

Ultimate KCET Crash Course 2026

MATHEMATICS

DPP: 2

Matrices and Determinants

Q1 If the matrix $\begin{bmatrix} 1 & 3 & \lambda + 2 \\ 2 & 4 & 8 \\ 3 & 5 & 10 \end{bmatrix}$ is

 singular, then λ is

- (A) -2 (B) 4
(C) 2 (D) -4

Q2 Find x , if $\begin{bmatrix} 1 & 2 & x \\ 1 & 1 & 2 \\ 2 & 1 & -2 \end{bmatrix}$ is singular.

- (A) 7 (B) 6
(C) 5 (D) 8

Q3 If $\begin{vmatrix} x & 2 \\ 18 & x \end{vmatrix} = \begin{vmatrix} 6 & 2 \\ 18 & 6 \end{vmatrix}$, then x

- (A) 6 (B) ± 6
(C) -6 (D) 0

Q4 If $A = \begin{bmatrix} \alpha & 3 \\ 3 & \alpha \end{bmatrix}$ and $|A^3| = 216$ then $\alpha =$

- (A) ± 5 (B) $\pm \sqrt{15}$
(C) $\pm \sqrt{17}$ (D) ± 6

Q5 If A is a square matrix of order $n \times n$, then $\text{adj}(\text{adj} A)$ is equal to:

- (A) $|A|^n A$ (B) $|A|^{n-1} A$
(C) $|A|^{n-2} A$ (D) $|A|^{n-3} A$

Q6 If $\Delta = \begin{vmatrix} 1 & 2 & 3 \\ 2 & 0 & 1 \\ 5 & 3 & 8 \end{vmatrix}$, write the cofactor of

 element a_{22}

- (A) 7 (B) -7
(C) -8 (D) 8

Q7

If $\det(A) = \begin{vmatrix} \sin \theta & 1 \\ 0 & \cos \theta \end{vmatrix} = -\frac{1}{4}$ where

 $\theta \in [\pi, \frac{3\pi}{2}]$, Then $\theta =$

- (A) $\frac{\pi}{12}$ (B) $\frac{5\pi}{6}$
(C) $\frac{7\pi}{6}$ (D) $\frac{7\pi}{12}$

Q8 If $\begin{pmatrix} a & b \\ c & d \end{pmatrix}$ is the inverse of the matrix

$$\begin{pmatrix} 1 & 5 \\ 7 & -3 \end{pmatrix}, \text{ then } d \text{ equals.}$$

- (A) -1/38 (B) -7/38
(C) 3/38 (D) 5/38

Q9 If $A = \begin{vmatrix} -1 & 2 & 4 \\ 3 & 1 & 0 \\ -2 & 4 & 2 \end{vmatrix}$ and

$$B = \begin{vmatrix} -2 & 4 & 2 \\ 6 & 2 & 0 \\ -2 & 4 & 8 \end{vmatrix} \text{ then } B \text{ is given by}$$

- (A) $B = 4A$ (B) $B = -4A$
(C) $B = -A$ (D) $B = 6A$

Q10 If the determinant

$$\Delta = \begin{vmatrix} 3 & -2 & \sin 3\theta \\ -7 & 8 & \cos 2\theta \\ -11 & 14 & 2 \end{vmatrix} = 0 \text{ then } \sin \theta =$$

- (A) 0, 1/2 (B) 0, 3/2
(C) 1/2, 1 (D) $\frac{1}{\sqrt{2}}, \frac{1}{2}$

Q11

If the matrices $A = \begin{bmatrix} 1 & 1 & 2 \\ 1 & 3 & 4 \\ 1 & -1 & 3 \end{bmatrix}$, $B = \text{adj}$

 A and $C = 3A$, then $\frac{|\text{adj } B|}{|C|}$ is equal to

- (A) 16 (B) 2



(C) 8 (D) 72

Q12 There are two values of a which makes

$$\text{determinant, } \Delta = \begin{vmatrix} 1 & -2 & 5 \\ 2 & a & -1 \\ 0 & 4 & 2a \end{vmatrix} = 86, \text{ then}$$

sum of these numbers is

(A) 4 (B) 5
(C) -4 (D) 9**Q13** If A is a matrix of order 3, and $|A| = 8$, then $|\text{adj } A|$ is(A) 8 (B) 8^2
(C) 8^3 (D) $\frac{1}{8}$ **Q14** The constant term of the polynomial

$$\begin{vmatrix} x^2 + 4 & 2x + 2 & 4 \\ -4x + 3 & 3x + 1 & -6x + 1 \\ 7x + 2 & x^2 - 3 & x + 1 \end{vmatrix} \text{ is}$$

