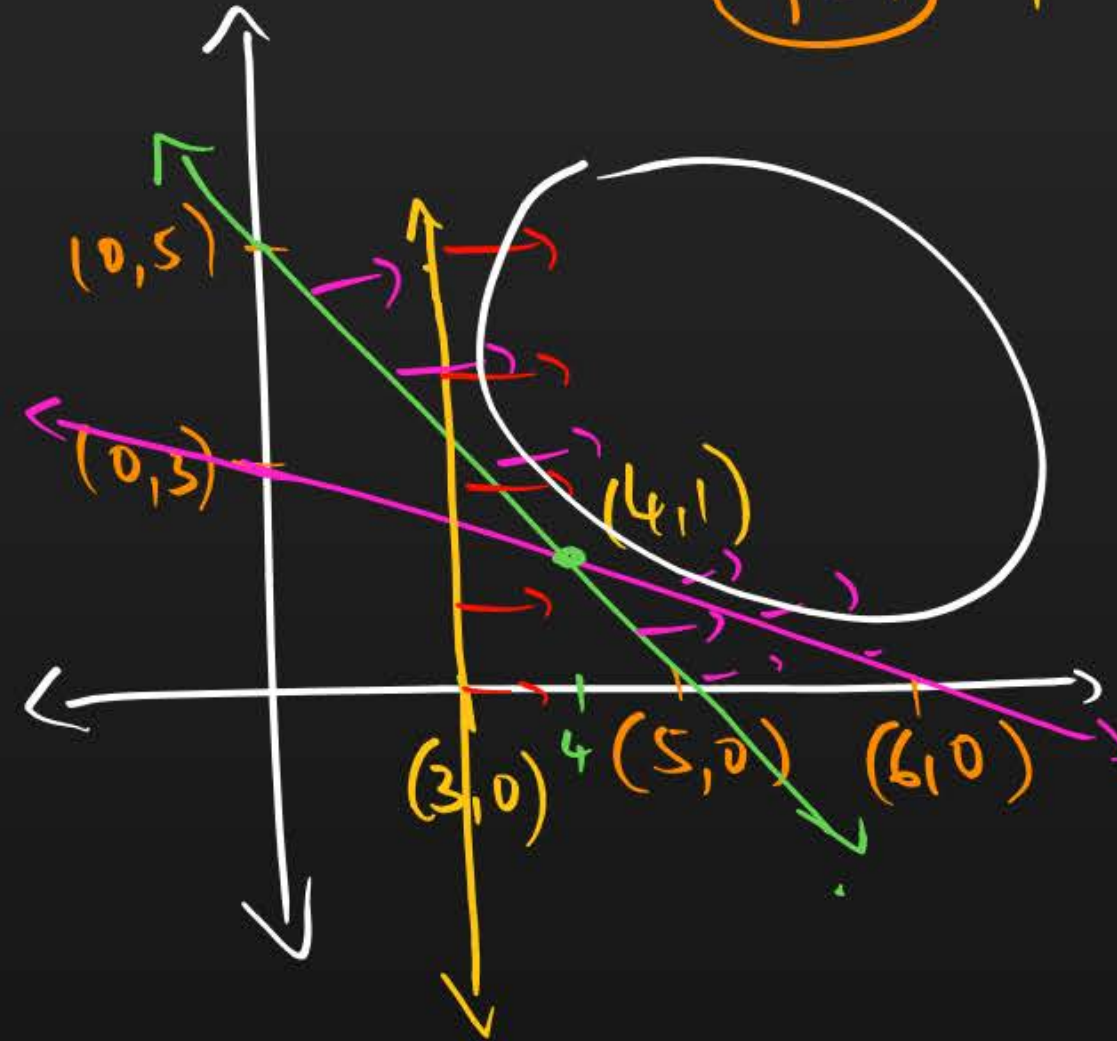
$$x \geq 3, x + y \geq 5, x + 2y \geq 6, y \geq 0$$

$$\frac{x}{5} + \frac{y}{5} = 1 \quad \left| \quad \frac{x}{6} + \frac{y}{3} = 1$$

$$\begin{array}{r} x + y = 5 \\ x + 2y = 6 \\ \hline -y = -1 \\ y = 1 \end{array}$$

$$\begin{array}{r} x + y = 5 \\ x = 4 \end{array}$$

- A** Unique solution
- B** Infinite number of optimal solutions
- C** Infeasible solution
- D** Unbounded solution



Question



Maximize $z = 3x_1 + 4x_2$, if possible, Subject to the constraints
 $x_1 - x_2 \leq -1$, $-x_1 + x_2 \leq 0$; $x_1, x_2 \geq 0$.

- A** 105
- B** 100
- C** 156
- D** Does not exist

Question



$Z = 6x_1 + 2x_2$, subject to $5x_1 + 9x_2 \leq 90$, $x_1 + x_2 \geq 4$, $x_2 \leq 8$, $x_1 \geq 0$, $x_2 \geq 0$. The minimum value of Z occurs at [2023]

- A** (18, 0)
- B** (3.6, 8)
- C** (0, 4)
- D** (4, 0)

Question



The maximum value of $z = 3x + 5y$ subject to $x + 2y \leq 20, x + y \leq 15, y \leq 5, x, y \geq 0$ is [2021]

A 25

B 45

C 55

D 65

Question



The objective function $Z = 4x + 3y$ can be minimum subjected to the constraints $3x + 4y \leq 24, 8x + 6y \leq 48, x \leq 5, y \leq 6; x, y \geq 0$ [2024]

- A** at only one point
- B** at two points only
- C** at an infinite number of points
- D** none of these

Thank

You