



2024 - 25

Moving Charges and Magnetism

Recall what did you study in previous class

Introduction

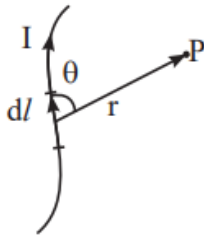
A static charge produces only electric field. A moving charge produces both electric field and magnetic field. A current carrying conductor produces only magnetic field.

Magnetic Field Produced By A Current Wire (Biot-Savart's Law)

The magnetic induction dB produced by an element dl carrying a current I at a distance r is given by:

$$dB = \frac{\mu_0 \mu_r}{4\pi} \frac{Idl \sin \theta}{r^2} \Rightarrow \vec{dB} = \frac{\mu_0 \mu_r}{4\pi} \frac{I(\vec{dl} \times \vec{r})}{r^3}$$

here the quantity Idl is called as current element.



μ = permeability of the medium = $\mu_0 \mu_r$

μ_0 = permeability of free space

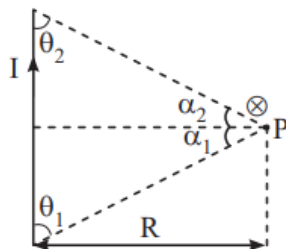
μ_r = relative permeability of the medium (Dimensionless quantity)

Unit of μ_0 & μ is NA^{-2} or Hm^{-1} ;

$\mu_0 = 4\pi \times 10^{-7} Hm^{-1}$

Magnetic Induction Due To a Straight Current Conductor

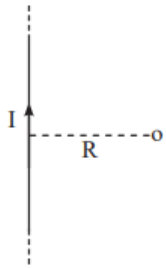
Magnetic induction due to a current carrying straight wire



$$B = \frac{\mu_0 I}{4\pi R} (\cos \theta_1 + \cos \theta_2) = \frac{\mu_0 I}{4\pi R} (\sin \alpha_1 + \sin \alpha_2)$$

Magnetic induction due to a infinitely long wire $B = \frac{\mu_0 I}{2\pi R} \otimes$

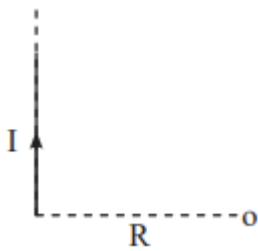
$\alpha_1 = 90^\circ, \alpha_2 = 90^\circ$



Magnetic induction due to semi infinite straight conductor

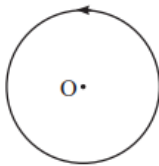
$$B = \frac{\mu_0 I}{4\pi R} \otimes$$

$$\alpha = 0^\circ; \alpha_2 = 90^\circ$$



Magnetic field due to a flat circular coil carrying a current:

- (i) At its centre $B = \frac{\mu_0 NI}{2R}$



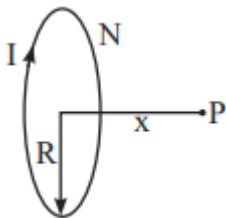
where

N = total number of turns in the coil

I = Current in the coil

R = Radius of the coil

- (ii) On the axis $B = \frac{\mu_0 NIR^2}{2(x^2 + R^2)^{3/2}}$



Where x = distance of the point from the centre.

It is maximum at the centre $B_c = \frac{\mu_0 NI}{2R}$

- (iii) Magnetic field due to – flat circular ARC:

$$B = \frac{\mu_0 I \theta}{4\pi R}$$



Magnetic field due to infinite long solid cylindrical conductor of radius R

$$\text{For } r \geq R: B = \frac{\mu_0 I}{2\pi r}$$

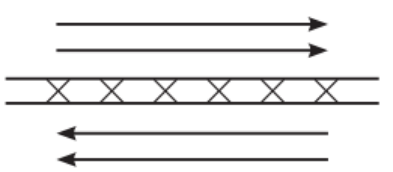
$$\text{For } r < R: B = \frac{\mu_0 I r}{2\pi R^2}$$

Magnetic Induction Due to Solenoid

- $B = \mu_0 n I$, direction along axis
Where $n \rightarrow$ number of turns meter;
 $I \rightarrow$ current

Magnetic Induction Due To Current Carrying Sheet

- $B = \frac{1}{2} \mu_0 \lambda$, where $\lambda =$ Linear current density (A/m)



Ampere's Circuital Law

$$\oint \vec{B} \cdot d\vec{l} = \mu \sum I = \text{algebraic sum of all the current.}$$

Motion of A Charge In Uniform Magnetic Field

(a) When $\vec{V} \parallel \vec{B}$; Motion will be in a straight line and $\vec{F} = 0$

(b) When $\vec{V} \perp \vec{B}$: Motion will be in circular path with radius

$$R = \frac{mv}{qB} \text{ and angular velocity } \omega = \frac{qB}{m} \text{ and } F = qvB.$$

(c) When \vec{V} is at $\angle \theta$ to \vec{B} : Motion will be helical with radius

$$R_k = \frac{mv \sin \theta}{qB} \text{ and pitch } P_H = \frac{2\pi mv \cos \theta}{qB} \text{ and } F = qvB \sin \theta$$

Lorentz Force

An electric charge 'q' moving with a velocity \vec{V} through a magnetic field of magnetic induction \vec{B} experiences a force \vec{F} , given by $\vec{F} = q\vec{v} \times \vec{B}$. Therefore, if the charge moves in a space where both electric and magnetic fields are superposed.