(A) 0 (B) -30
(C) 60 (D) -10**Q15** If A is a matrix of order 4×4 & $|A| = 3$, then $|6A|^{-1} =$ (A) $1/6480$ (B) $1/80$
(C) 6480 (D) $1/3888$ **Q16** The matrix having multiplicative inverse is(A) $\begin{bmatrix} 4 & 12 \\ 3 & 9 \end{bmatrix}$ (B) $\begin{bmatrix} 1 & 0 \\ 1 & 1 \end{bmatrix}$
(C) $\begin{bmatrix} 3 & 2 \\ 6 & 4 \end{bmatrix}$ (D) $\begin{bmatrix} 1 & 1 \\ 1 & 1 \end{bmatrix}$ **Q17** If $B = \begin{bmatrix} 1 & 3 \\ 1 & \alpha \end{bmatrix}$ be the adjoint of a matrix A and $|A| = 2$, then the value of α is(A) 3 (B) 4
(C) 5 (D) 2**Q18** If area of a triangle is 35 sq. units with vertices (2, -6), (5, 4) and (k, 4). Then k is

(A) 12 (B) -2

(C) -12, -2 (D) 12, -2

Q19 If $A = \begin{vmatrix} -1 & 2 & 4 \\ 3 & 1 & 0 \\ -2 & 4 & 2 \end{vmatrix}$ and

$$B = \begin{vmatrix} -2 & 4 & 2 \\ 6 & 2 & 0 \\ -2 & 4 & 8 \end{vmatrix} \text{ then } B \text{ is given by}$$

(A) $B = 4A$ (B) $B = -4A$
(C) $B = -4$ (D) $B = 6A$ **Q20** If $A = \begin{bmatrix} 1 & 3 \\ 4 & 2 \end{bmatrix}$, $B = \begin{bmatrix} 2 & -1 \\ 1 & 2 \end{bmatrix}$, then

$$|ABB'| =$$

(A) 50 (B) -250
(C) 100 (D) 250**Q21** Let $A = \begin{pmatrix} 0 & 2q & r \\ p & q & -r \\ p & -q & r \end{pmatrix}$. If $AA^T = I_3$,then $|p|$ is(A) $\frac{1}{\sqrt{3}}$ (B) $\frac{1}{\sqrt{2}}$
(C) $\frac{1}{\sqrt{5}}$ (D) $\frac{1}{\sqrt{6}}$ **Q22** If $4x + 3y + 6z = 25$, $x + 9y + 7z = 13$, $2x + 9y + z = 1$, then $z =$ (A) 1 (B) 3
(C) -2 (D) 2**Q23** Using determinant, find the equation of line joining the points (1,-1) and (4,1).(A) $2x - 3y - 5 = 0$ (B) $4x - 3y = 0$ (C) $2x - 4y = 5$ (D) $2x + 3y = 5$ **Q24** Find equation of line joining (3,1) and (9, 3) using determinants(A) $x - 3y = 0$ (B) $x - 2y = 0$ (C) $3x - y = 0$ (D) $2x - y = 0$ 

- Q25** If $A = \begin{bmatrix} 0 & 1+2i & i-2 \\ -1-2i & 0 & K \\ 2-i & 7 & 0 \end{bmatrix}$ and A^{-1} does not exist then $K =$ (where $i = \sqrt{-1}$)
- (A) $1+2i$ (B) -7
(C) 7 (D) $1-2i$

- Q26** If $A = \begin{bmatrix} 1 & 3 \\ 2 & 1 \end{bmatrix}$, then the determinant $A^2 - 2A$ is
- (A) 5 (B) 25
(C) -5 (D) -25

- Q27** If $A = \begin{bmatrix} 3 & 1 \\ -1 & 2 \end{bmatrix}$ find A^{-1} .
- (A) $\frac{1}{7} \begin{bmatrix} 2 & -1 \\ 1 & 3 \end{bmatrix}$
(B) $\frac{1}{7} \begin{bmatrix} 3 & 1 \\ -1 & 2 \end{bmatrix}$
(C) $\frac{1}{7} \begin{bmatrix} -2 & 1 \\ -1 & -3 \end{bmatrix}$
(D) $\frac{1}{7} \begin{bmatrix} 2 & 1 \\ 1 & -3 \end{bmatrix}$

- Q28** Using matrices, solve the following system of equations :
- $$3x + 4y + 7z = 4; 2x - y + 3z = -3; x + 2y - 3z = 8$$
- (A) $x = 2, y = -6, z = 3$
(B) $x = 6, y = 3, z = -2$
(C) $x = 1, y = 1, z = 2$
(D) $x = 1, y = 2, z = -1$

- Q29** Find the value of λ if the points $(1,-5), (-4,5), (\lambda,7)$ are collinear.
- (A) -4 (B) -5
(C) -10 (D) 15

Q30

The constant term of the polynomial

$$\begin{vmatrix} x+3 & x & x+2 \\ x & x+1 & x-1 \\ x+2 & 2x & 3x+1 \end{vmatrix} \text{ is}$$

(A) 2 (B) 0
(C) 1 (D) -1



Answer Key

Q1 (B)
Q2 (D)
Q3 (B)
Q4 (B)
Q5 (C)
Q6 (B)
Q7 (D)
Q8 (A)
Q9 (B)
Q10 (A)
Q11 (C)
Q12 (C)
Q13 (B)
Q14 (B)
Q15 (D)

Q16 (B)
Q17 (C)
Q18 (D)
Q19 (B)
Q20 (B)
Q21 (B)
Q22 (D)
Q23 (A)
Q24 (A)
Q25 (B)
Q26 (B)
Q27 (A)
Q28 (D)
Q29 (B)
Q30 (D)



[Android App](#) | [iOS App](#) | [PW Website](#)

Hints & Solutions

Note: scan the QR code to watch video solution

Q1 Text Solution:

$$\begin{aligned}
 |A| &= 0 \\
 \Rightarrow -3[20-24] &= (\lambda+2)[10-12] = 0 \\
 -3(-4) + (\lambda+2)(-2) &= 0 \\
 12 - 2\lambda - 4 &= 0 \\
 2\lambda &= 8 \\
 \lambda &= 4
 \end{aligned}$$

Video Solution:



Q2 Text Solution:

For singular matrix, $|A| = 0$

$$\begin{aligned}
 \therefore \begin{vmatrix} 1 & 2 & x \\ 1 & 1 & 2 \\ 2 & 1 & -2 \end{vmatrix} &= 0 \\
 \Rightarrow 1(-2-2) - 2(-2-4) + x(1-2) & \\
 &= 0 \\
 \Rightarrow -4 + 12 - x &= 0 \quad \therefore x = 8
 \end{aligned}$$

Video Solution:



Q3 Text Solution:

$$\begin{aligned}
 \begin{vmatrix} x & 2 \\ 18 & x \end{vmatrix} &= \begin{vmatrix} 6 & 2 \\ 18 & 6 \end{vmatrix} \\
 \Rightarrow x^2 - 36 &= 36 - 36 \\
 \Rightarrow x^2 &= 36 \\
 \Rightarrow x &= \pm 6
 \end{aligned}$$

Video Solution:



Q4 Text Solution:

$$\text{Given } A = \begin{bmatrix} \alpha & 3 \\ 3 & \alpha \end{bmatrix} \text{ \& } |A^3| = 216$$

$$\begin{aligned}
 \text{Then } |A| &= 6 \\
 \Rightarrow \alpha^2 - 9 &= 6 \\
 \Rightarrow \alpha^2 &= 15 \\
 \alpha &= \pm\sqrt{15}
 \end{aligned}$$

Video Solution:



Q5 Text Solution:

A is $n \times n$ square matrix, then $\text{adj}(\text{adj } A) = |A|^{n-2}A$
(By the property of adjoint of matrix)