$\vec{F} =$ net electromagnetic force on the charge $= q\vec{E} + q\vec{v} \times \vec{B}$. This force is called the Lorentz Force



Motion of Charge In Combined Electric Field & Magnetic Field

When $\vec{v} \parallel \vec{B}$ & $\vec{v} \parallel \vec{E}$, Motion will be uniformly accelerated in a straight line as $F_{\text{magnetic}} = 0$ and $F_{\text{electrostatic}} = qE$

So the particle will be either speeding up or speeding down

When $\vec{v} \parallel \vec{B}$ & $\vec{v} \perp \vec{E}$, motion will be uniformly accelerated in a parabolic path

When $\vec{v} \perp \vec{B}$ & $\vec{v} \perp \vec{E}$, the particle will move undeflected & undeviated with same uniform speed if $v = \frac{E}{B}$

Magnetic Force On A straight Current Carrying Wire :

$$\vec{F} = I(\vec{L} \times \vec{B})$$

I = current in the straight conductor

\vec{L} = displacement between the ends of the conductor in the direction of the current in it

\vec{B} = magnetic induction. (Uniform throughout the length of conductor)

Note : In general, force is $\vec{F} = \int I(d\vec{l} \times \vec{B})$

Magnetic Interaction Force Between Two Parallel Long Straight Currents

The interactive force between two parallel long straight wires is:

(i) Repulsive if the currents are anti-parallel

(ii) Attractive if the currents are parallel.

This force per unit length on either conductor is given by

$$F = \frac{\mu_0}{2\pi} \frac{I_1 I_2}{r}$$

Where r = perpendicular distance between the parallel conductors

Magnetic Torque On a current loop

When a plane current loop of 'N' turns and of area 'A' per turn carrying a current I is placed in uniform magnetic field, it experiences zero net force, but experiences a torque given by $\vec{\tau} = NI\vec{A} \times \vec{B} = \vec{M} \times \vec{B} = BINAsin\theta$ where \vec{A} = area vector outward from the face of the circuit where the current is anticlockwise, \vec{B} = magnetic induction of the uniform magnetic field.

\vec{M} = magnetic moment of the current circuit = $NI\vec{A}$

Force on A Random Shaped Conductor in A Uniform Magnetic Field



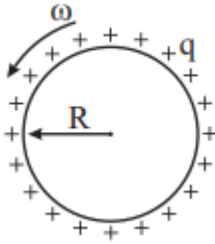
Magnetic force on a closed loop in a uniform \vec{B} is zero.

Force experienced by a wire of any shape is equivalent to force on a wire joining points A & B in a uniform magnetic field.

Magnetic Moment of A Rotating Charge

If a charge q is rotating at an angular velocity ω , its equivalent current is given as $I = \frac{q\omega}{2\pi}$ & its magnetic moment

$$\text{is } M = IpR^2 = \frac{1}{2}q\omega R^2$$



Key Note

The ratio of magnetic moment to angular momentum of a uniform rotating object which is charged uniformly is always a constant, irrespective of the shape of conductor $M/L = q/2m$.

Magnetic dipole

Magnetic moment $M = m \times 2l$ where m = pole strength of the magnet

Magnetic field at axial point (or End-on) of dipole \vec{B}

$$= \vec{B} = \frac{\mu_0}{4\pi} \frac{(-\vec{M})}{r^3}$$

At a point which is at a distance r from midpoint of dipole and making angle θ with dipole axis.

$$\text{Magnetic field } B = \frac{\mu_0}{4\pi} \frac{M\sqrt{1+3\cos^2\theta}}{r^3}$$

Torque on dipole placed in uniform magnetic field $M \times B$

Potential energy of dipole placed in an uniform field

$$U = -\vec{M} \cdot \vec{B}$$

Intensity of magnetisation $I = M/V$

Magnetic induction $B = m_H = m_0(H + I)$

Magnetic permeability $\mu = \frac{B}{H}$

Magnetic susceptibility $\chi_m = \frac{1}{H} = \mu - 1$

Curies Law for paramagnetic materials $\chi_m \propto \frac{1}{T}$

Curie-Wiess law for $\chi_m \propto \frac{1}{T - T_C}$ Ferromagnetic materials

Where T_C = Curie temperature



PW Web/App - <https://smart.link/7wwosivoicgd4>

Library- <https://smart.link/sdfez8ejd80if>