Video Solution:



Q6 Text Solution:

$$\text{We have, } \Delta = \begin{vmatrix} 1 & 2 & 3 \\ 2 & 0 & 1 \\ 5 & 3 & 8 \end{vmatrix}$$



[Android App](#) | [iOS App](#) | [PW Website](#)

Cofactor of

$$a_{22} = (-1)^{2+2} \begin{vmatrix} 1 & 3 \\ 5 & 8 \end{vmatrix} = 8 - 15 = -7$$

Video Solution:



Q7 Text Solution:

$$\begin{aligned} \sin \theta \cos \theta &= -\frac{1}{4} \\ \frac{\sin 2\theta}{2} &= -\frac{1}{4} \\ \sin 2\theta &= -\frac{1}{2} \end{aligned}$$

$$\begin{aligned} \text{Since } \theta &\in \left[\pi, \frac{3\pi}{2} \right] \\ \sin 2\theta &= \sin \left[\pi + \frac{\pi}{6} \right] \\ 2\theta &= \frac{7\pi}{6} \\ \theta &= \frac{7\pi}{12} \end{aligned}$$

Video Solution:



Q8 Text Solution:

$$A = \begin{bmatrix} 1 & 5 \\ 7 & -3 \end{bmatrix}$$

$$A^{-1} = \begin{bmatrix} -3 & -5 \\ -7 & 1 \end{bmatrix} \left(\frac{-1}{38} \right)$$

$$A^{-1} = \begin{bmatrix} 3/38 & 5/38 \\ 7/38 & -1/38 \end{bmatrix} = \begin{bmatrix} a & b \\ c & d \end{bmatrix}$$

$$d = \frac{-1}{38}$$

Video Solution:



Q9 Text Solution:

$$\begin{aligned} A &= -1(2 - 0) - 2(6 - 0) + 4(12 + 2) \\ &= -2 - 12 + 56 = 42 \\ B &= -2(16 - 0) - 4(48 - 0) + 2(24 + 4) \\ &= -32 - 192 + 56 = -224 + 56 = -168 \\ \text{Clearly } B &= -4A \end{aligned}$$

Video Solution:



Q10 Text Solution:

Expand wrt 3rd column

$$\text{Given } \begin{vmatrix} 3 & -2 & \sin 3\theta \\ -7 & 8 & \cos 2\theta \\ -11 & 14 & 2 \end{vmatrix} = 0$$

$$\sin 3\theta [-98 + 88] - \cos 2\theta [42 - 22] + 2 [24 - 14] = 0$$

$$-10 \sin 3\theta - 20 \cos 2\theta + 20 = 0$$

$$\sin 3\theta + 2 \cos 2\theta - 2 = 0$$

$$3 \sin \theta - 4 \sin^3 \theta + 2 - 2 \sin^2 \theta - 2 = 0$$

$$4 \sin^3 \theta + 2 \sin^2 \theta - 3 \sin \theta = 0$$

$$\sin \theta [4 \sin^2 \theta + 2 \sin \theta + 3] = 0$$

$$\sin \theta [2 \sin \theta - 1] [2 \sin \theta + 3] = 0$$

$$\Rightarrow \sin \theta = 0; \sin \theta = \frac{1}{2} \text{ is true}$$

$$\text{and } \sin \theta = \frac{-3}{2} \text{ is not possible since } \sin \theta \in [-1, 1]$$

Video Solution:





Q11 Text Solution:

(C)

$$\text{Here, } |A| = \begin{vmatrix} 1 & 1 & 2 \\ 1 & 3 & 4 \\ 1 & -1 & 3 \end{vmatrix}$$

$$= (9 + 4) - 1(3 - 4) + 2(-1 - 3) = 13 + 1 - 8 = 6$$

$$\text{Now, } |\text{dj B}| = |\text{adj}(\text{adj A})| =$$

$$|A|^{(n-1)^2} = |A|^4 = (6)^4$$

$$\text{Again, } |C| = |3A| = 3^3 \times 6$$

$$\therefore \frac{|\text{adjB}|}{|C|} = \frac{6^4}{3^3 \times 6} = 8$$

Video Solution:



Q12 Text Solution:

On solving the determinant we get

$$a = -7 \text{ \& } a = 3$$

Now the required sum of these numbers is -4

Video Solution:



Q13 Text Solution:

By using the property

$$|\text{AdjA}| = |A|^{n-1} \Rightarrow |\text{AdjA}| = 8^2$$

where 'n' is order of the given matrix.

Video Solution:



Q14 Text Solution:

Put $x = 0$

$$\text{We get } \begin{vmatrix} 4 & 2 & 4 \\ +3 & 1 & 1 \\ 2 & -3 & 1 \end{vmatrix} = -30$$

Video Solution:



Q15 Text Solution:

$$|6A|^{-1} = (6^{-1})^4 |A|^{-1} = \frac{1}{6^4} \frac{1}{|A|} = \frac{1}{1296 \times (3)} = 1/3888$$

Video Solution:



Q16 Text Solution:

$$A = \begin{bmatrix} 1 & 0 \\ 1 & 1 \end{bmatrix} \text{ since } |A| \neq 0$$

Video Solution:





Q17 Text Solution:

$$|B| = |\text{adj}A| = |A| = \alpha - 3 = 2 \Rightarrow \alpha = 5$$

Video Solution:



Q18 Text Solution:

By application of determinants

$$\frac{1}{2} \begin{vmatrix} 2 & -6 & 1 \\ 5 & 4 & 1 \\ k & 4 & 1 \end{vmatrix} = 35$$

on solving the above determinant we get
 $k = 12$ & $k = -2$

Video Solution:



Q19 Text Solution:

$$\begin{aligned} A &= -1(2 - 0) - 2(6 - 0) + 4(12 + 2) \\ &= -2 - 12 + 56 = 42 \\ B &= -2(16 - 0) - 4(48 - 0) + 2(24 + 4) \\ &= -32 - 192 + 56 = -224 + 56 = -168 \\ \text{Clearly } B &= -4A \end{aligned}$$

Video Solution:



Q20 Text Solution:

$$\begin{aligned} |ABB'| &= |A| |B| |B'| \\ &= \begin{vmatrix} 1 & 3 \\ 4 & 2 \end{vmatrix} \begin{vmatrix} 2 & -1 \\ 1 & 2 \end{vmatrix} \begin{vmatrix} 2 & 1 \\ -1 & 2 \end{vmatrix} \\ &= (-10)(5)(5) = -250 \end{aligned}$$

Video Solution:



Q21 Text Solution:

$$\begin{aligned} \text{Here, } A &= \begin{pmatrix} 0 & 2q & r \\ p & q & -r \\ p & -q & r \end{pmatrix} \\ \therefore A^T &= \begin{pmatrix} 0 & p & p \\ 2q & q & -q \\ r & -r & r \end{pmatrix} \\ \therefore AA^T &= \begin{pmatrix} 0 & 2q & r \\ p & q & -r \\ p & -q & r \end{pmatrix} \begin{pmatrix} 0 & p & p \\ 2q & q & -q \\ r & -r & r \end{pmatrix} \\ &= \begin{pmatrix} 4q^2 + r^2 & 2q^2 - r^2 & -2q^2 + r^2 \\ 2q^2 - r^2 & p^2 + q^2 + r^2 & p^2 - q^2 - r^2 \\ -2q^2 + r^2 & p^2 - q^2 - r^2 & p^2 + q^2 + r^2 \end{pmatrix} \\ \text{Also, } AA^T &= I_3 \end{aligned}$$



$$\Rightarrow 2q^2 = r^2, p^2 = q^2 + r^2 \text{ and } p^2 + q^2 + r^2 = 1$$

$$\therefore |p| = \frac{1}{\sqrt{2}}$$

Video Solution:



Q22 Text Solution:

The given equation are

$$4x + 3y + 6z = 25$$

$$x + 5y + 7z = 13$$

$$2x + 9y + z = 1$$

The above equations can be written in matrix

form as,

$$\begin{bmatrix} 4 & 3 & 6 \\ 1 & 5 & 7 \\ 2 & 9 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 25 \\ 13 \\ 1 \end{bmatrix}$$

Now,

$$|A| = \begin{vmatrix} 4 & 3 & 6 \\ 1 & 5 & 7 \\ 2 & 9 & 1 \end{vmatrix} = 4(5 - 63) - 3(1 - 14) + 6(9 - 10)$$

$$= 4(-58) - 3(-13) + 6(-1)$$

$$= -232 + 39 - 6 = -199 \neq 0$$

So, A is invertible

\therefore The given system has unique solution,

$$X = A^{-1}B$$

Now, cofactor matrix of A

$$= \begin{bmatrix} -58 & 13 & -1 \\ 51 & -8 & -30 \\ -9 & -22 & 17 \end{bmatrix}$$

$$\therefore \text{adj } A = \begin{bmatrix} -58 & 13 & -1 \\ 51 & -8 & -30 \\ -9 & -22 & 17 \end{bmatrix}^T$$

$$= \begin{bmatrix} -58 & 51 & -9 \\ 13 & -8 & -22 \\ -1 & -30 & 17 \end{bmatrix}$$

$$\text{So, } A^{-1} = \frac{1}{|A|} (\text{adj } A)$$

$$= \frac{-1}{199} \begin{bmatrix} -58 & 51 & -9 \\ 13 & -8 & -22 \\ -1 & -30 & 17 \end{bmatrix}$$

$$\therefore X = A^{-1}B$$

$$= \frac{-1}{199} \begin{bmatrix} -58 & 51 & -9 \\ 13 & -8 & -22 \\ -1 & -30 & 17 \end{bmatrix} \begin{bmatrix} 25 \\ 13 \\ 1 \end{bmatrix}$$

$$= \frac{-1}{199} \begin{bmatrix} -1450 + 663 - 9 \\ 325 - 104 - 22 \\ -25 - 390 + 17 \end{bmatrix}$$

$$= -\frac{1}{199} \begin{bmatrix} -796 \\ -111 \\ -398 \end{bmatrix} = \begin{bmatrix} 4 \\ -1 \\ 2 \end{bmatrix}$$

Or comparing, we get $x = 4, y = -1$ and $z = 2$

Video Solution:



Q23 Text Solution:



[Android App](#) | [iOS App](#) | [PW Website](#)

Equation of line is

$$\begin{vmatrix} x & y & 1 \\ x_1 & y_1 & 1 \\ x_2 & y_2 & 1 \end{vmatrix} = 0$$

$$\begin{vmatrix} x & y & 1 \\ 1 & -1 & 1 \\ 4 & 1 & 1 \end{vmatrix} = 0$$

$$x(-1-1) - y(1-4) + 1(1+4) = 0$$

$$-2x + 3y + 5 = 0$$

$$2x - 3y - 5 = 0$$

Video Solution:



Q24 Text Solution:

Equation of the line is

$$\begin{vmatrix} x & y & 1 \\ x_1 & y_1 & 1 \\ x_2 & y_2 & 1 \end{vmatrix} = 0 \Rightarrow \begin{vmatrix} x & y & 1 \\ 3 & 1 & 1 \\ 9 & 3 & 1 \end{vmatrix} = 0$$

$$\Rightarrow x(1-3) - y(3-9) + 1(9-9) = 0$$

$$\Rightarrow -2x + 6y = 0 \Rightarrow x - 3y = 0$$

Hence, $x - 3y = 0$ is the required line

Video Solution:



Q25 Text Solution:

$$A = \begin{bmatrix} 0 & i+2i & i-2 \\ -1-2i & 0 & K \\ 2-i & 7 & 0 \end{bmatrix}$$

Given that, A^{-1} does not exist.

$$\Rightarrow |A| = 0$$

$$\Rightarrow 0 - (1+2i)(-K(2-i)) + (i-2)(-7-14i) = 0$$

(expanding along A)

$$\Rightarrow (1+2i)(2K-Ki) - 7i+14+14+28i=0$$

$$\Rightarrow 2K - Ki + 4Ki + 2K - 7i + 28 + 28i = 0$$

$$\Rightarrow (28+4K) + (3K+21)i = 0$$

$$\Rightarrow 28+4K=0 \text{ and } 3K+21=0 \Rightarrow K=-7$$

Video Solution:



Q26 Text Solution:

$$A^2 - 2A = \begin{bmatrix} 7 & 6 \\ 4 & 7 \end{bmatrix} - \begin{bmatrix} 2 & 6 \\ 4 & 2 \end{bmatrix} = \begin{bmatrix} 5 & 0 \\ 0 & 5 \end{bmatrix}$$

$$\text{Now } \begin{vmatrix} 5 & 0 \\ 0 & 5 \end{vmatrix} = 25$$

Video Solution:



Q27 Text Solution:

$$\text{Given, } A = \begin{bmatrix} 3 & 1 \\ -1 & 2 \end{bmatrix}$$

$$(\text{adj } A) = \begin{bmatrix} 2 & -1 \\ 1 & 3 \end{bmatrix}$$

$$|A| = 6 + 1 = 7$$

$$A^{-1} = \frac{1}{7} \begin{bmatrix} 2 & -1 \\ 1 & 3 \end{bmatrix}$$

Video Solution:



**Q28 Text Solution:**

$$3x + 4y + 7z = 4$$

$$2x - y + 3z = -3$$

$$x + 2y - 3z = 8$$

The system of equations can be written as

$$AX = B$$

$$\text{Where, } A = \begin{bmatrix} 3 & 4 & 7 \\ 2 & -1 & 3 \\ 1 & 2 & -3 \end{bmatrix}; X = \begin{bmatrix} x \\ y \\ z \end{bmatrix}$$

$$\text{and } B = \begin{bmatrix} 4 \\ -3 \\ 8 \end{bmatrix}$$

$$\text{Now, } |A| = \begin{vmatrix} 3 & 4 & 7 \\ 2 & -1 & 3 \\ 1 & 2 & -3 \end{vmatrix}$$

$$= 3(3 - 6) - 4(-6 - 3) + 7(4 + 1) = -9$$

$$+ 36 + 35 = 62 \neq 0$$

$\therefore A^{-1}$ exists. So, system of equations has a unique solution given by $X = A^{-1}B$

Now,

$$A_{11} = -3, A_{12} = 9, A_{13} = 5, A_{21} = 26, A_{22} = -16$$

$$A_{23} = -2, A_{31} = 19, A_{32} = 5, A_{33} = -11$$

$$\therefore \text{adj}A = \begin{bmatrix} -3 & 26 & 19 \\ 9 & -16 & 5 \\ 5 & -2 & -11 \end{bmatrix}$$

$$A^{-1} = \frac{1}{|A|} \cdot \text{adj}A$$

$$= \frac{1}{62} \begin{bmatrix} -3 & 26 & 19 \\ 9 & -16 & 5 \\ 5 & -2 & -11 \end{bmatrix}$$

$$\text{Now, } X = A^{-1}B$$

$$= \frac{1}{62} \begin{bmatrix} -3 & 26 & 19 \\ 9 & -16 & 5 \\ 5 & -2 & -11 \end{bmatrix} \begin{bmatrix} 4 \\ -3 \\ 8 \end{bmatrix}$$

$$= \frac{1}{62} \begin{bmatrix} 62 \\ 124 \\ -62 \end{bmatrix}$$

$$\Rightarrow \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 1 \\ 2 \\ -1 \end{bmatrix} \Rightarrow x = 1, y = 2, z =$$

$$-1$$

Video Solution:**Q29 Text Solution:**

The given points are collinear if

$$\begin{vmatrix} 1 & -5 & 1 \\ -4 & 5 & 1 \\ \lambda & 7 & 1 \end{vmatrix} = 0$$

$$\Rightarrow 1(-2) + 5(-4 - \lambda) + 1(-28 - 5\lambda)$$

$$= 0$$

$$\Rightarrow -50 - 10\lambda = 0 \Rightarrow \lambda = -5$$

Video Solution:**Q30 Text Solution:**

Put $x = 0$



$$\therefore \text{ We get } \begin{vmatrix} 3 & 0 & 2 \\ 0 & 1 & -1 \\ 2 & 0 & 1 \end{vmatrix}$$

We get

$$3 - 4 = -1$$

Video Solution:



[Android App](#) | [iOS App](#) | [PW Website](#)

